

pn junctions

pn junctions are found in:

diodes

solar cells

LEDs

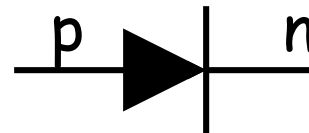
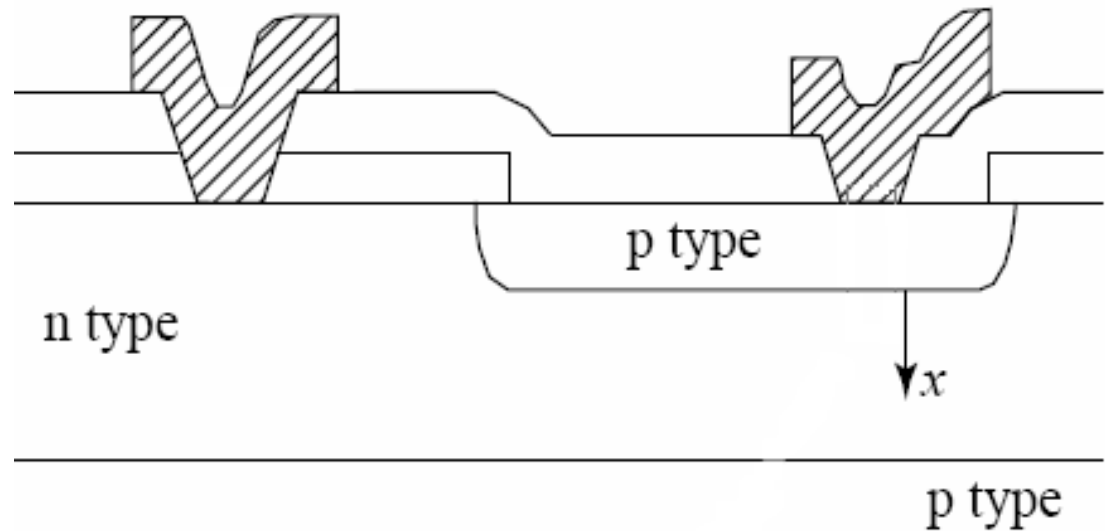
isolation

JFETs

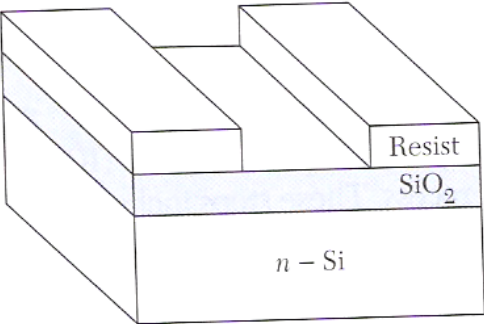
bipolar transistors

MOSFETs

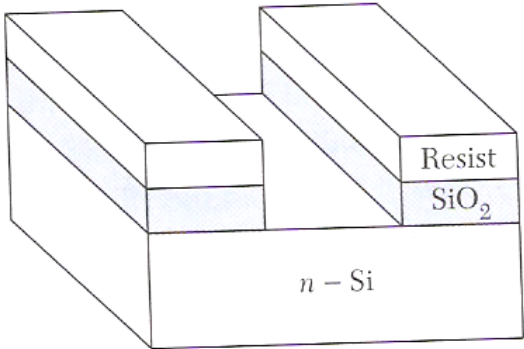
solid state lasers



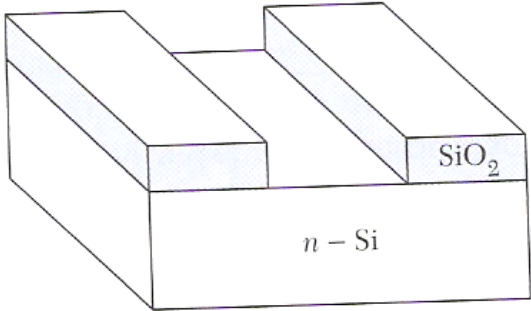
diode fabrication



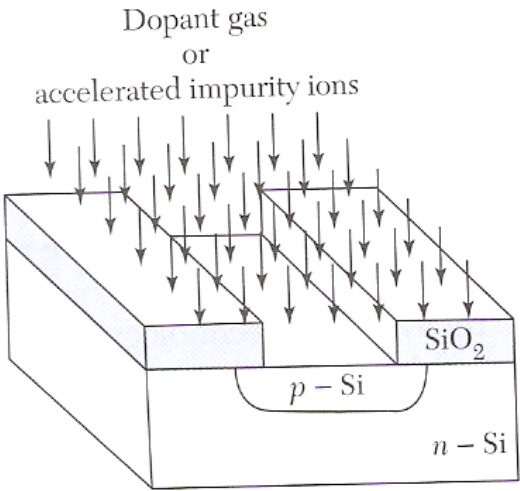
(a)



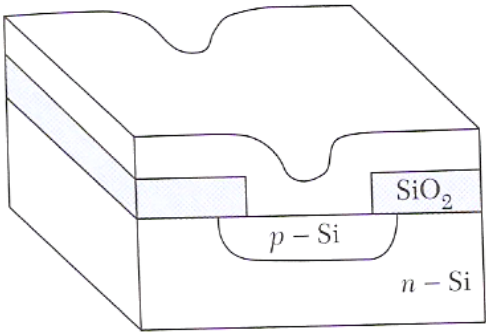
(b)



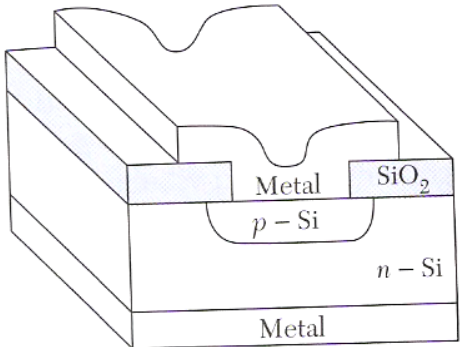
(c)



(d)

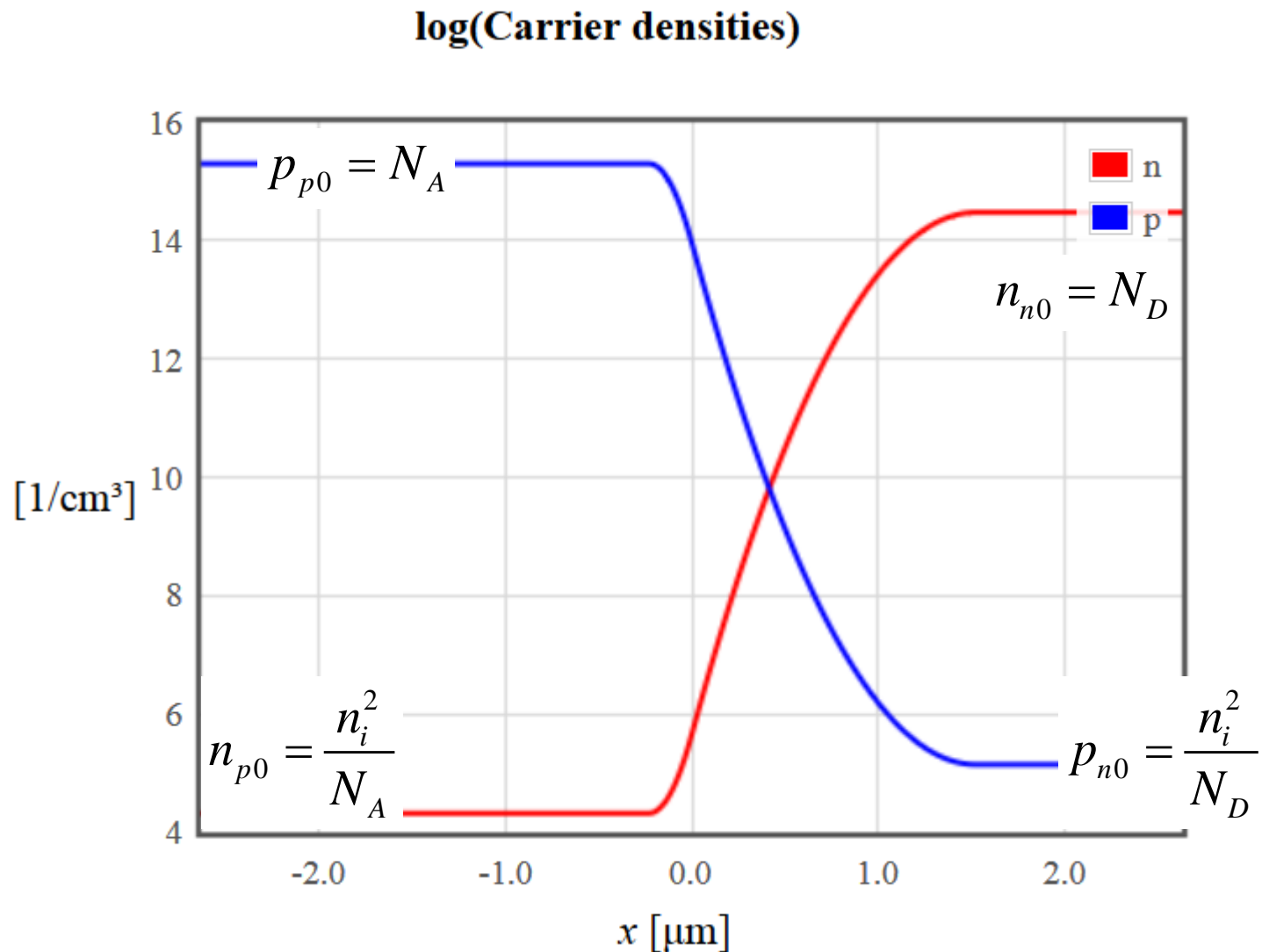


(e)



(f)

Equilibrium concentrations, $V = 0$

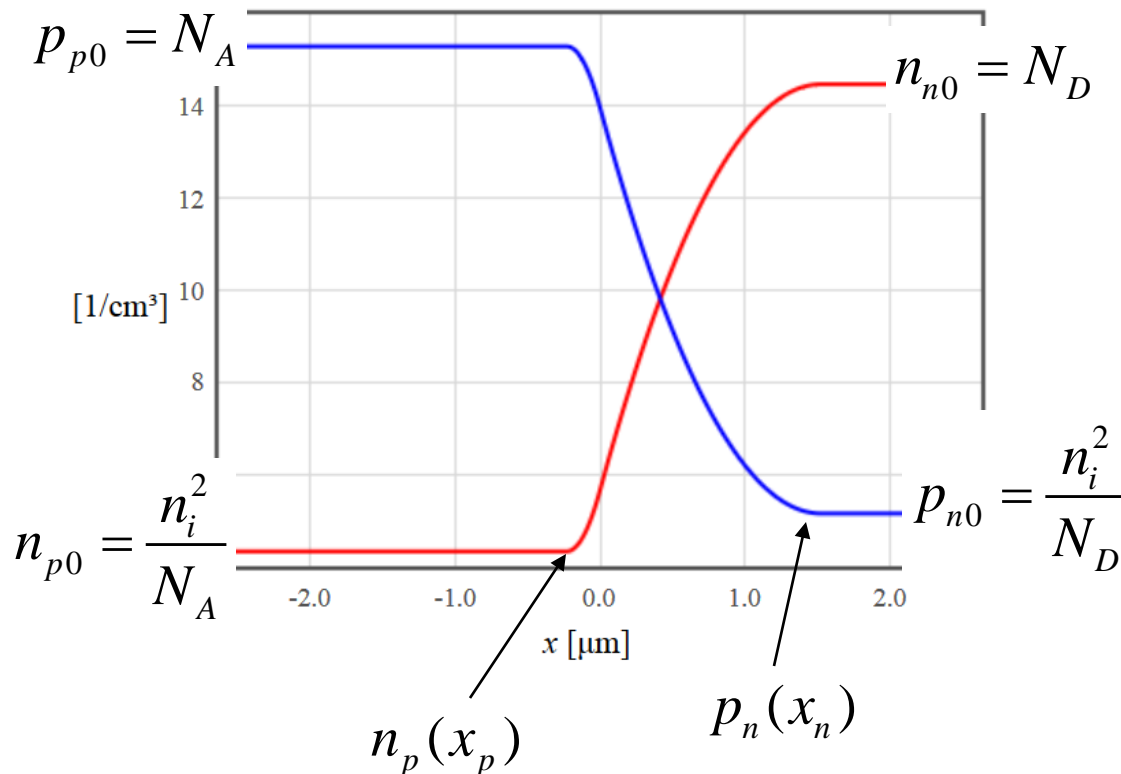


$$n_{p0}p_{p0} = n_{n0}p_{n0} = n_i^2$$

Bias voltage, $V = 0$

$$eV_{bi} = k_B T \ln\left(\frac{N_D N_A}{n_i^2}\right) = k_B T \ln\left(\frac{N_D}{n_{p0}}\right) = k_B T \ln\left(\frac{N_A}{p_{n0}}\right)$$

log(Carrier densities)



$$n_{p0} p_{p0} = n_{n0} p_{n0} = n_i^2$$

$$V = 0$$

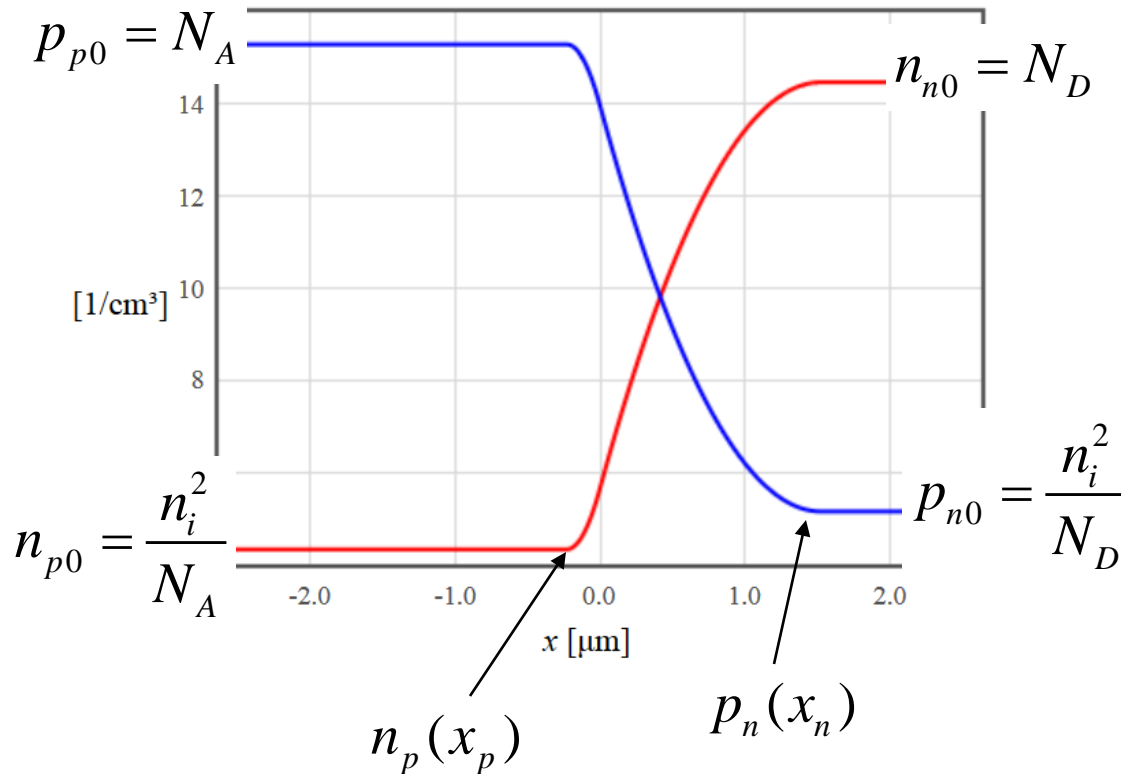
$$n_{p0} = N_D \exp\left(\frac{-eV_{bi}}{k_B T}\right)$$

$$p_{n0} = N_A \exp\left(\frac{-eV_{bi}}{k_B T}\right)$$

Bias voltage, $V \neq 0$

$$eV_{bi} = k_B T \ln \left(\frac{N_D N_A}{n_i^2} \right) = k_B T \ln \left(\frac{N_D}{n_{p0}} \right) = k_B T \ln \left(\frac{N_A}{p_{n0}} \right)$$

log(Carrier densities)



$$n_{p0} p_{p0} = n_{n0} p_{n0} = n_i^2$$

$V = 0$

$$n_{p0} = N_D \exp \left(\frac{-eV_{bi}}{k_B T} \right)$$

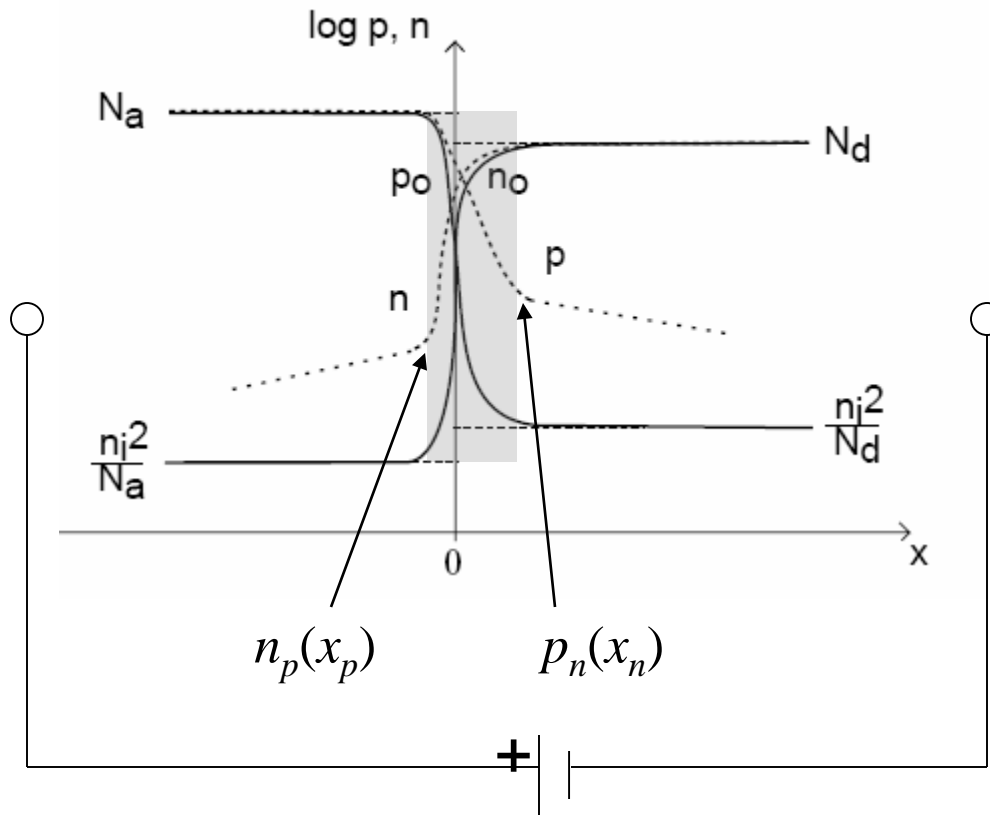
$$p_{n0} = N_A \exp \left(\frac{-eV_{bi}}{k_B T} \right)$$

$V \neq 0$

$$n_p(x_p) = N_D \exp \left(\frac{-e(V_{bi} - V)}{k_B T} \right)$$

$$p_n(x_n) = N_A \exp \left(\frac{-e(V_{bi} - V)}{k_B T} \right)$$

Forward bias, $V > 0$



Electrons and holes are driven towards the junction.
The depletion region becomes narrower

$$n_p(x_p) = N_D \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

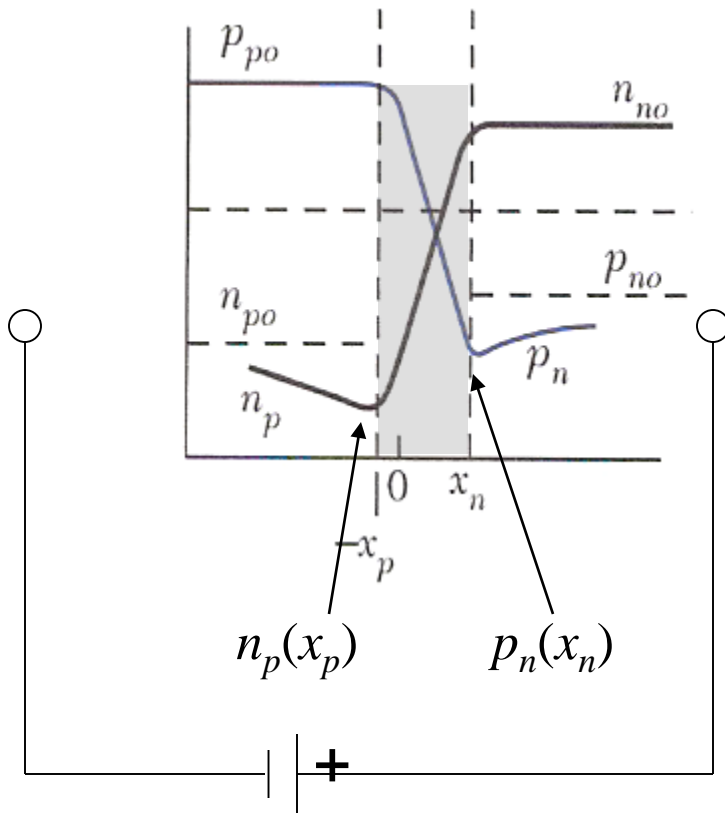
$$p_n(x_n) = N_A \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

Minority electrons are injected into the p-region
Minority holes are injected into the n-region

Reverse bias, $V < 0$

Electrons and holes are driven away from the junction.

The depletion region becomes wider



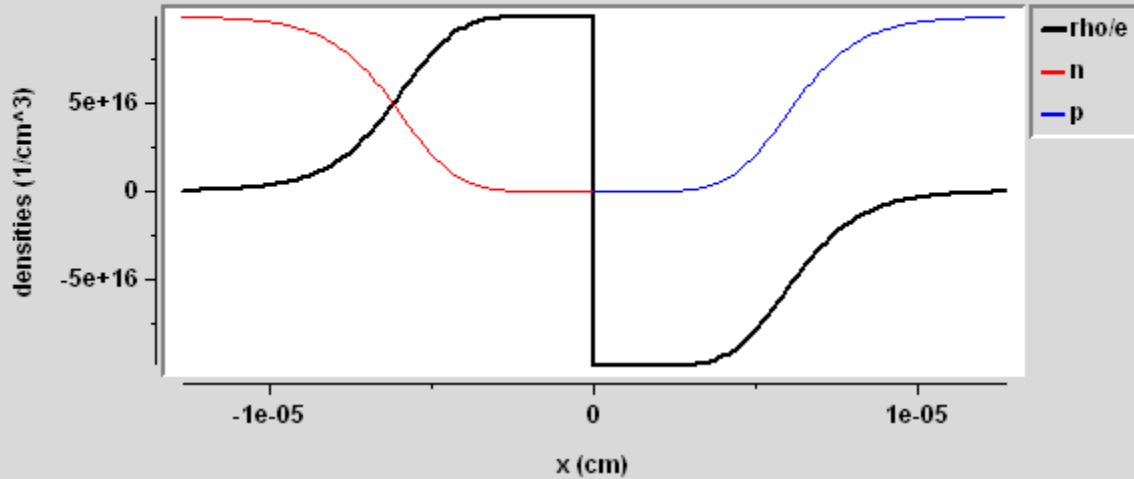
$$n_p(x_p) = N_D \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

$$p_n(x_n) = N_A \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

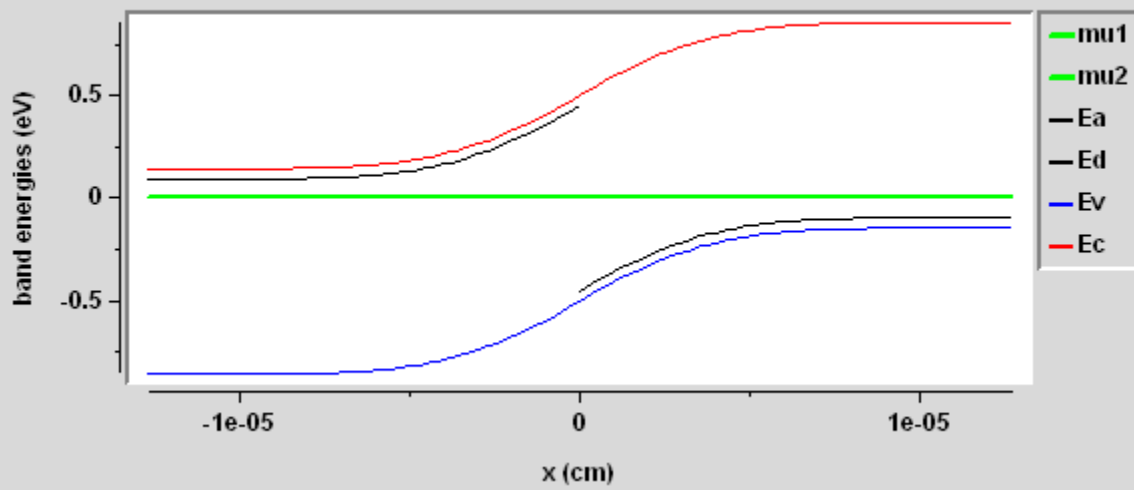
Minority electrons are extracted from the p-region by the electric field
Minority holes are extracted from the n-region by the electric field

C:\Program Files\Cornell\SSS\winbin\poisson.exe

quit display: large configure... presets help...



device: pn junction
solution: 'exact'
Nd ($1/\text{cm}^3$): 1.00×10^{17}
Na ($1/\text{cm}^3$): 1.00×10^{17}
Egap (eV): 1
Vapplied (V): 0



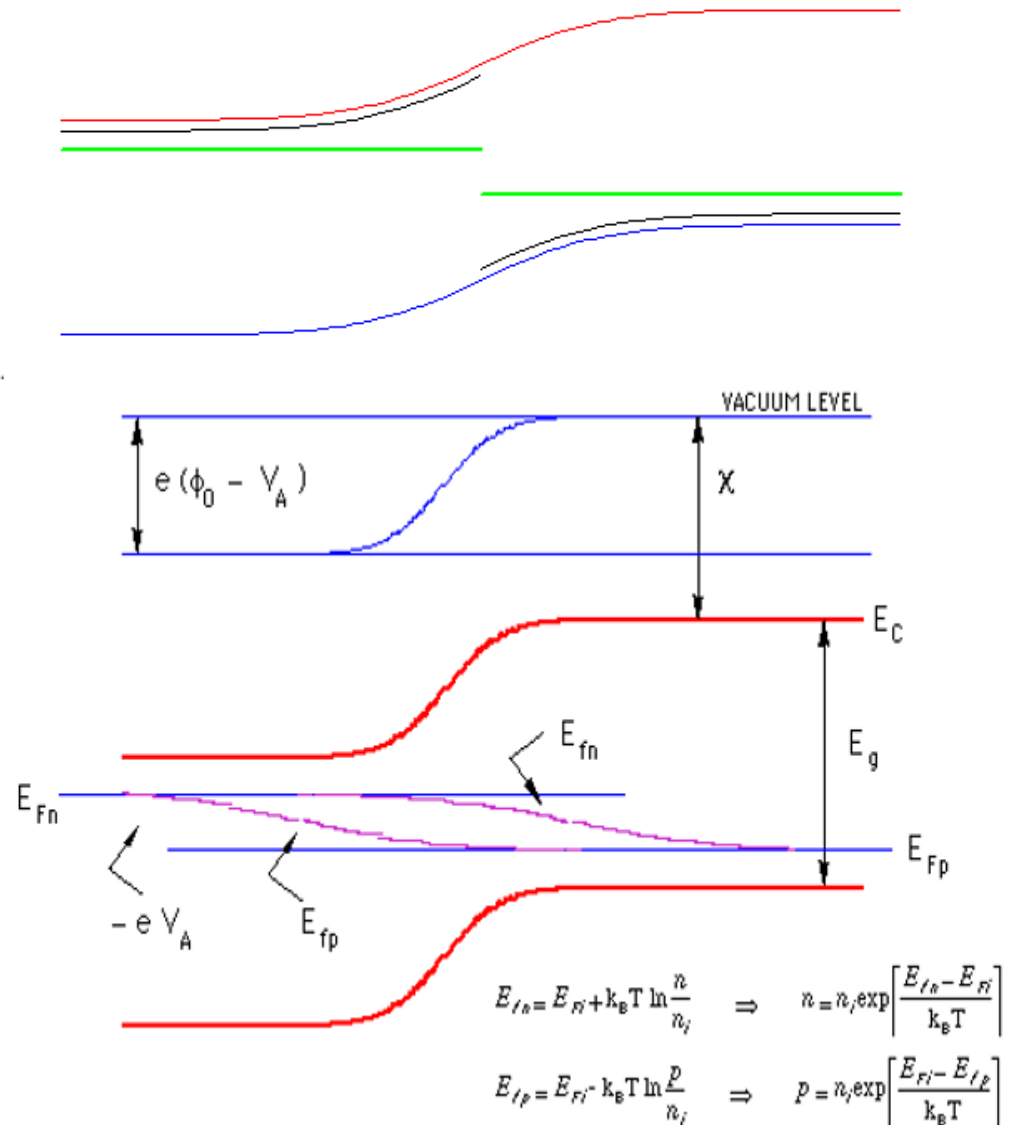
Qdepl= 6.47×10^{11} ($\#/\text{cm}^2$)
copy densities
copy energies
autoscale

Quasi Fermi level

When the charge carriers are not in equilibrium the Fermi energy can be different for electrons and holes.

$$n = N_c \exp\left(\frac{E_{Fn} - E_c}{k_B T}\right)$$

$$p = N_v \exp\left(\frac{E_v - E_{Fp}}{k_B T}\right)$$



Student Projects

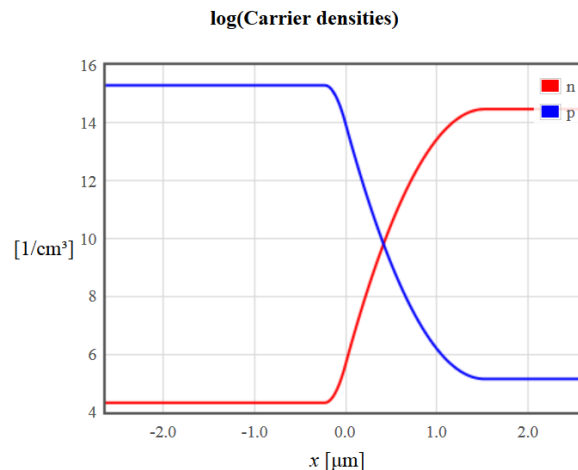
Write derivation of V_{bi} , $n_p(x_p)$, and $p_n(x_n)$ in mathjax

The electric field can be calculated by integrating Gauss's law for the positive and the negative charged regions,

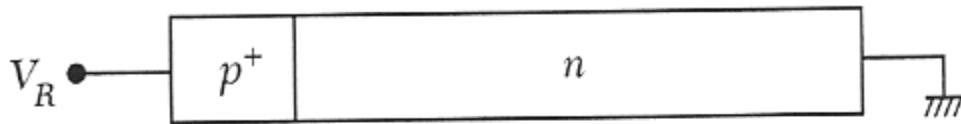
$$\frac{dE}{dx} = \frac{\rho}{\epsilon_r \epsilon_0}$$

$$E_p = \frac{-eN_A}{\epsilon_r \epsilon_0} \int dx = \frac{-eN_A}{\epsilon_r \epsilon_0} x + c_1 \quad E_n = \frac{eN_D}{\epsilon_r \epsilon_0} \int dx = \frac{eN_D}{\epsilon_r \epsilon_0} x + c_2$$

Write program to plot n and p with a bias



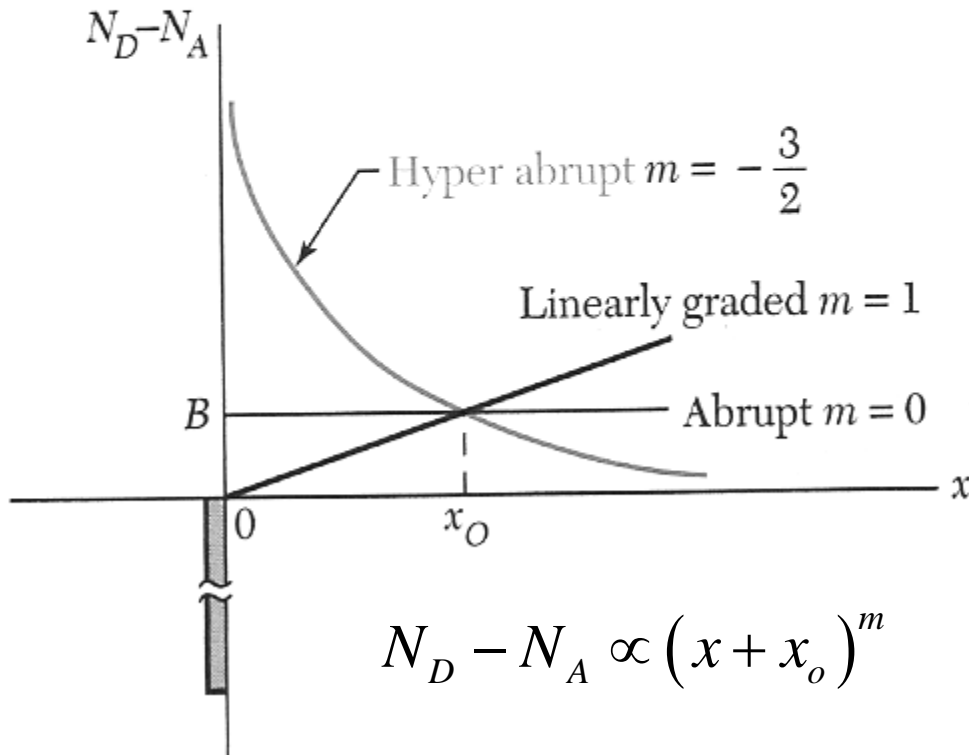
Varactor



$$C_j \propto (V_{bi} + V_R)^{-n}$$

abrupt: $n = 1/2$

linearly graded: $n = 1/3$



$$n = 1/(m+2)$$

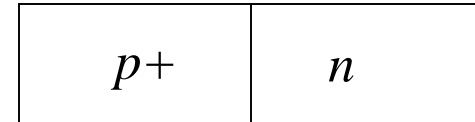


Capacitance-voltage characteristics

specific capacitance $C_j = \frac{\epsilon}{W} \text{ F m}^{-2}$

abrupt junction: $W = \frac{\epsilon}{C_j} = \sqrt{\frac{2\epsilon(N_D + N_A)(V_{bi} - V)}{eN_D N_A}}$

a one sided abrupt junction in reverse bias:



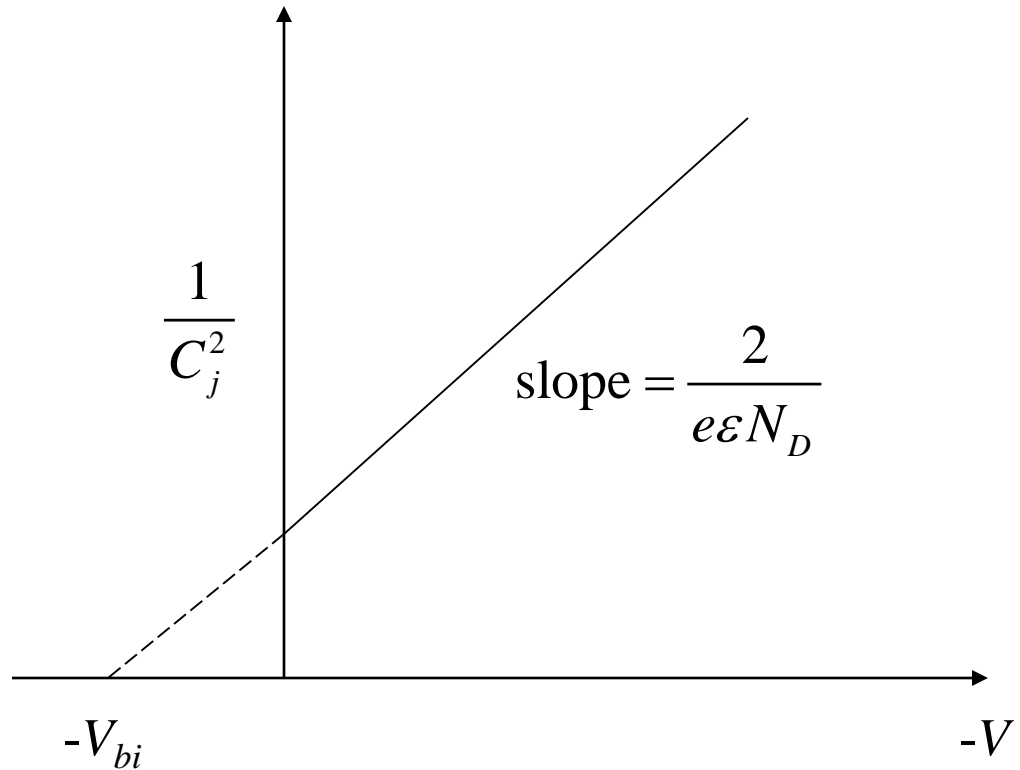
$$\frac{1}{C_j^2} = \frac{2(V_{bi} - V)}{e\epsilon N_D}$$

Capacitance-voltage characteristics

a one sided abrupt
junction in reverse
bias:

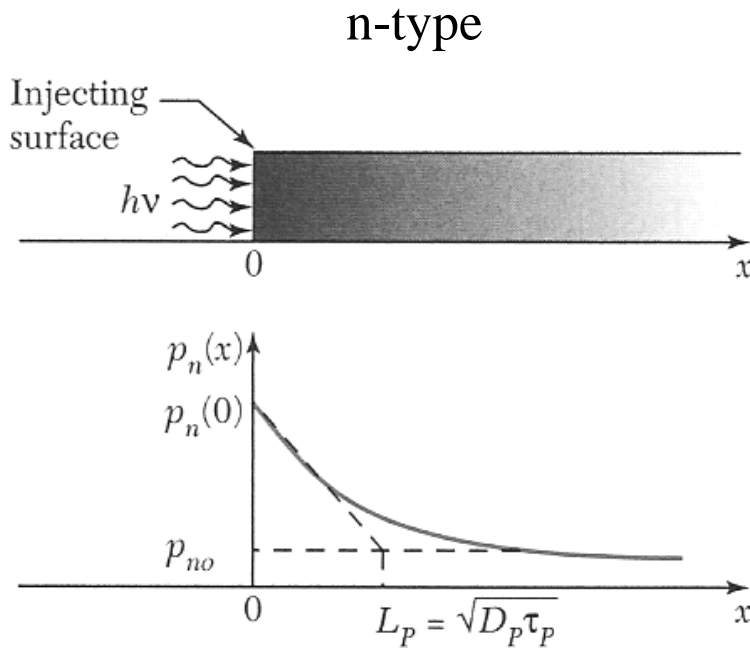
$p+$	n
------	-----

$$\frac{1}{C_j^2} = \frac{2(V_{bi} - V)}{e\epsilon N_D}$$



slope gives impurity concentration and the intercept gives V_{bi}

Review of Diffusion



$$D_p \frac{\partial^2 p_n}{\partial x^2} = \frac{p_n - p_{n0}}{\tau_p}$$

↑
recombination time

$$p_n(x) = p_{n0} + (p_n(0) - p_{n0}) \exp\left(\frac{-x}{L_p}\right)$$

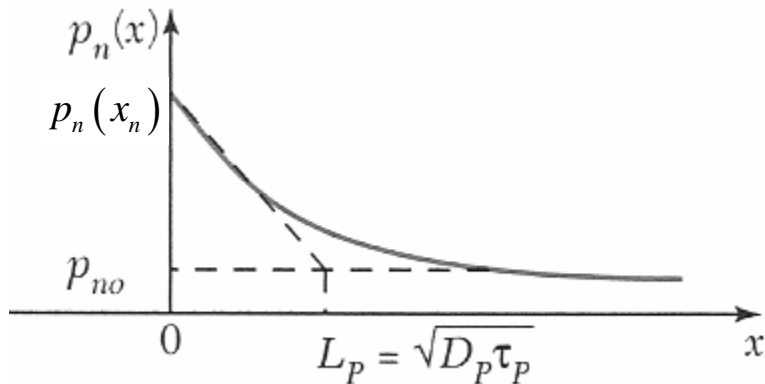
$$L_p = \sqrt{D_p \tau_p}$$

↑
diffusion length

Injection only occurs at the surface. There the minority carrier density is $p_n(0)$.

Diffusion current

n-type



$$p_n(x) = p_{n0} + (p_n(x_n) - p_{n0}) \exp\left(\frac{-x}{L_p}\right)$$

$$J_{diff,p} = -eD_p \frac{dp}{dx}$$

$$J_{diff,p} = -eD_p \frac{dp}{dx} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p} \exp\left(\frac{-x}{L_p}\right)$$

At the edge of the depletion region:

$$J_{diff,p} = -eD_p \frac{dp}{dx} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p}$$

Diffusion current

$$J_{diff,p} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p}$$

$p_n(x_n) = p_{p0} \exp\left(-\frac{e(V_{bi} - V)}{k_B T}\right)$

$$J_{diff,p} = \left(p_{p0} \exp\left(-\frac{e(V_{bi} - V)}{k_B T}\right) - p_{n0} \right) \frac{eD_p}{L_p}$$

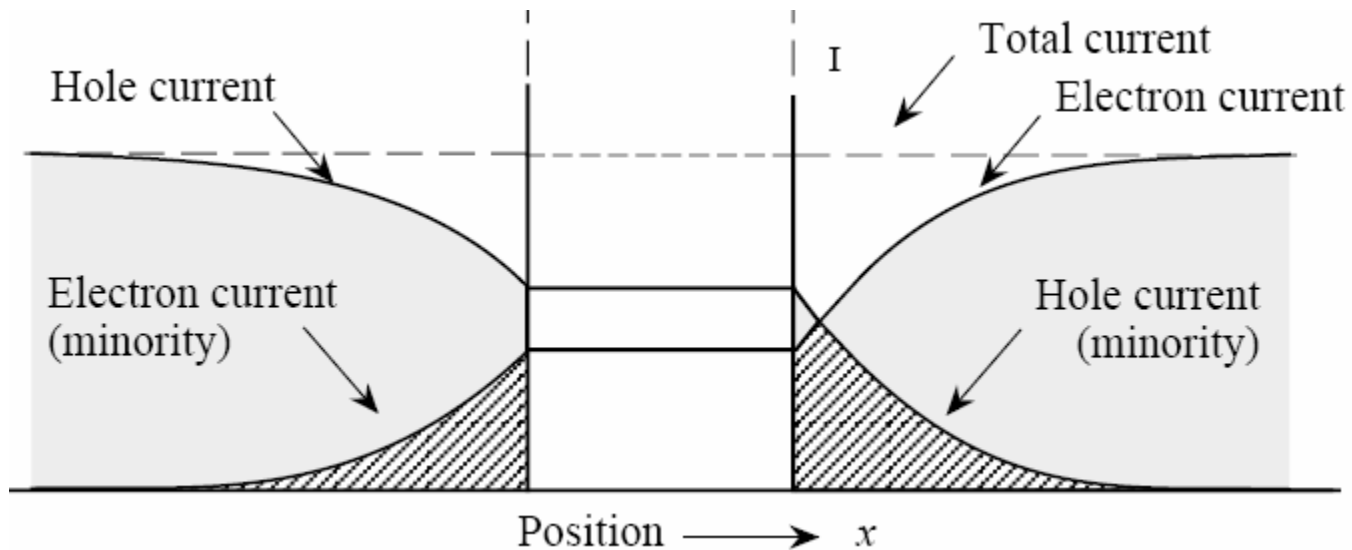
$p_{p0} = p_{n0} \exp\left(\frac{eV_{bi}}{k_B T}\right)$

$$J_{diff,p} = p_{n0} \frac{eD_p}{L_p} \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

Diffusion current

$$J_{diff,p} = \frac{p_{n0} e D_p}{L_p} \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

$$J_{diff,n} = \frac{n_{p0} e D_n}{L_n} \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

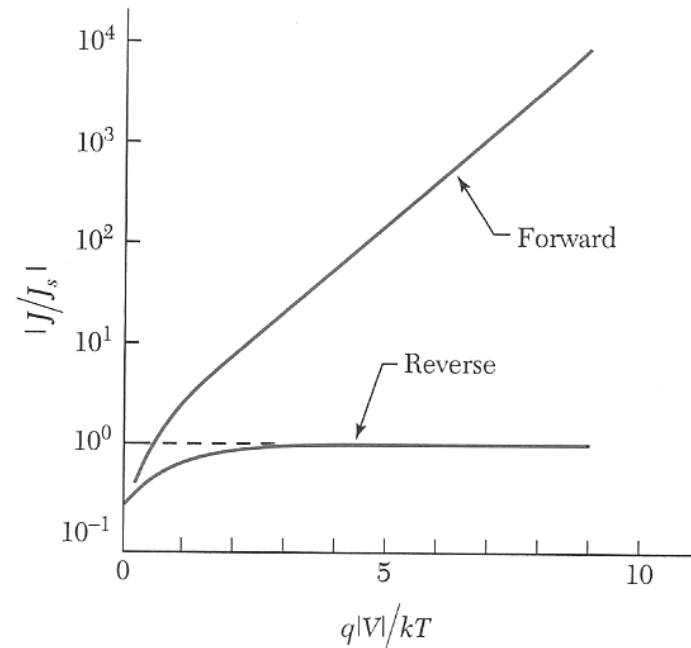
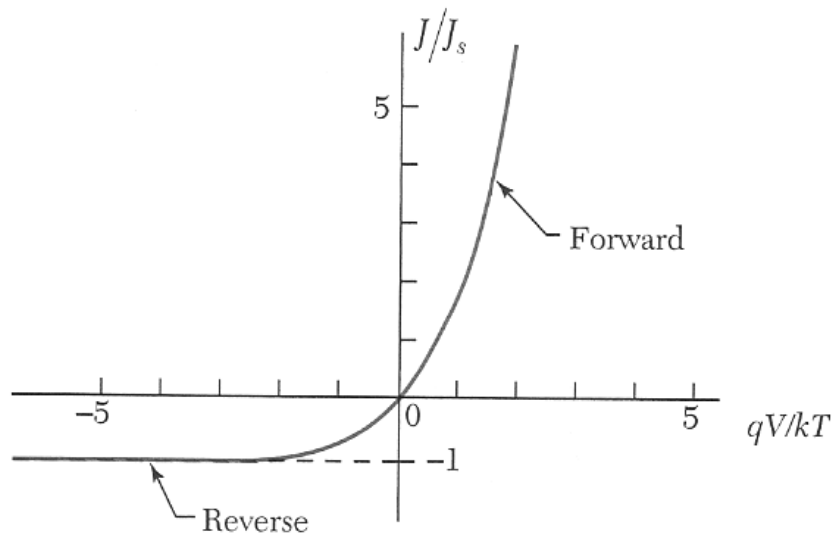


Diode current

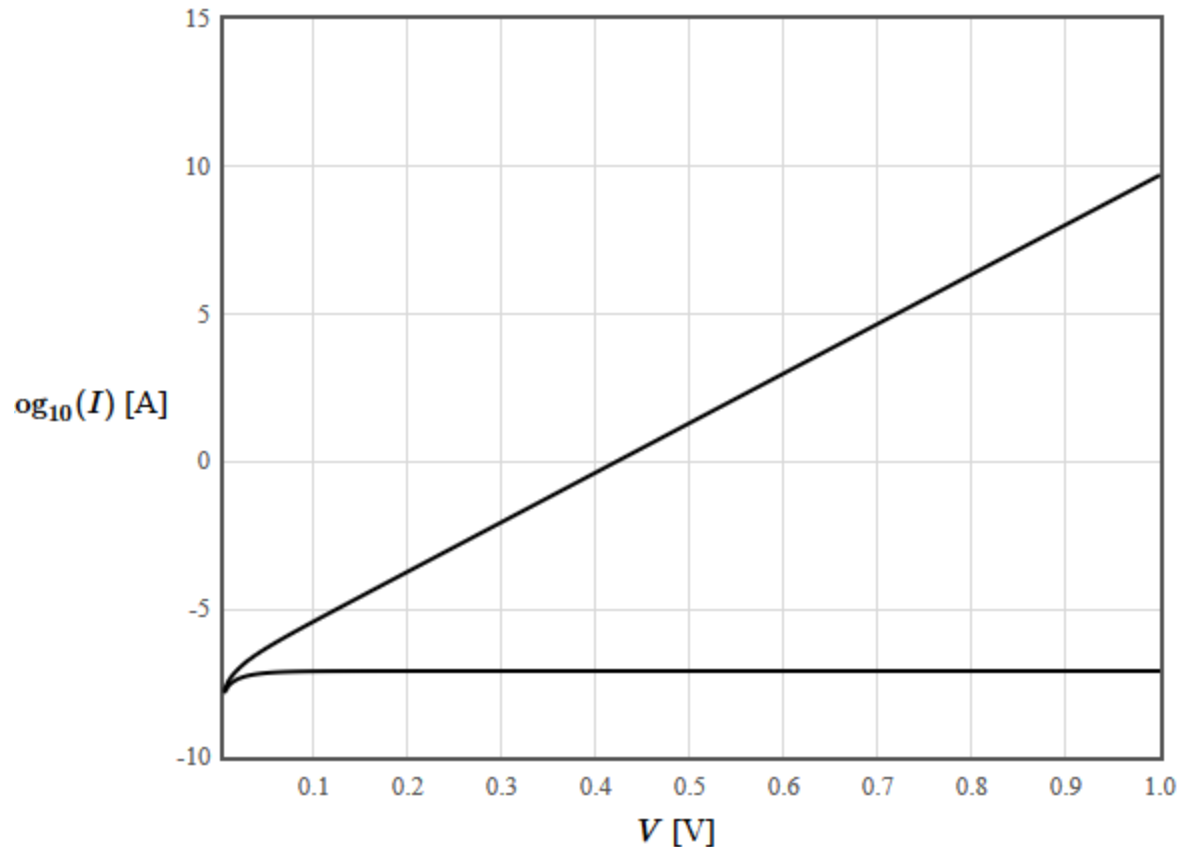
$$I = eA \left(\frac{p_{n0} D_p}{L_p} + \frac{n_{p0} D_n}{L_n} \right) \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right) = I_s \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

Area

Saturation current



Diode I-V characteristics



Simulation parameters for a diode:

- $A = 1\text{E-}3$ cm²
- $N_c(300\text{K}) = 1.04\text{E}19$ cm⁻³
- $N_v(300\text{K}) = 6.0\text{E}18$ cm⁻³
- $E_g = 0.7437 - 4.77\text{E-}4 * T * T / (T + 235)$ eV
- $\mu_p = 1900$ cm²/Vs
- $\tau_p = 1\text{E-}8$ s
- $N_a = 1\text{E}17$ cm⁻³
- $\mu_n = 3900$ cm²/Vs
- $\tau_n = 1\text{E-}8$ s
- $N_d = 5\text{E}17$ cm⁻³
- $T = 300$ K

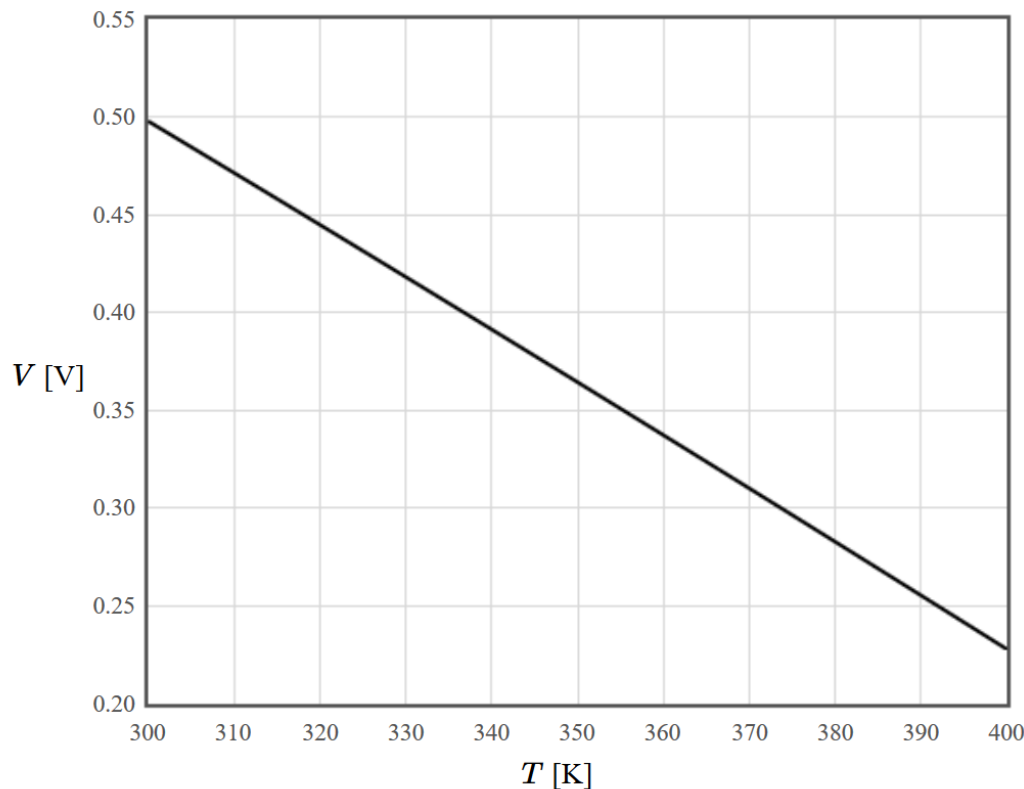
Material selection:

Thermometer

$$I_S = Aen_i^2 \left(\frac{D_p}{L_p N_d} + \frac{D_n}{L_n N_a} \right)$$

$$n_i = \sqrt{N_c \left(\frac{T}{300} \right)^{3/2} N_v \left(\frac{T}{300} \right)^{3/2} \exp\left(\frac{-E_g}{2k_B T} \right)}$$

$$D_n = \frac{\mu_n k_B T}{e}$$



Simulation parameters:

- $A = 1\text{E-}3$ cm²
- $N_c(300\text{K}) = 2.78\text{E}19$ cm⁻³
- $N_v(300\text{K}) = 9.84\text{E}18$ cm⁻³
- $E_g = 1.166 - 4.73\text{E-}4 * T * T / (T + 636)$ eV
- $\mu_p = 480$ cm²/Vs
- $\tau_p = 1\text{E-}8$ s
- $N_a = 1\text{E}17$ cm⁻³
- $\mu_n = 1350$ cm²/Vs
- $\tau_n = 1\text{E-}8$ s
- $N_d = 5\text{E}17$ cm⁻³
- $T_{start} = 300$ K
- $T_{stop} = 400$ K
- $I = 1\text{E-}6$ A

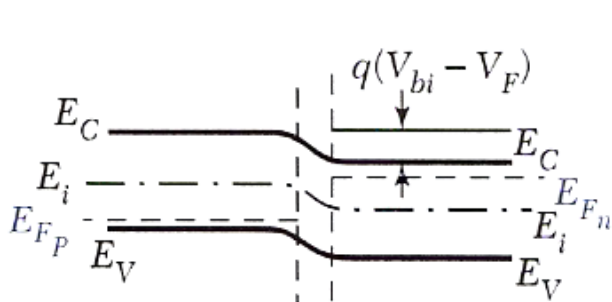
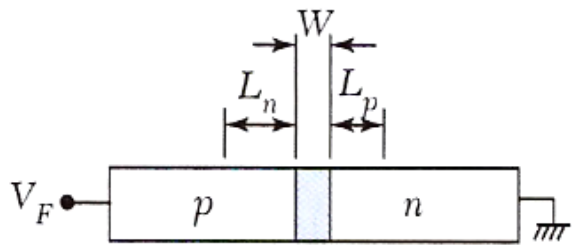
Replot

Si

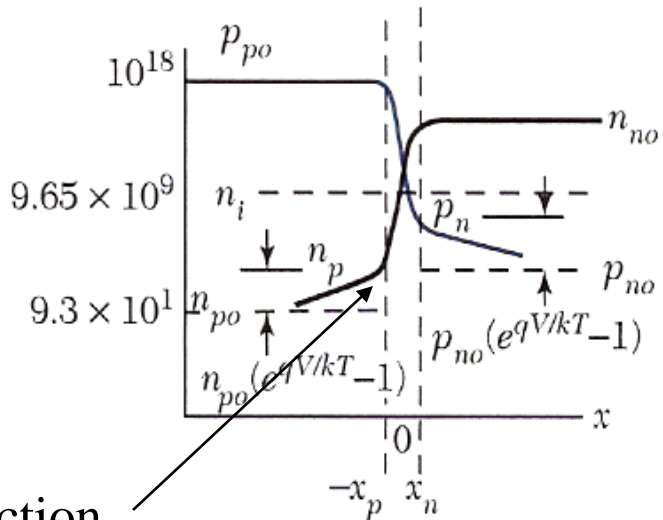
Ge

GaAs

Forward

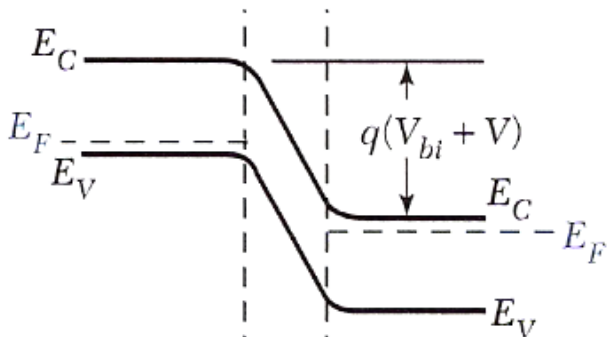
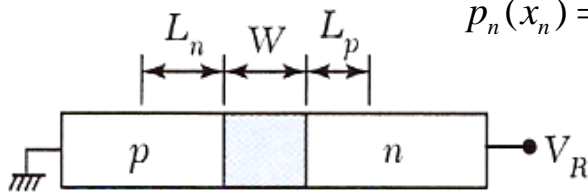


$$J_{diff} > J_{drift}$$

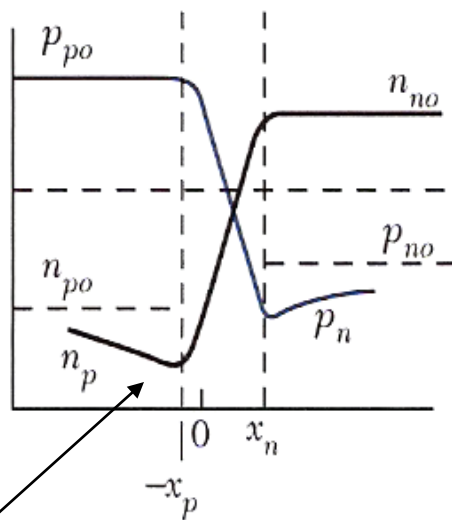


Injection

Reverse



$$J_{diff} < J_{drift}$$



Extraction

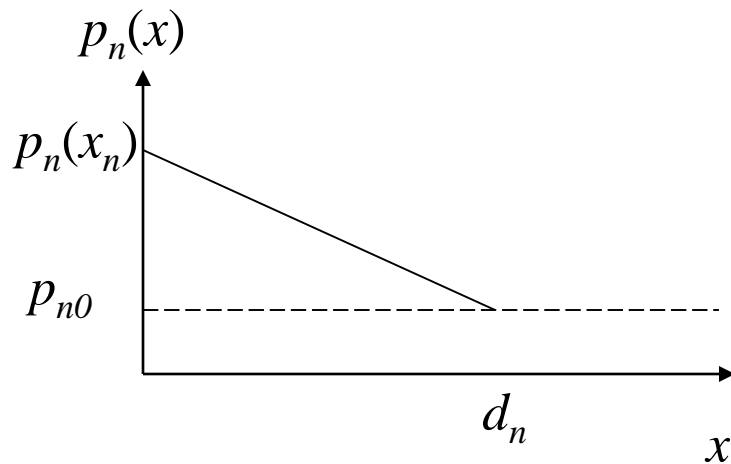
$$n_p(x_p) = N_D \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

$$p_n(x_n) = N_A \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

Short diode

n-type

$$d_n \ll L_p$$



Metal contact is much closer to the depletion region than the diffusion length

$$J_{diff,p} = -eD_p \frac{dp}{dx}$$

$$J_{diff,p} = -eD_p \frac{dp}{dx} = \frac{eD_p}{d_n} (p_n(x_n) - p_{n0})$$

Diffusion current

$$J_{diff,p} = (p_n(x_n) - p_{n0}) \frac{eD_p}{d_n}$$

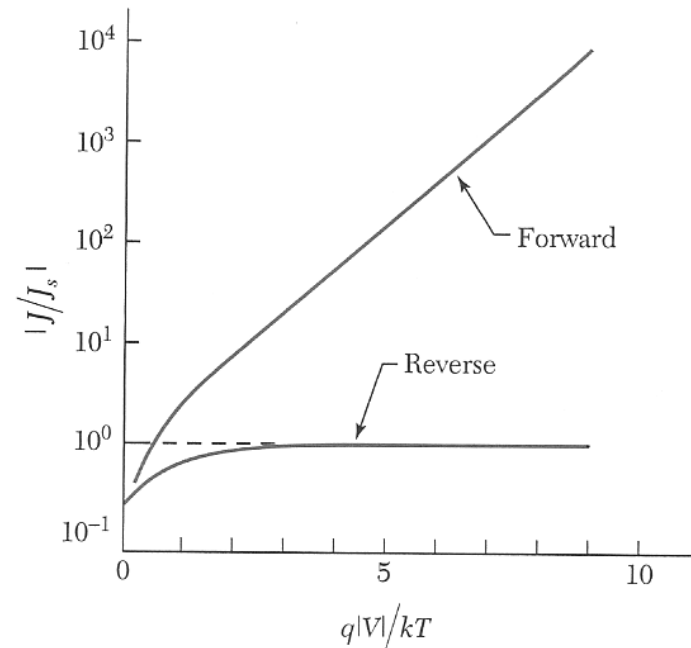
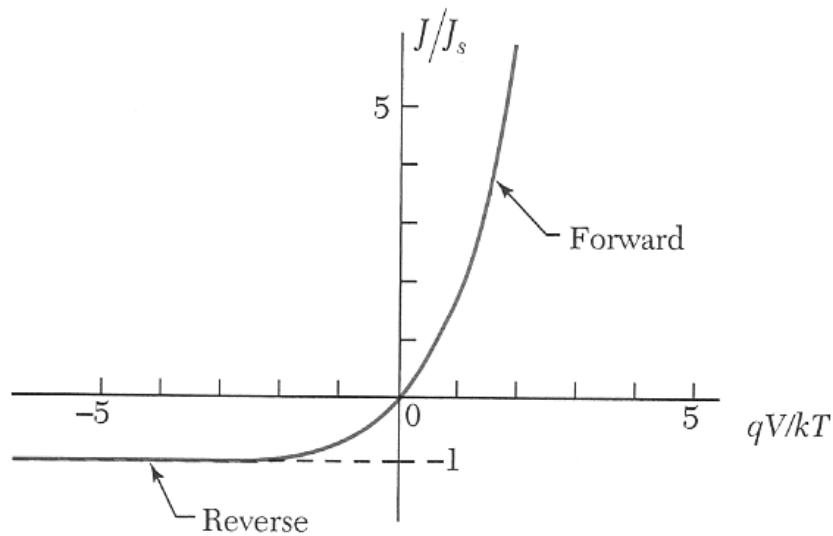
$$J_{diff,p} = \left(p_{n0} \exp\left(\frac{e(V)}{k_B T}\right) - p_{n0} \right) \frac{eD_p}{d_n}$$

$$J_{diff,p} = \frac{p_{n0} eD_p}{d_n} \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

Short diode current

$$I = eA \left(\frac{p_{n0} D_p}{d_n} + \frac{n_{p0} D_n}{d_p} \right) \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right) = I_s \left(\exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

Area

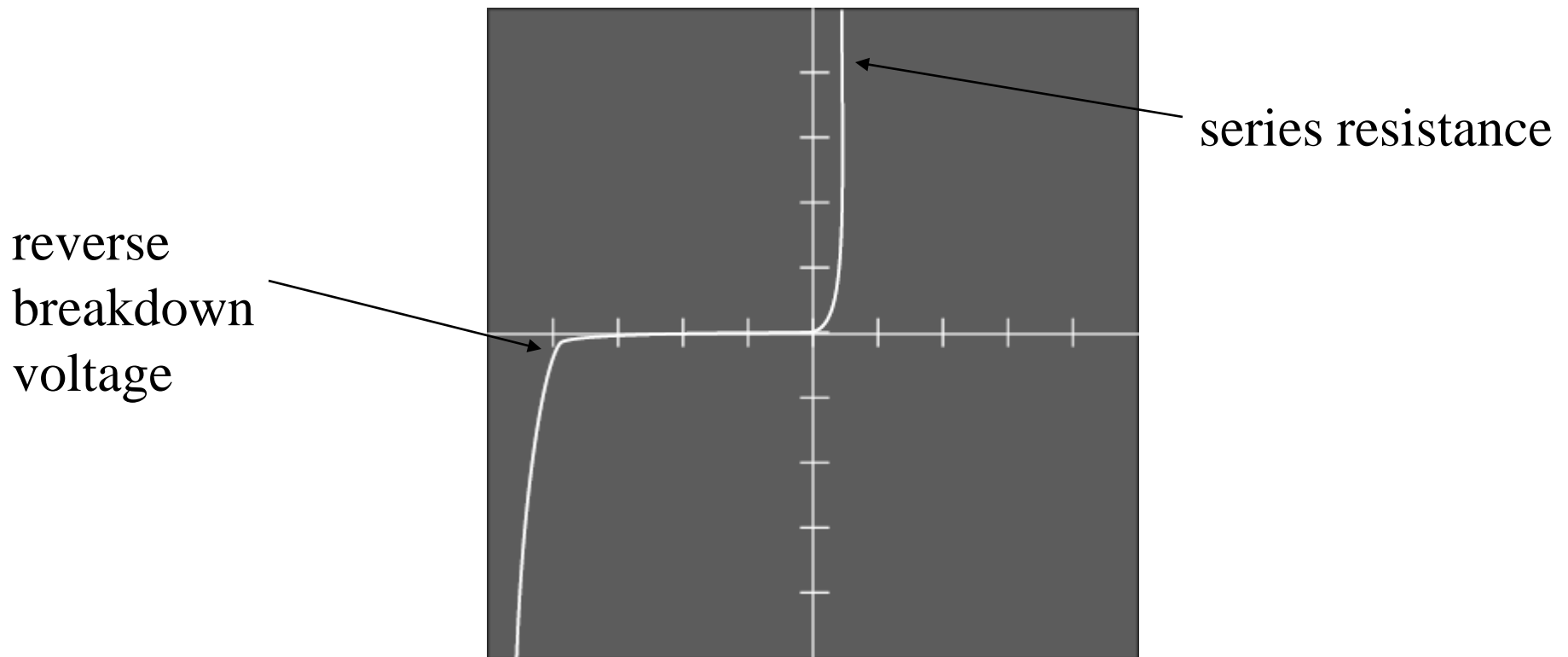


Real diodes

$$I = I_s \left(\exp\left(\frac{eV}{nk_B T}\right) - 1 \right)$$

n = nonideality factor

$n = 1$ for an ideal diode



Real diodes

There is constant generation/recombination of electron hole pairs.

In forward bias there is an extra current from recombination.

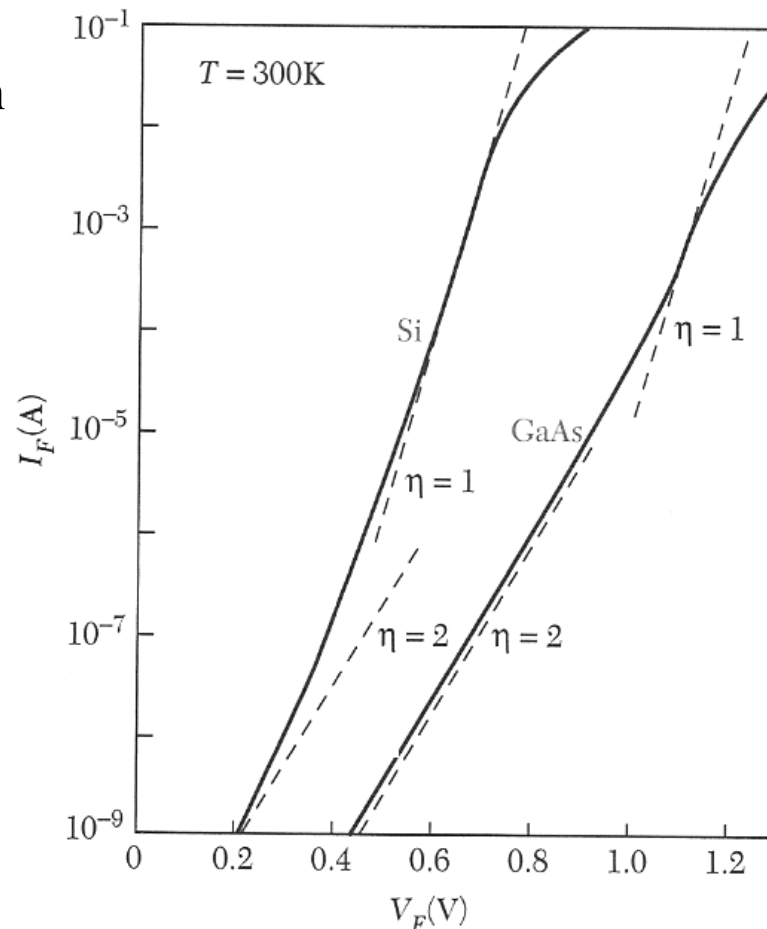
In reverse bias there is an extra current from generation.

Low bias: recombination dominates, $n = 2$

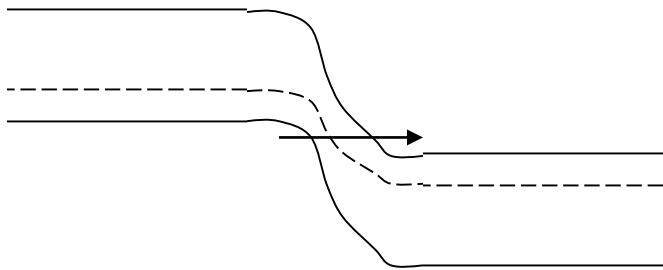
$$I = I_s \left(\exp \left(\frac{eV}{nk_B T} \right) - 1 \right)$$

Very high bias: series resistance

High bias: ideal behavior, $n = 1$



Zener tunneling



Electrons tunnel from valence band to conduction band

Occurs at high doping



(Zener diode)

