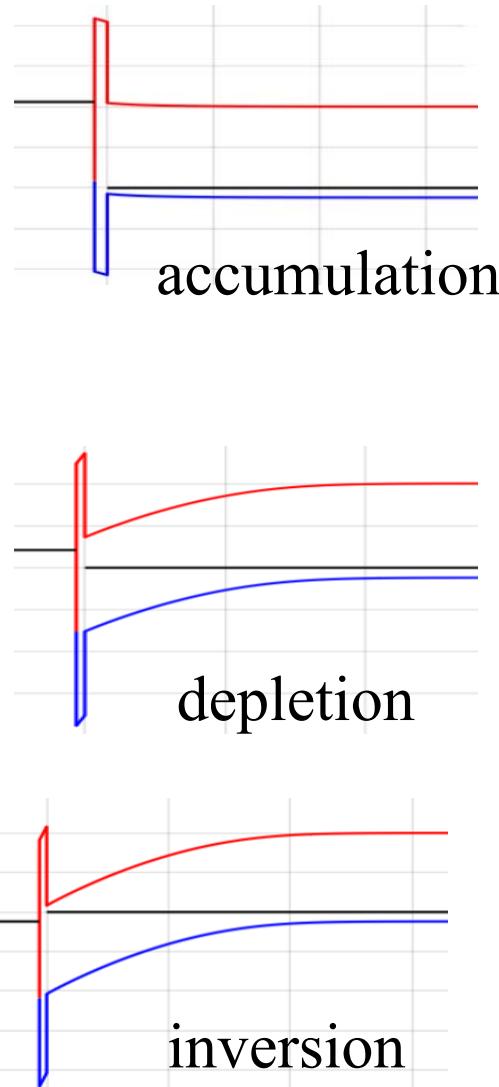


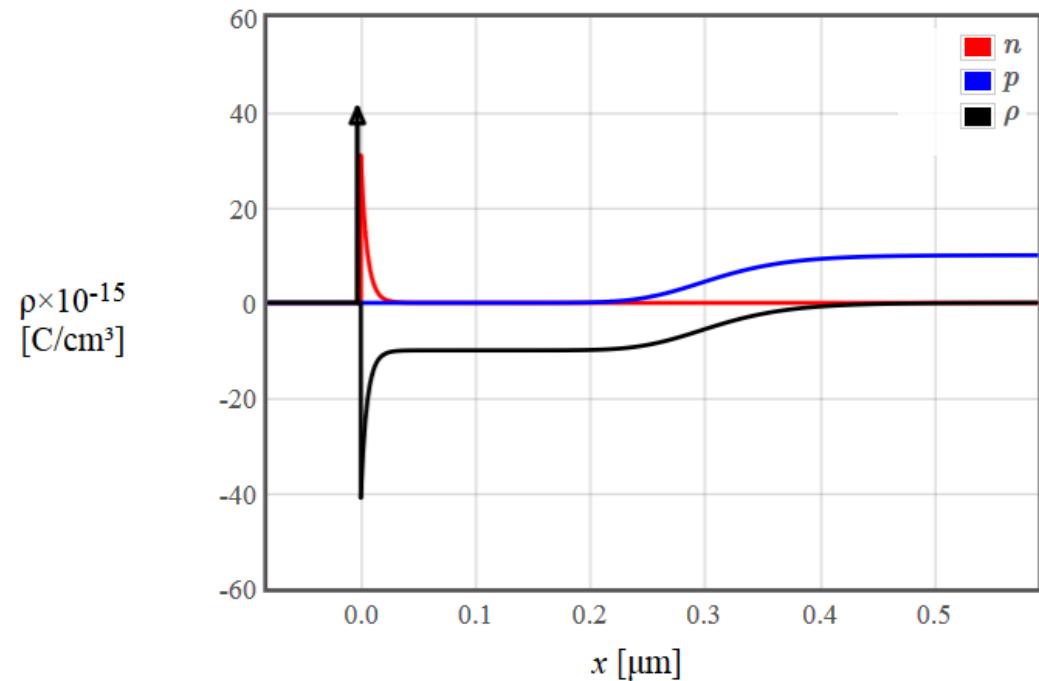
11. MOSFETs

Dec. 11, 2019

Gradual channel approximation



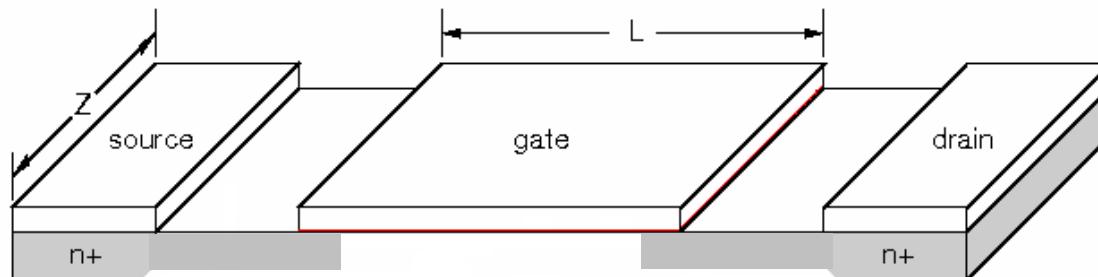
$$Q_{\text{mobile}} = \begin{cases} 0, & \text{for } V_G - V_B < V_T \\ -C_{\text{ox}}(V_G - V_B - V_T) & \text{for } V_G - V_B > V_T \end{cases}$$



Gradual channel approximation

Ohm's law $\longrightarrow j = -nev_d = ne\mu_n E_y$

$$I = Ztj = Ztn\mu_n E_y = Ze\mu_n n_s E_y$$



$n_s = nt$ is the sheet charge at the interface.

$$n_s(y) = -\frac{Q}{e} = \frac{C_{ox}(V_G - V_{ch}(y) - V_T)}{e}$$

Gradual channel approximation

$$n_s(y) = -\frac{Q(y)}{e} = \frac{C_{ox}(V_G - V_{ch}(y) - V_T)}{e}$$

$$I = Ztj = Ztnev_d = Zen_s\mu_nE_y$$

$$I_D = -Z\mu_nC_{ox}(V_G - V_{ch}(y) - V_T)\frac{dV_{ch}}{dy}$$

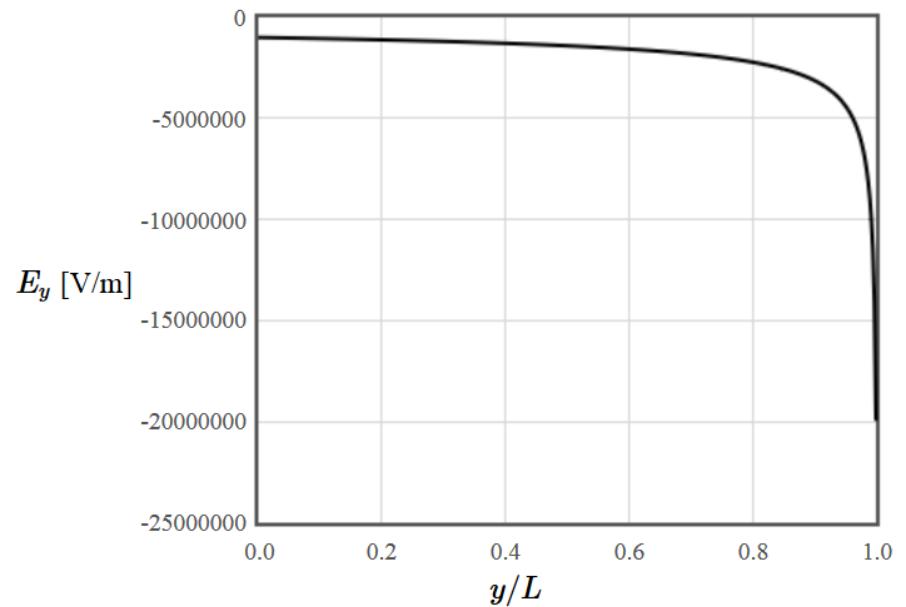
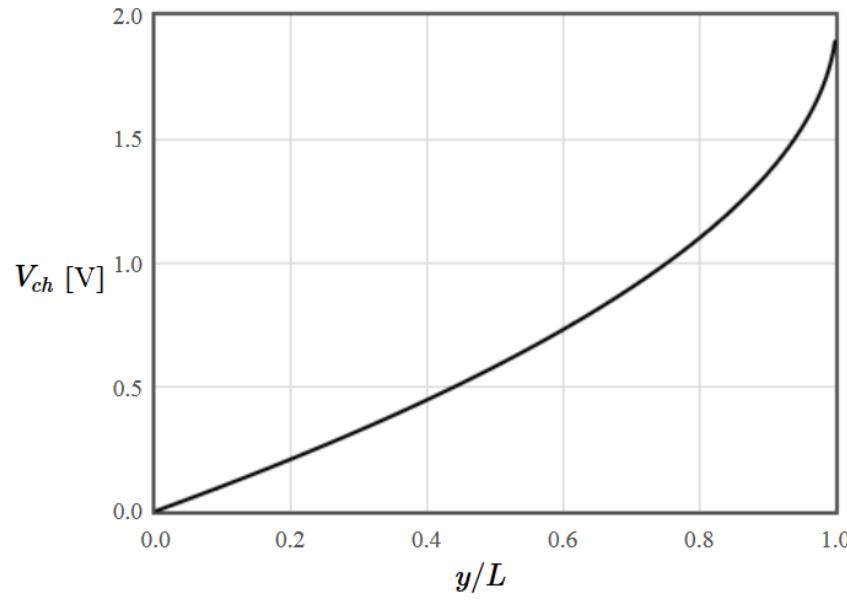


differential equation for V_{ch}

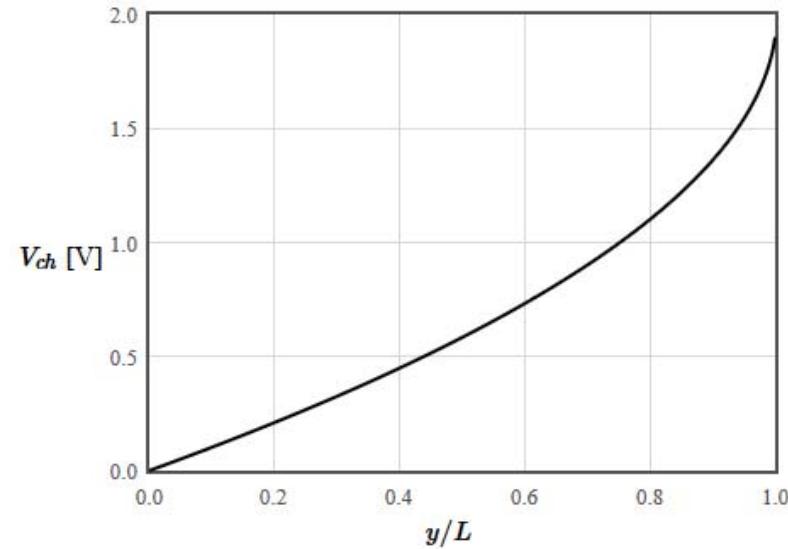
Gradual channel approximation

$$V_{ch}(y) = V_G - V_T - \sqrt{(V_G - V_T)^2 - \frac{2I_D y}{Z\mu_n C_{ox}}}$$

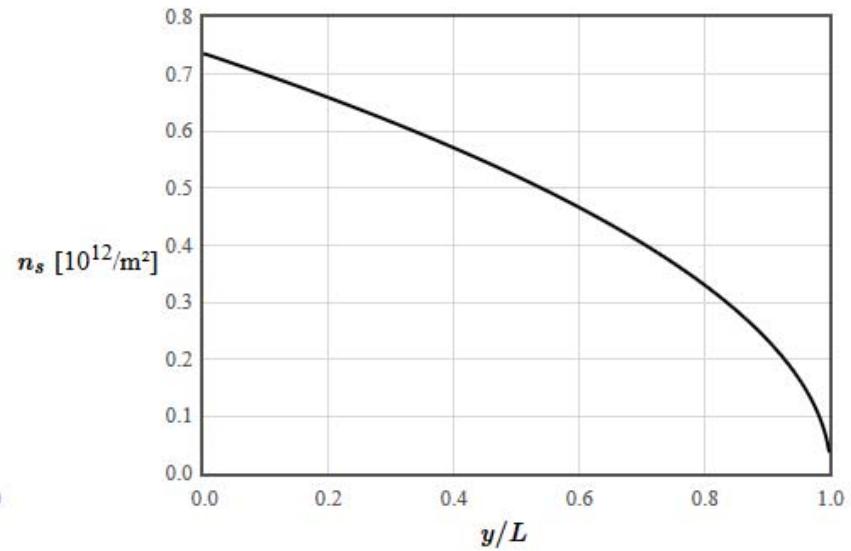
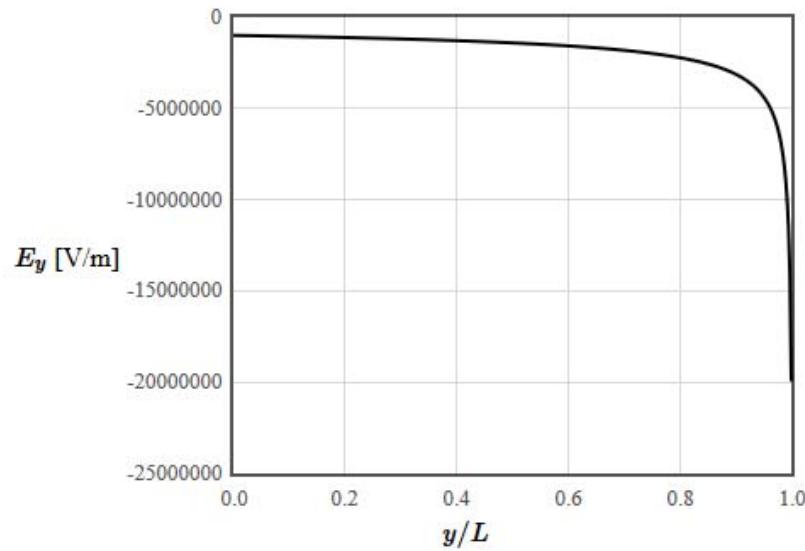
$$E_y = -\frac{dV_{ch}}{dy} = -\frac{I_D}{Z\mu_n C_{ox} \sqrt{(V_G - V_T)^2 - \frac{2I_D y}{Z\mu_n C_{ox}}}}$$



MOSFET Gradual Channel Approximation



| | |
|---------------------------------------|-------------------------|
| $Z = 1E-5$ | m |
| $L = 1E-6$ | m |
| $\mu_n = 1500$ | cm^2/Vs |
| $\epsilon_r = 4$ | |
| $t_{ox} = 3E-9$ | m |
| $V_D = 1.9$ | V |
| $V_G = 3$ | V |
| $V_T = 1$ | V |
| <input type="button" value="Replot"/> | |

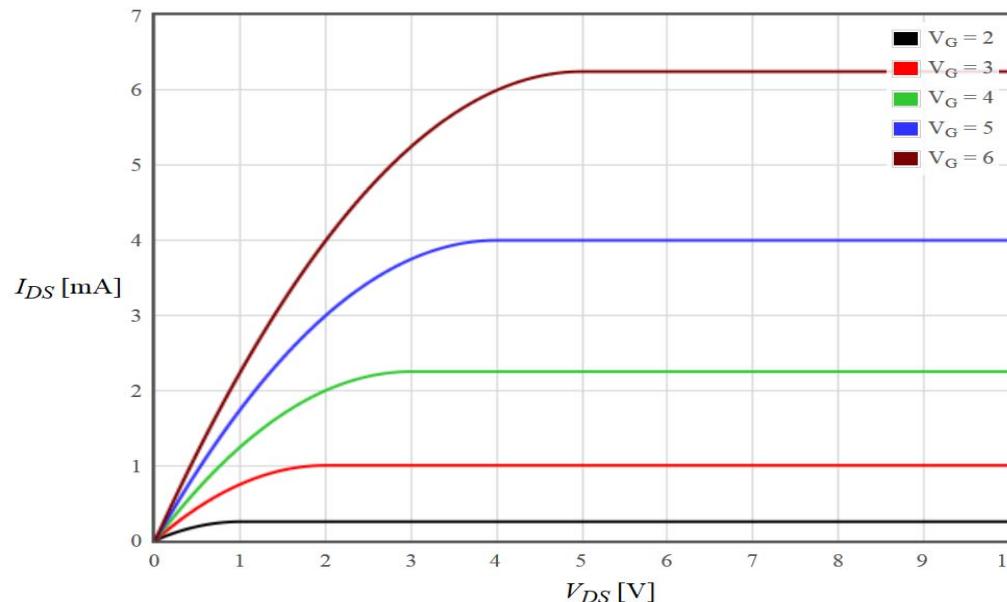


Gradual channel approximation

$$\int_0^L I_D \, dy = \int_0^{V_D} Z \mu_n C_{ox} (V_G - V_{ch}(y) - V_T) \, dV$$

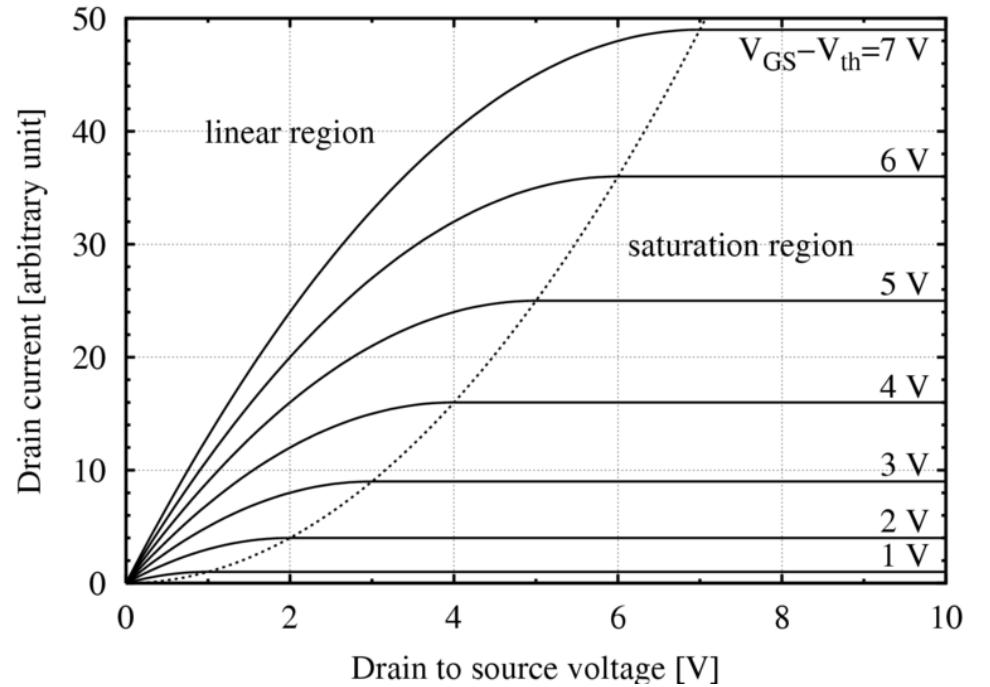
$$I_D = \frac{Z}{L} \mu_n C_{ox} \left[(V_G - V_T) V_D - \frac{V_D^2}{2} \right]$$

Valid in the linear regime (until pinch-off occurs at the drain).



MOSFET-saturation voltage

$$I = \frac{Z}{L} \mu_n C_{ox} \left[(V_G - V_T) V_D - \frac{V_D^2}{2} \right]$$



At pinch-off, $dI_{ds}/dV_{ds} = 0$

$$\frac{dI}{dV_D} = \frac{Z}{L} \mu_n C_{ox} \left[(V_G - V_T) - V_D \right] = 0 \quad V_{sat} = (V_G - V_T)$$

A MOSFET in saturation is a voltage controlled current source.

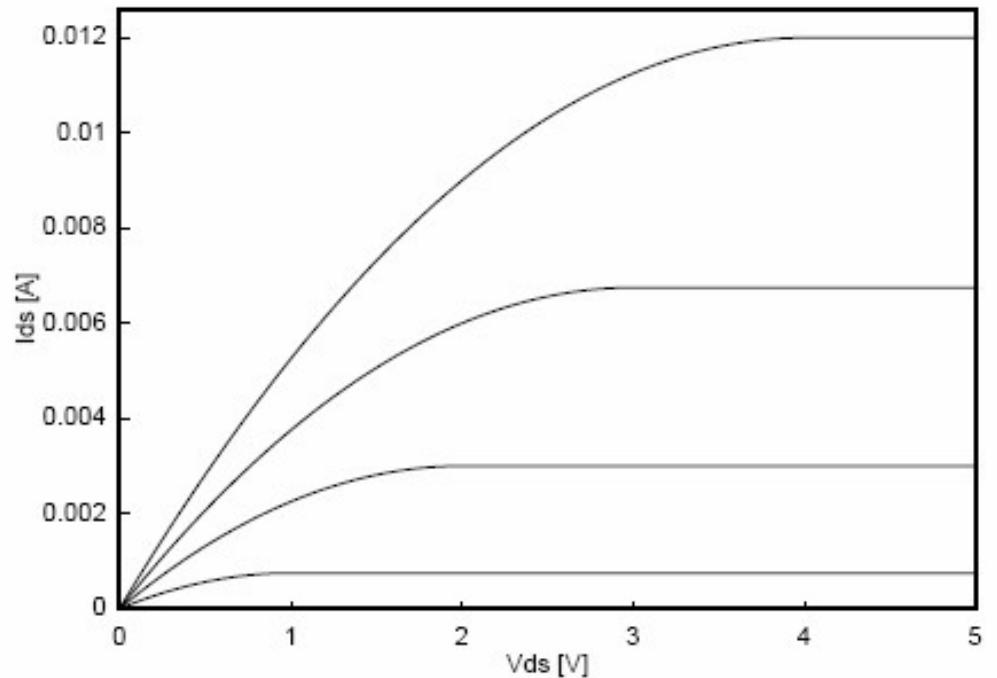
MOSFET - saturation current

Use the saturation voltage at pinch-off to determine the saturation current

$$V_{sat} = (V_G - V_T)$$

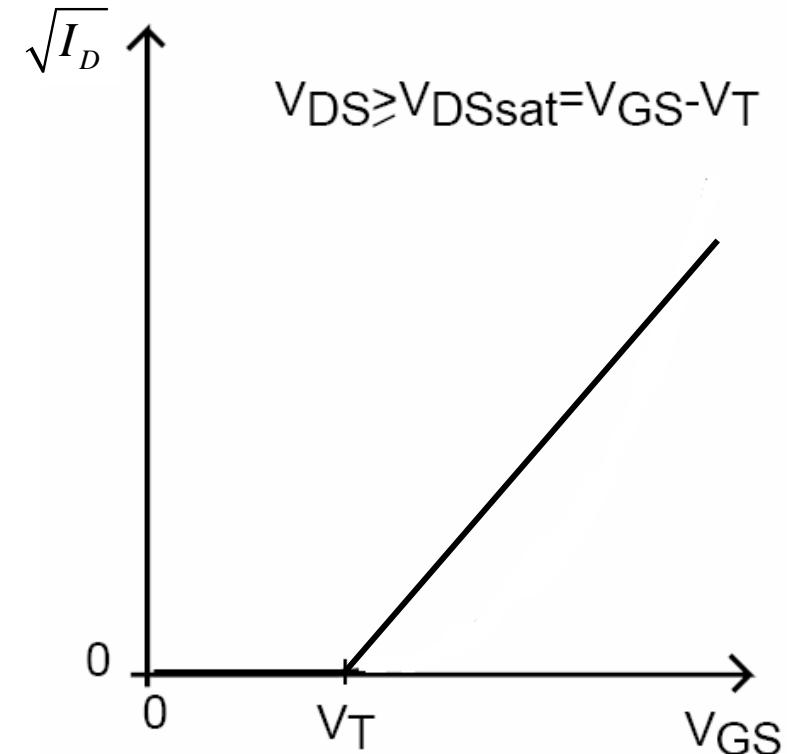
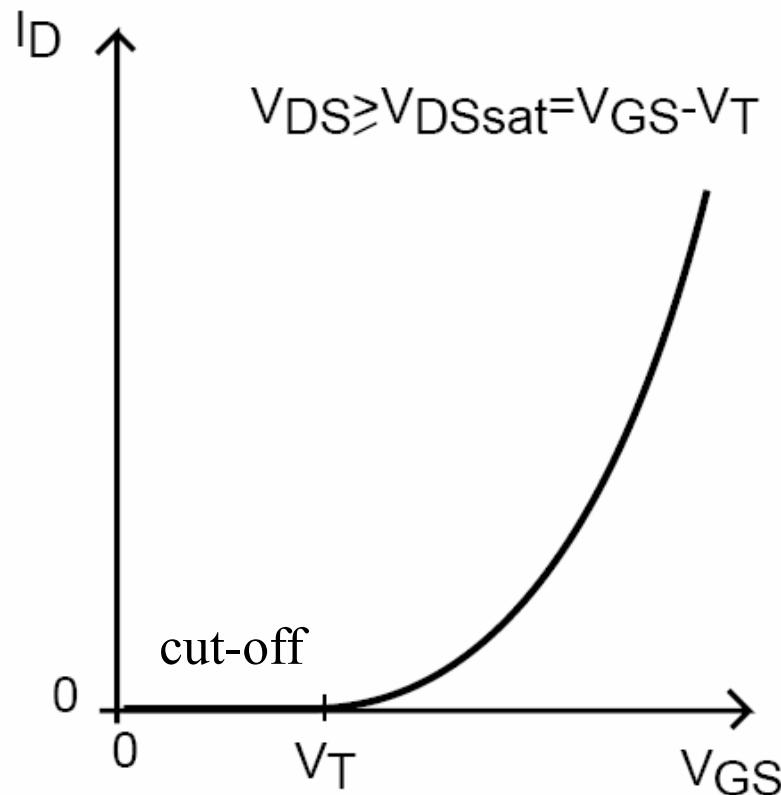
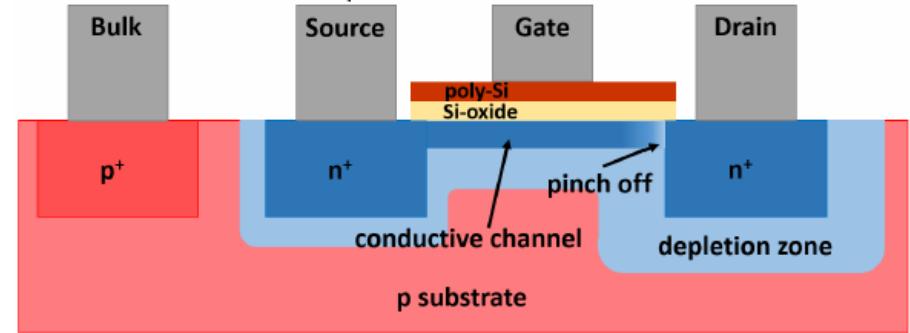
$$I = \frac{Z}{L} \mu_n C_{ox} \left[(V_G - V_T) V_D - \frac{V_D^2}{2} \right]$$

$$I_{sat} = \frac{Z}{2L} \mu_n C_{ox} (V_G - V_T)^2$$



MOSFET (saturation regime)

$$I_{sat} = \frac{Z}{2L} \mu_n C_{ox} (V_{GS} - V_T)^2$$

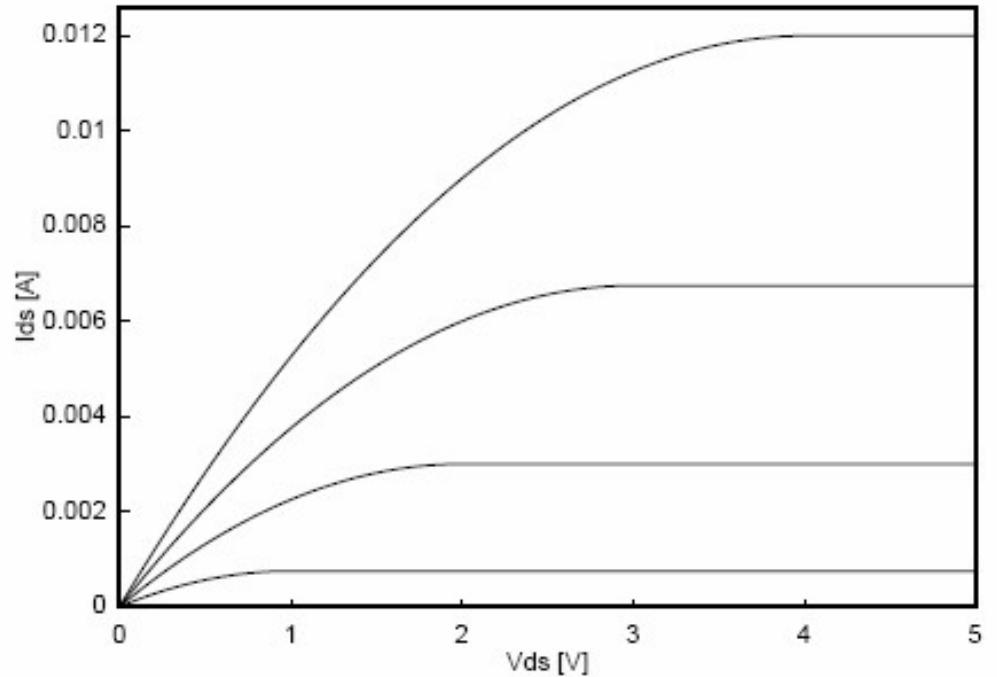


MOSFET (linear regime)

Channel conductance in the linear regime. For small V_D

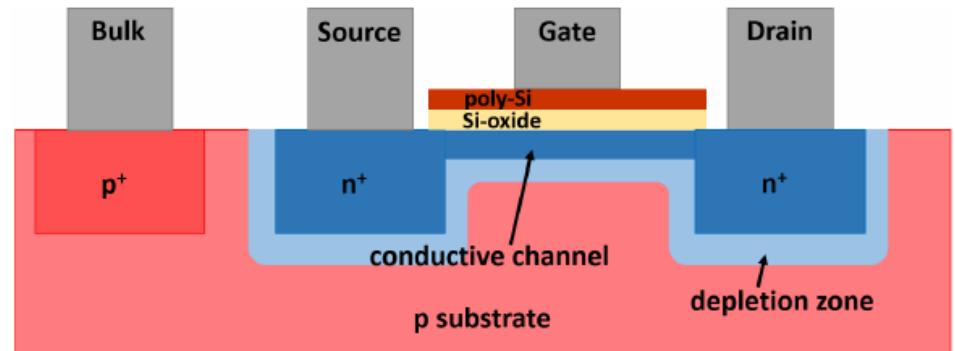
$$I \approx \frac{Z}{L} \mu_n C_{ox} [(V_G - V_T) V_D]$$

$$g_D = \frac{dI_D}{dV_D} = \frac{Z}{L} \mu_n C_{ox} (V_G - V_T)$$

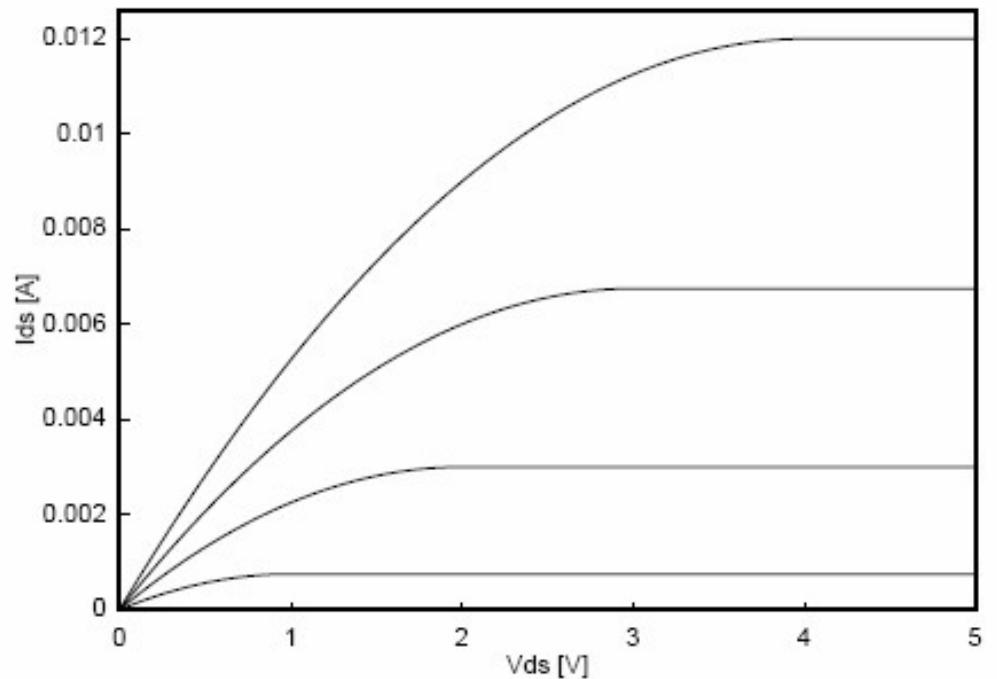
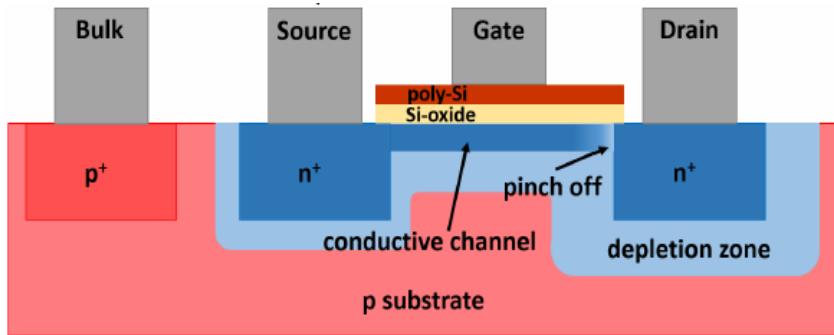


Transconductance

$$g_m = \frac{dI_D}{dV_G} = \frac{Z}{L} \mu_n C_{ox} V_D$$



MOSFET (saturation regime)



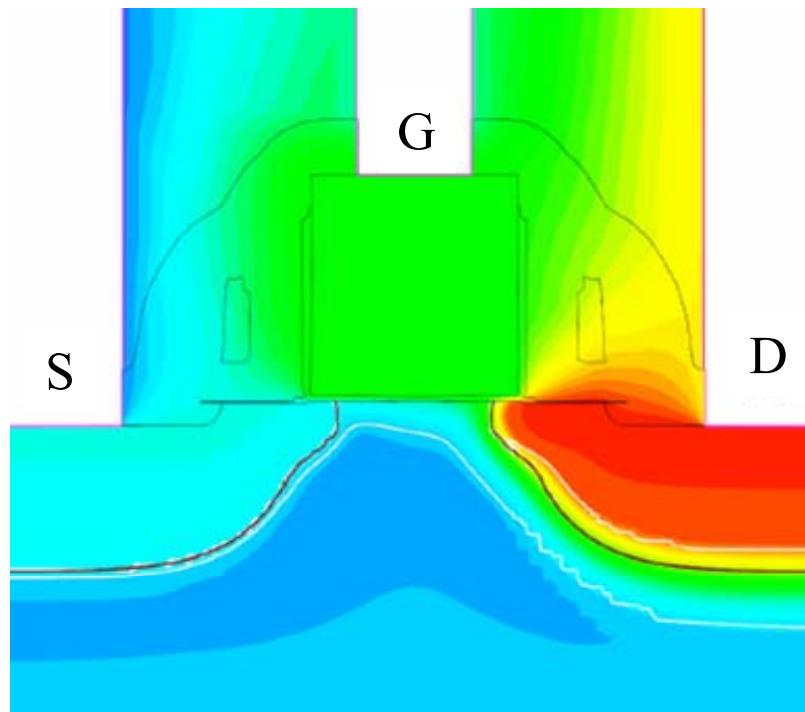
$$I_{sat} = \frac{Z}{2L} \mu_n C_{ox} (V_G - V_T)^2$$

Transconductance

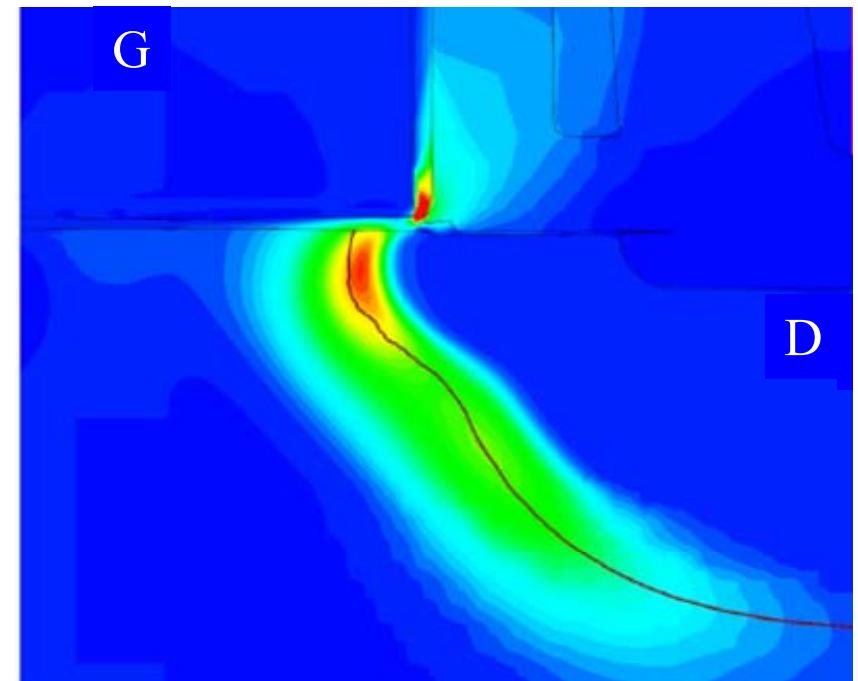
$$g_m = \frac{dI_D}{dV_G} = \frac{Z}{L} \mu_n C_{ox} (V_G - V_T)$$

A MOSFET in the saturation regime acts like a voltage controlled current source.

Saturation



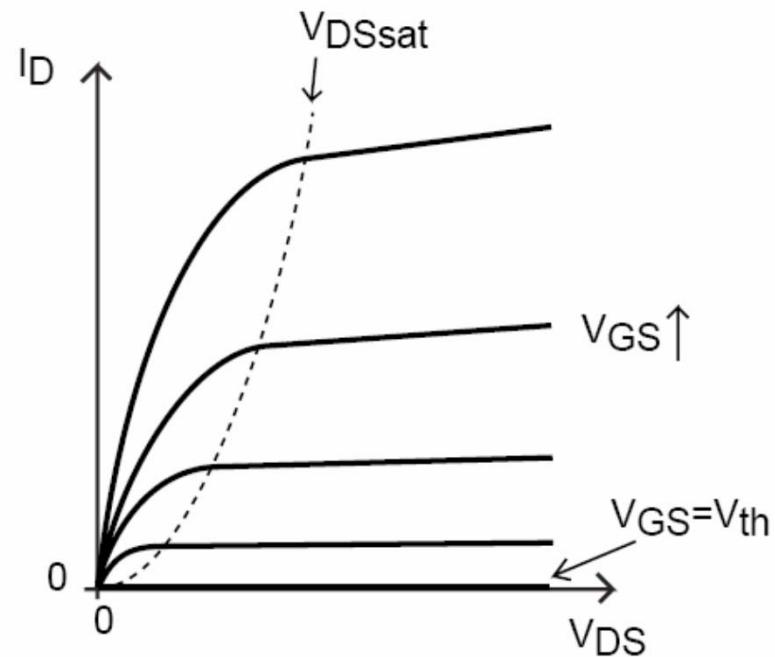
Potential



Electric field strength

MOSFET (saturation regime)

$$I_{sat} = \frac{Z}{2L} \mu_n C_{ox} (V_G - V_T)^2 (1 - \lambda (V_D - V_{sat}))$$



Experimentally: channel length modulation

$$\lambda \propto \frac{1}{L}$$

High frequencies

$$\tilde{i}_{in} = 2\pi f C_G \tilde{v}_G$$

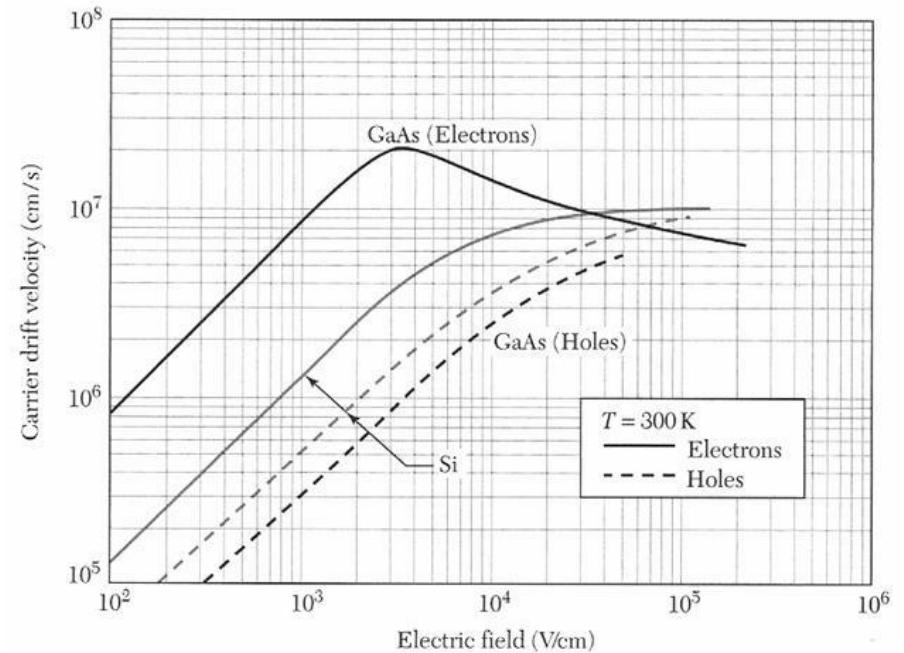
$$\tilde{i}_{out} = g_m \tilde{v}_G$$

$$\tilde{i}_{in} < \tilde{i}_{out}$$

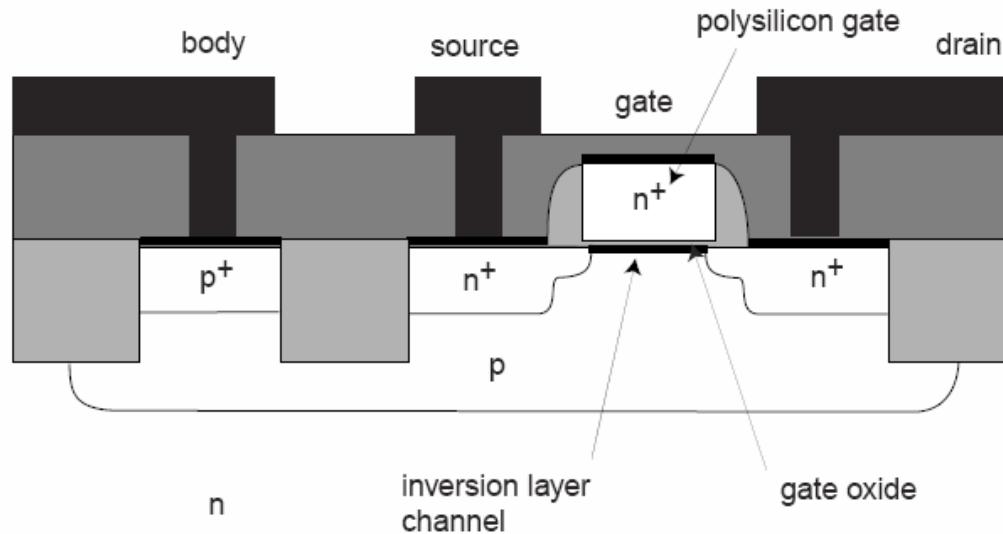
$$f < \frac{g_m}{2\pi C_G} \propto \frac{1}{L^2} = f_T$$

For large E , Ohm's law ($j = ne\mu E$) is not valid. The electron velocity saturates. For velocity saturation:

$$f_T \approx \frac{v_s}{L}$$



Constant E-field Scaling



Gate length L , transistor width Z , oxide thickness t_{ox} are scaled down.

V_{ds} , V_{gs} , and V_T are reduced to keep the electric field constant.

Power density remains constant.

$$L \sim 45 t_{ox}$$

1975 - 1990: "Days of happy scaling"

Constant E-field scaling

$$I_{sat} = \frac{Z}{2L} \mu_n \frac{\epsilon_{ox}}{t_{ox}} (V_G - V_T)^2$$

$$L \Rightarrow sL, \quad Z \Rightarrow sZ, \quad t_{ox} \Rightarrow st_{ox}, \quad V_{th} \Rightarrow sV_{th}$$

$$I_{sat} \Rightarrow sI_{sat} \quad \longleftarrow \quad I_{sat} \text{ gets smaller}$$

$$g_m = \frac{dI_D}{dV_G} = \frac{Z}{L} \mu_n \frac{\epsilon_{ox}}{t_{ox}} (V_G - V_T) \quad \longleftarrow \quad \text{Transconductance stays the same.}$$

Power per transistor decreases like L^2 . Power per unit area remains constant.

The heat dissipation problem

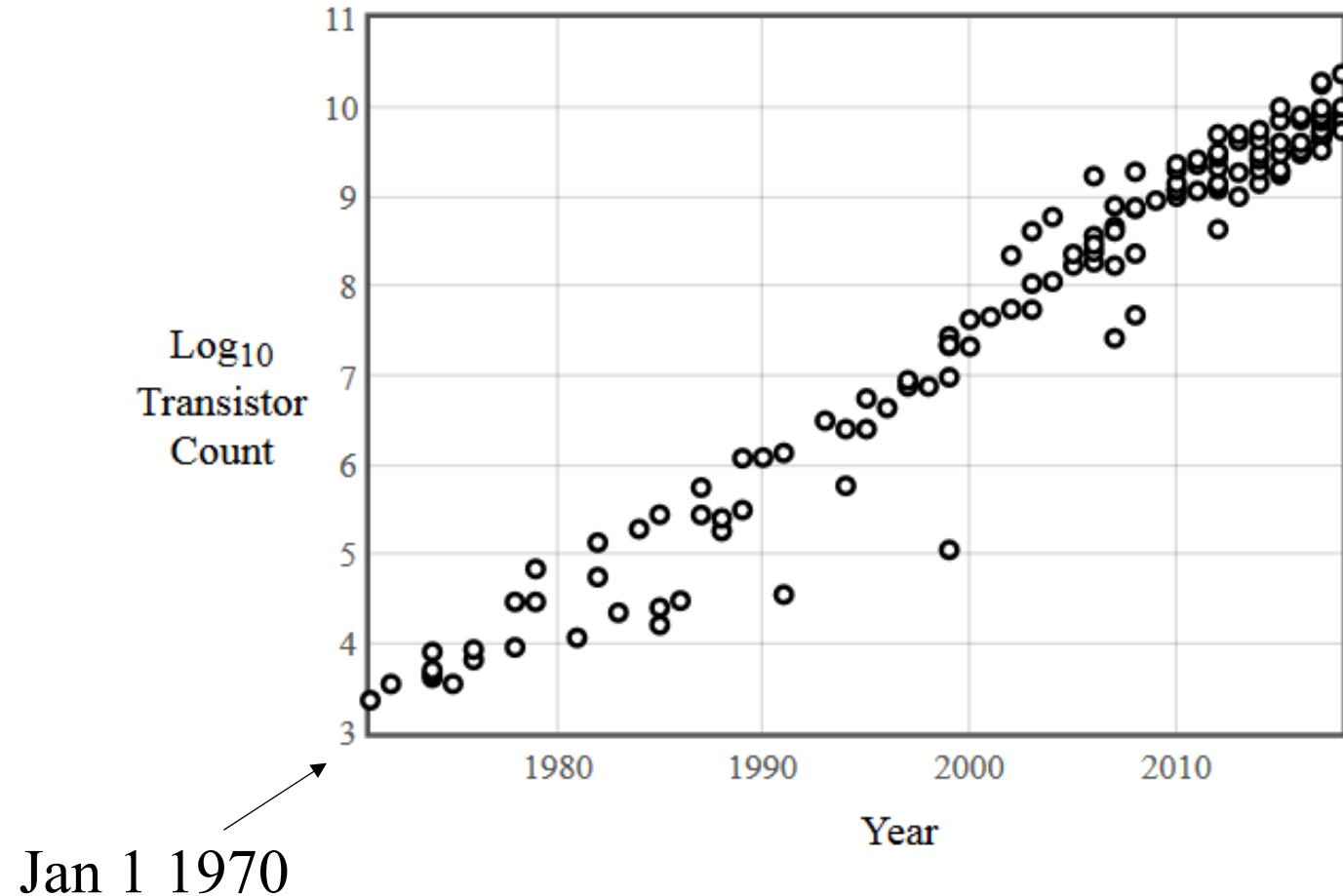
Microprocessors are hot $\sim 100\text{ C}$

Hotter operation will cause dopants to diffuse

When more transistors are put on a chip they must dissipate less power.

Power per transistor decreases like L^2 .

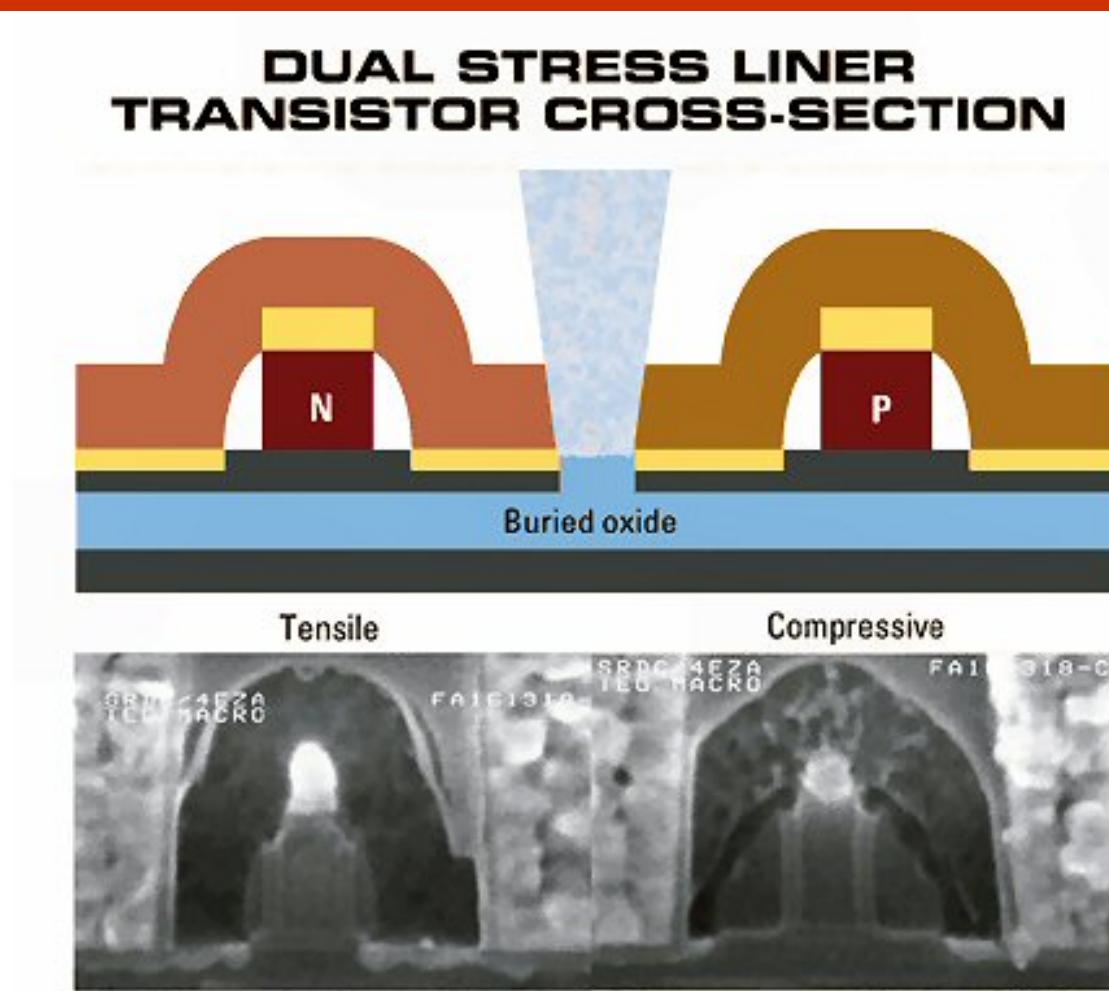
Transistor Count 2018



Transistor count doubles about every 2 years

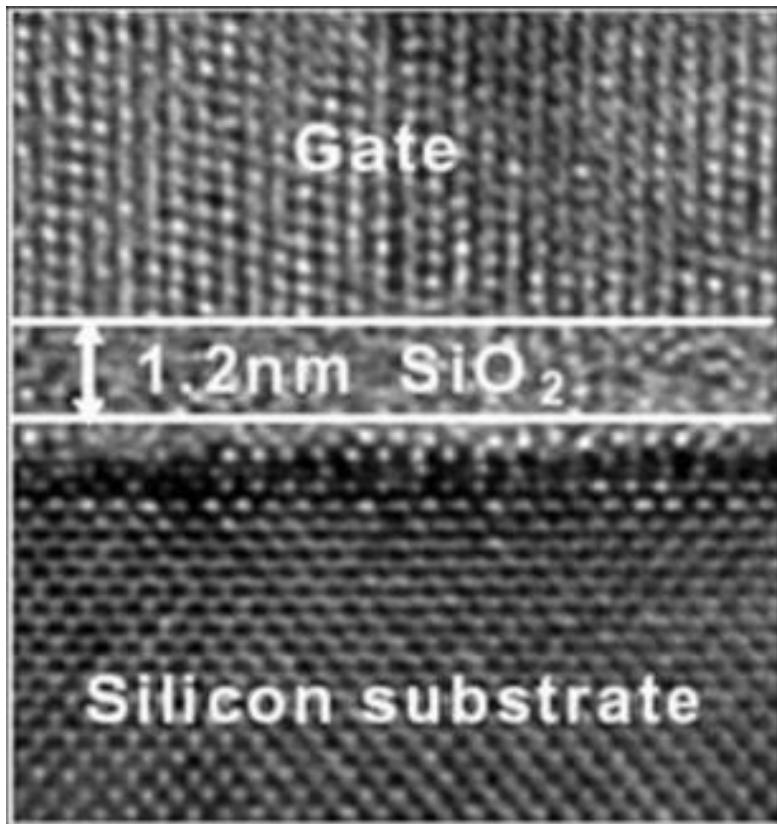
https://en.wikipedia.org/wiki/Transistor_count

Dual stress liners



Tensile silicon nitride film over the NMOS and a compressive silicon nitride film over the PMOS improves the mobility.

Gate dielectric

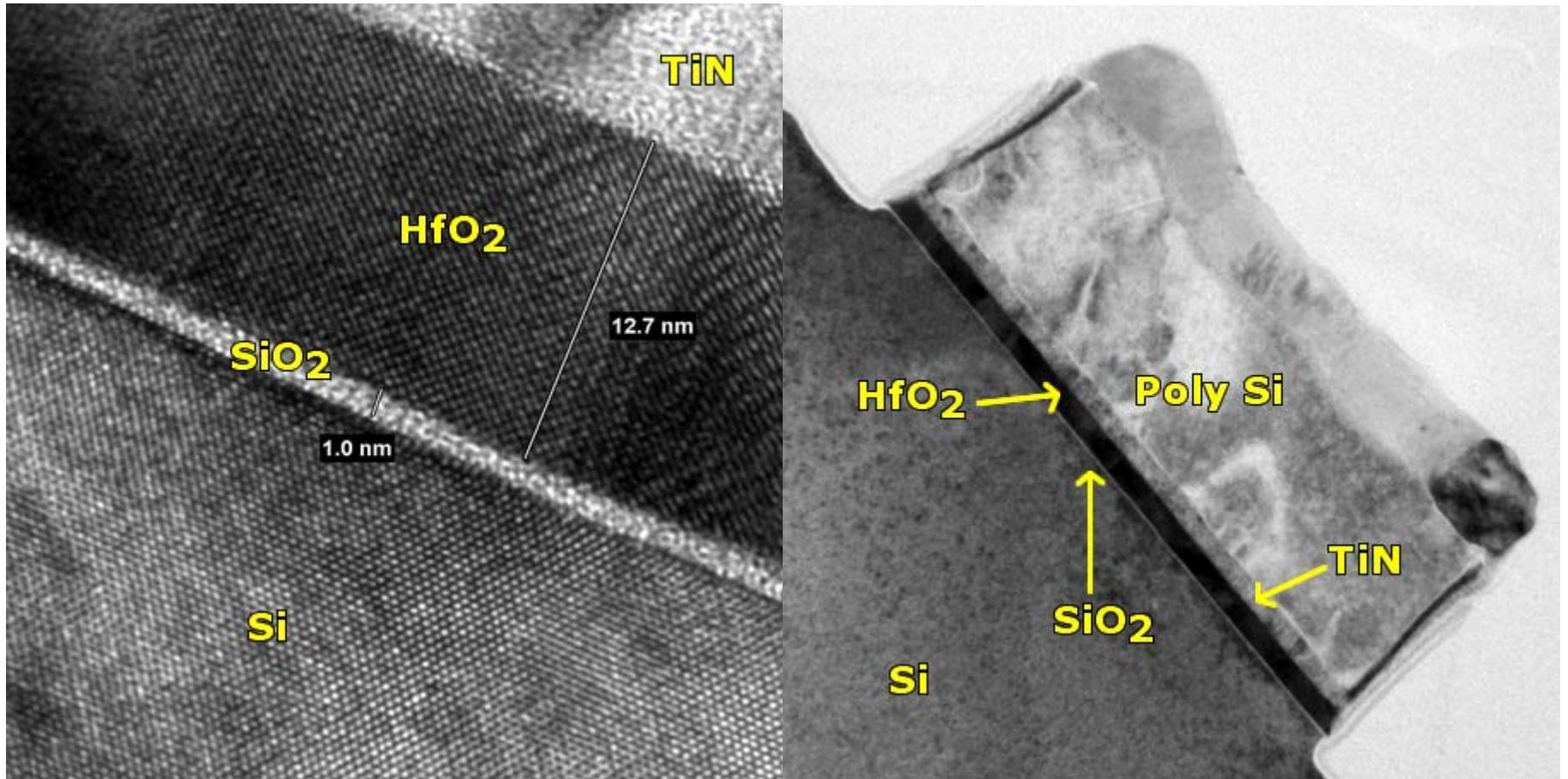


Thinner than 1 nm:
electrons tunnel

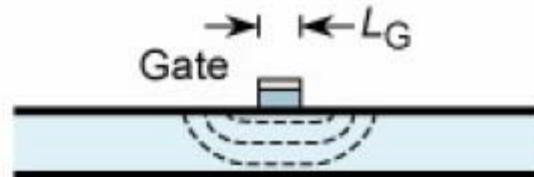
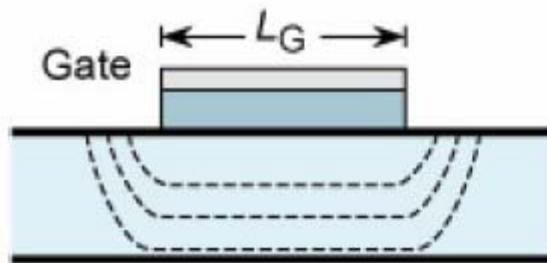
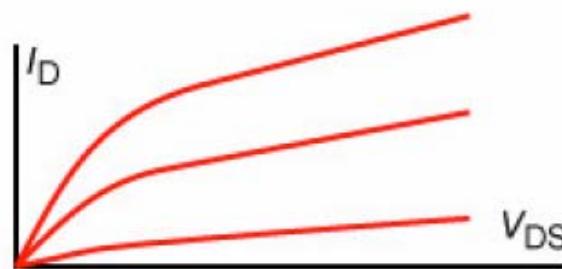
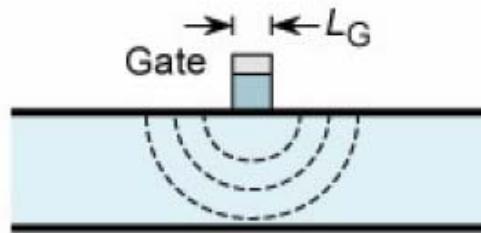
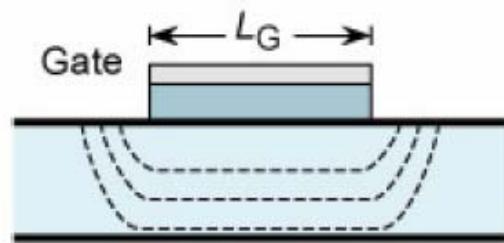
Large dielectric
constant desirable
 $\varepsilon_r(\text{SiO}_2) \sim 4$

$\varepsilon_r(\text{Si}_3\text{N}_4) \sim 7$

High-k dielectrics



Short channel effects



- Short-channel effects:
- Threshold-voltage shift
- Lack of pinch-off
- Increased leakage current
- Increase of output conductance

SOI: silicon on insulator

CMOS SOI

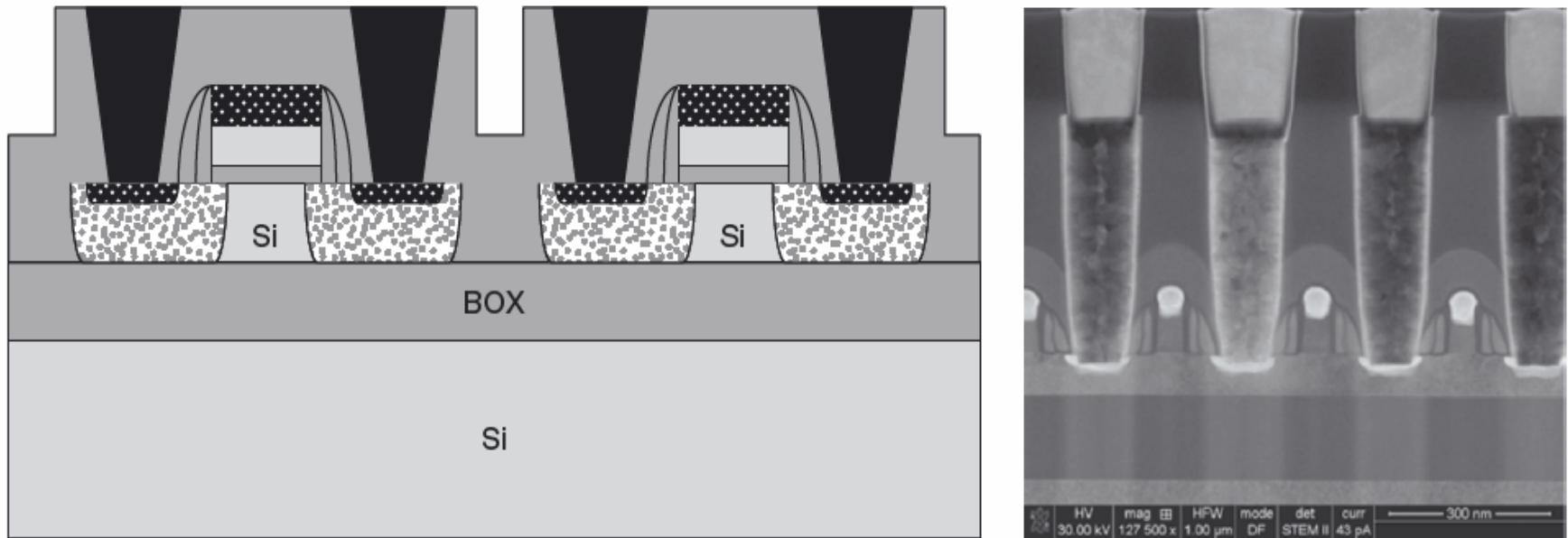


Figure 26.16 SOI MOSFET with first-level metal, schematic and TEM. Courtesy Brandon Van Leer, FEI Company⁴

Fransila



Intel® Pentium® 4 90 nm



Intel® Pentium® D 65 nm

Intel® Core™2 Duo 45 nm

Intel® Atom™ Z6xx Series 45 nm

Intel® Core™2 Celeron 45 nm

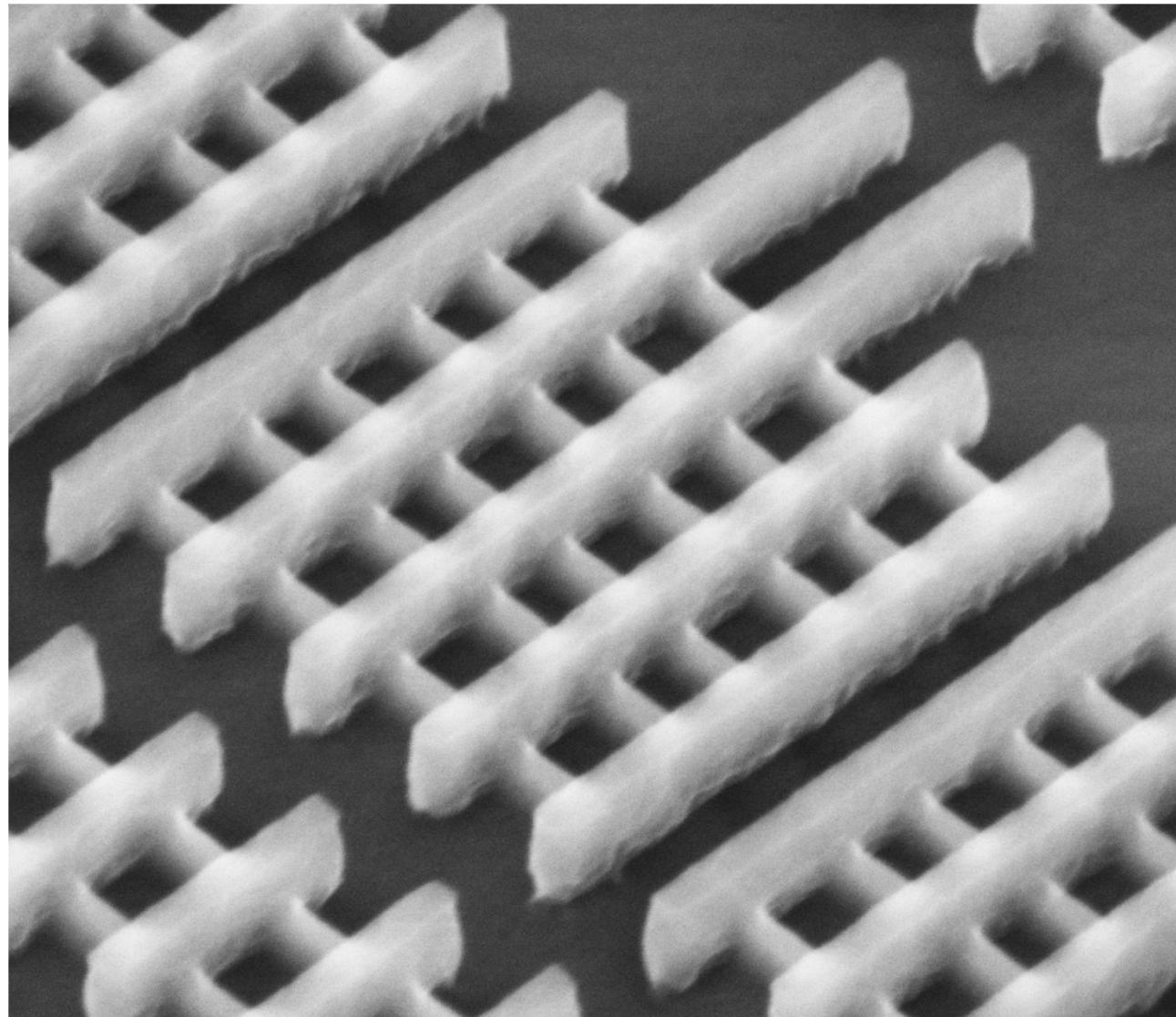
Intel® Core™ i7-900 32 nm

Intel® Xeon® 5600 Series 32 nm

Intel® Ivy bridge tri-gate 22 nm

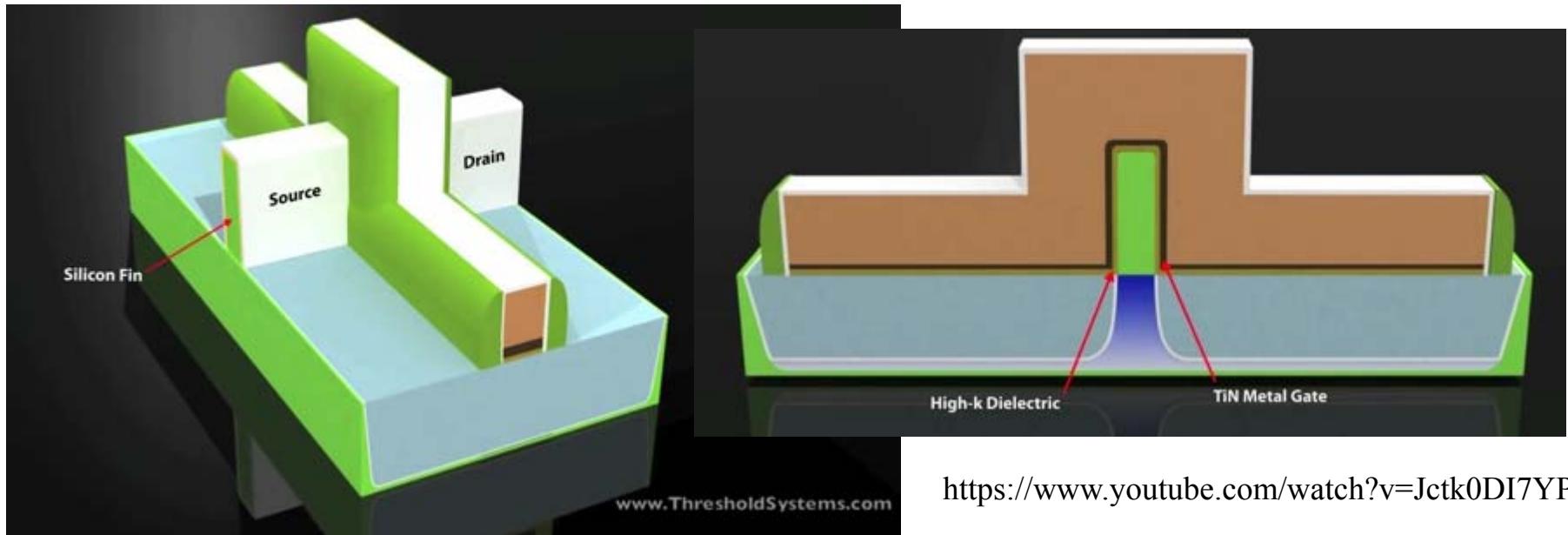
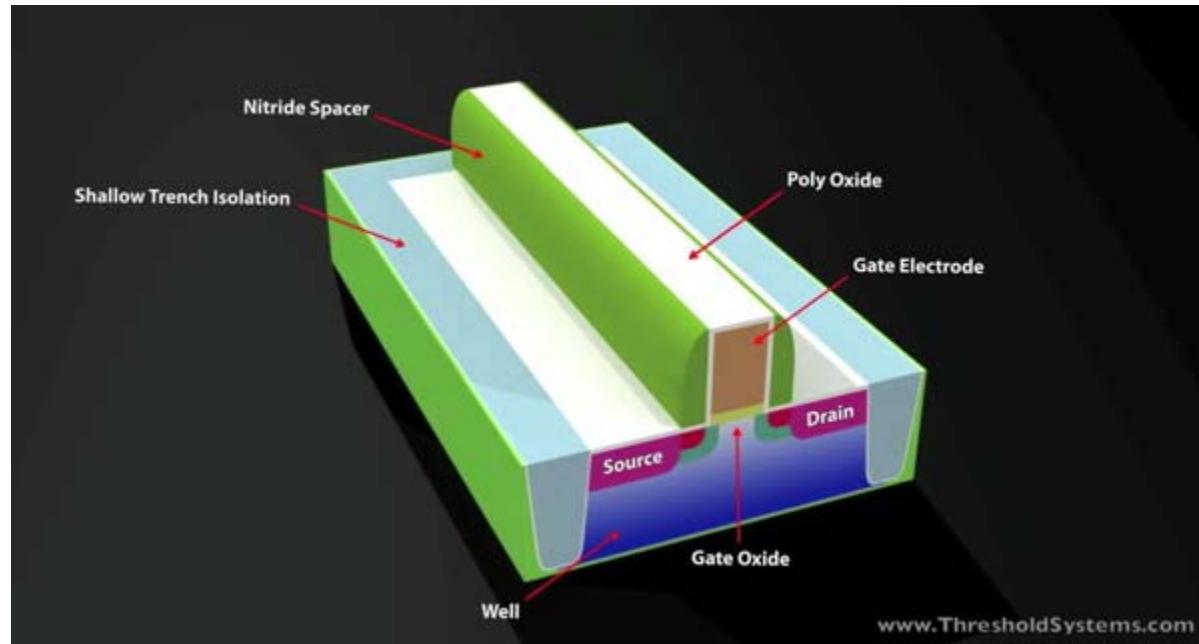
Intel® Haswell FinFET 16 nm

Intel 22nm 3D tri-gate transistor



http://download.intel.com/newsroom/kits/22nm/gallery/images/Intel-22nm_Transistor.jpg

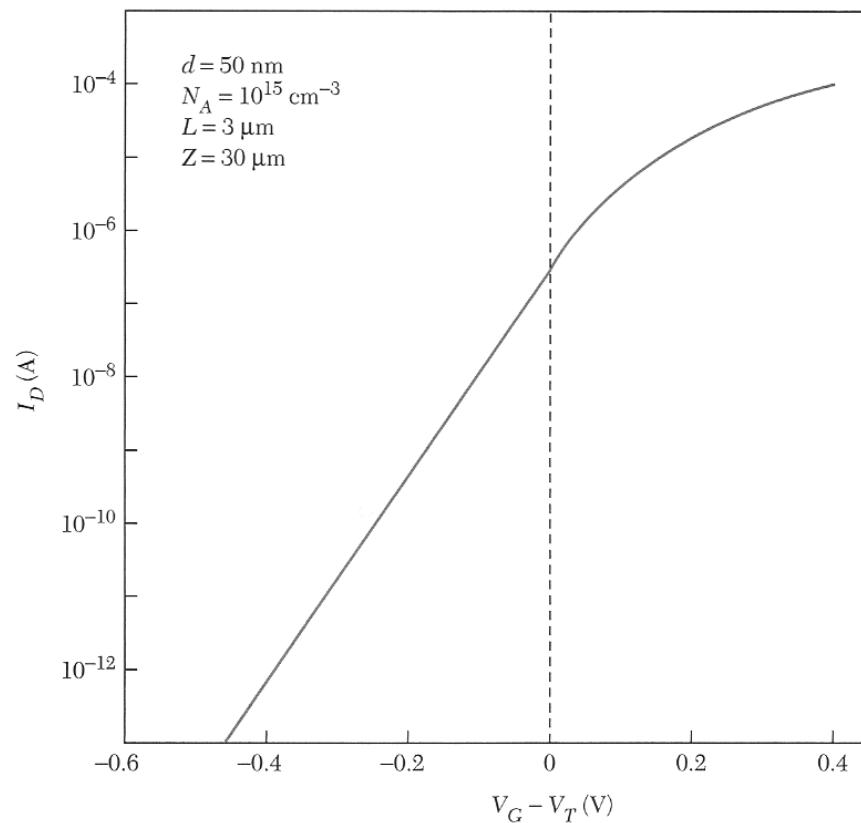
FinFET



<https://www.youtube.com/watch?v=Jctk0DI7YP8>

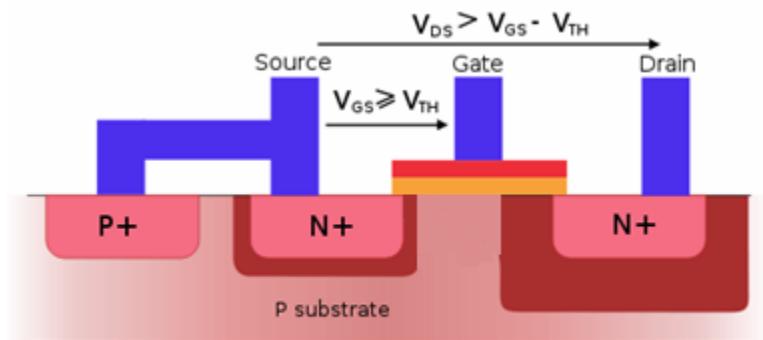
Subthreshold current

For $V_G < V_T$ the transistor should switch off but there is a diffusion current. The current is not really off until ~ 0.5 V below the threshold voltage.



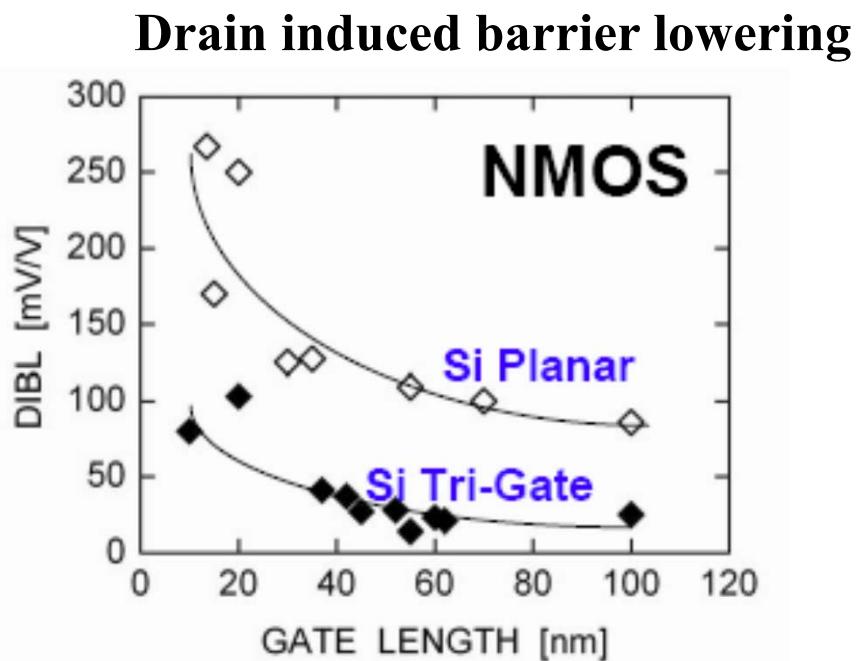
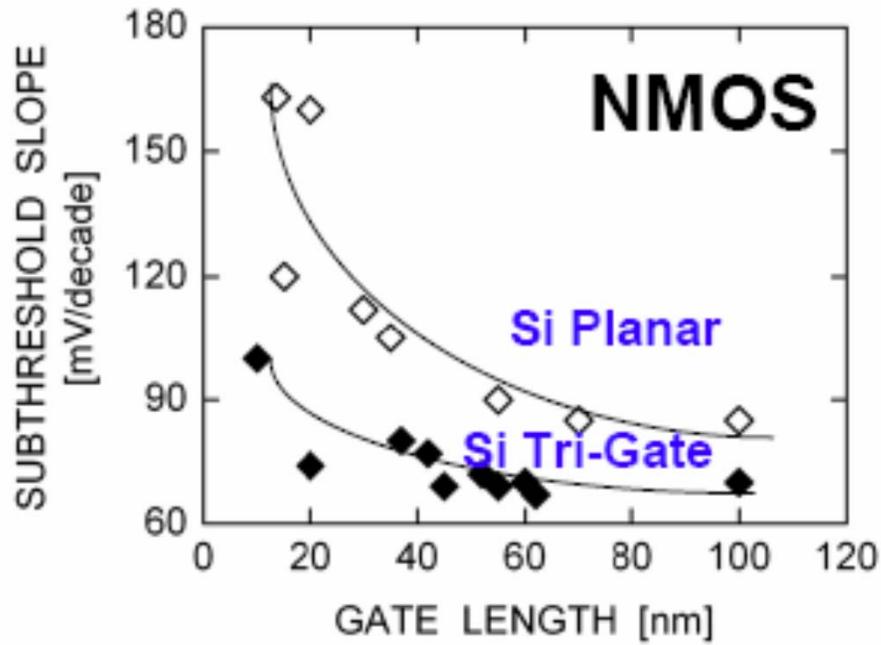
Weak inversion

$$I_D \propto \exp\left(\frac{e(V_G - V_T)}{k_B T}\right)$$



Subthreshold swing: 70-100 mV/decade

FinFET, Tri-gate



Robert Chau, Intel

