

Technische Universität Graz

Institute of Solid State Physics

# 13. Bipolar transistors

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## bipolar transistors





lightly doped p substrate

Used in front-end high-frequency receivers (mobile telephones).



Oxide isolated integrated BJT - a modern process

### abrupt junction



$$eV_{bi} = k_B T \ln\left(\frac{N_D N_A}{n_i^2}\right)$$

$$E = -\frac{eN_A}{\varepsilon} \left( x + x_p \right) \qquad -x_p > x > 0$$

$$E = \frac{eN_D}{\varepsilon} (x - x_n) \qquad 0 > x > x_n$$

$$V = \frac{eN_A}{\varepsilon} \left( \frac{x^2}{2} + xx_p \right) \qquad -x_p > x > 0$$
$$V = \frac{-eN_D}{\varepsilon} \left( \frac{x^2}{2} - xx_n \right) \qquad 0 > x > x_n$$

### Forward bias, V > 0

log(Carrier Densities)



Electrons and holes are driven towards the junction. The depletion region becomes narrower

$$n_{p}(x_{p}) = n_{p0} \exp\left(\frac{eV}{k_{B}T}\right)$$
$$p_{n}(x_{n}) = p_{n0} \exp\left(\frac{eV}{k_{B}T}\right)$$

 $p_{e0} \exp\left(\frac{eV_{be}}{k_B T}\right)$ 

Minority electrons are injected into the p-region Minority holes are injected into the n-region

### Reverse bias, V < 0



log(Carrier Densities)

Electrons and holes are driven away from the junction.

The depletion region becomes wider

$$n_{p}(x_{p}) = n_{p0} \exp\left(\frac{eV}{k_{B}T}\right)$$
$$p_{n}(x_{n}) = p_{n0} \exp\left(\frac{eV}{k_{B}T}\right)$$

Minority electrons are extracted from the p-region by the electric field Minority holes are extracted from the n-region by the electric field

### pnp transistor, no bias





### pnp transistor, forward active bias





Always dissipate power due to the forward bias

The base-emitter voltage controls the minority carriers injected from the emitter to the base. These diffuse to the base-collector junction and are swept into the collector.

### Long/Short diode



#### Minority carrier concentration



#### Emitter current

$$I_{E} = I_{En} + I_{Ep} = \left[\frac{eA_{be}D_{p}P_{e0}}{W_{eb} - x_{e}} + \frac{eA_{be}D_{n}n_{b0}}{W_{bc} - W_{be}}\right] \left(e^{eV_{be}/k_{B}T} - 1\right) - \frac{eA_{be}D_{n}n_{b0}}{W_{bc} - W_{be}} \left(e^{eV_{bc}/k_{B}T} - 1\right)$$
$$I_{E} = I_{ES} \left(e^{eV_{be}/k_{B}T} - 1\right) - \alpha_{R}I_{CS} \left(e^{eV_{bc}/k_{B}T} - 1\right)$$



#### Collector current



#### Collector current

$$I_{c} = I_{cp} + I_{cn} = \frac{eA_{bc}D_{n}n_{b0}}{W_{bc} - W_{be}} \left(e^{eV_{be}/k_{B}T} - 1\right) - \left[\frac{eA_{bc}D_{p}P_{c0}}{x_{c} - W_{c}} + \frac{eA_{bc}D_{n}n_{b0}}{W_{bc} - W_{be}}\right] \left(e^{eV_{bc}/k_{B}T} - 1\right)$$

$$I_{c} = I_{cp} + I_{cn} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$



#### Ebers-Moll model

$$I_{E} = I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - \alpha_{R} I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$
$$I_{C} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$
$$I_{B} = I_{E} - I_{C}$$



### Not an npn transistor





### Emitter efficiency

$$\gamma_{e} = \frac{I_{En}}{I_{En} + I_{Ep}} = \frac{1}{1 + I_{Ep} / I_{En}} \qquad \text{for npn}$$

$$I_{Ep} = eA_{be}D_{p} \frac{p_{e0}\left(e^{eV_{be}/k_{B}T} - 1\right)}{W_{eb} - x_{e}}$$

$$I_{En} = -eA_{be}D_{n} \frac{n_{b0}\left(e^{eV_{be}/k_{B}T} - e^{eV_{bc}/k_{B}T}\right)}{W_{bc} - W_{be}}$$
For  $\gamma_{e} \sim 1$ ,  $W_{bc} - W_{be} << L_{b}$ ,  $W_{eb} - x_{e}$  and  $n_{b0} >> p_{e0}$ 

$$\int \frac{n_{i}^{2}}{N_{Ab}} \qquad \frac{n_{i}^{2}}{N_{De}}$$
neutral base width

Small base width and heavy emitter doping

#### Base transport factor

$$B = \frac{I_c}{I_{En}}$$

ratio of the injected current to the collected current

recombination in the base would reduce the base transport factor

A thin base with low doping results in a base transport factor  $\sim 1$ 

#### Current transfer ratio

$$\alpha = \frac{I_C}{I_E} = B\gamma_e$$

 $\alpha \sim 1$  for a good BJT

### Transistor modes

- 1. Forward active: emitter-base forward, base-collector reverse
- 2. Saturation: emitter-base forward, base-collector forward
- 3. Reverse active: emitter-base reverse, base-collector forward
- 4. Cut-off: emitter-base reverse, base-collector reverse



#### Ebers-Moll model

$$I_{E} = I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - \alpha_{R} I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$
$$I_{C} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$
$$I_{B} = I_{E} - I_{C}$$



#### Common base configuration

$$I_{E} = I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - \alpha_{R} I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$
  
solve for  $V_{be}$   
$$I_{c} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$



http://lamp.tu-graz.ac.at/~hadley/psd/L13/commonbase/pnp\_current.html

#### Ebers - Moll Model

$$I_{ES} = \left[\frac{eA_{be}D_{p}P_{e0}}{W_{eb} - x_{e}} + \frac{eA_{be}D_{n}n_{b0}}{W_{bc} - W_{be}}\right]$$
$$\alpha_{R}I_{CS} = \frac{eA_{be}D_{n}n_{b0}}{W_{bc} - W_{be}}$$

$$\alpha_{F} I_{ES} = \frac{eA_{bc}D_{n}n_{b0}}{W_{bc} - W_{be}}$$
$$I_{CS} = \left[\frac{eA_{bc}D_{p}p_{c0}}{x_{c} - W_{c}} + \frac{eA_{bc}D_{n}n_{b0}}{W_{bc} - W_{be}}\right]$$

#### Common emitter configuration

$$I_{E} = I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - \alpha_{R} I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right) \qquad I_{B} = I_{E} - I_{C}$$

$$I_{c} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$



current amplification ~100

### Current amplification factor

$$\beta = h_{fe} = \frac{I_C}{I_B}$$

$$I_B = I_E - I_C$$

$$I_C = \alpha I_E$$

$$I_B = \left(\frac{1}{\alpha} - 1\right) I_C$$

$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha} = \frac{B\gamma_e}{1 - B\gamma_e}$$

 $\beta \sim 50 - 500$ 



#### Transconductance

$$g_{m} = \frac{\partial I_{C}}{\partial V_{be}}$$
$$I_{c} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$

The first term depends on  $V_{be}$ 

$$g_m = \frac{e\alpha_F I_{ES}}{k_B T} e^{eV_{be}/k_B T} \approx \frac{eI_C}{k_B T} = \frac{e\beta I_B}{k_B T}$$

The transconductance can be very high.

### Early effect

Ebers - Moll:  

$$I_{E} = I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - \alpha_{R} I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$

$$I_{c} = \alpha_{F} I_{ES} \left( e^{eV_{be}/k_{B}T} - 1 \right) - I_{CS} \left( e^{eV_{bc}/k_{B}T} - 1 \right)$$

$$I_{B} = I_{E} - I_{C}$$

$$I_{ES} = \left[\frac{eA_{be}D_{p}P_{e0}}{W_{eb} - x_{e}} + \frac{eA_{be}D_{n}n_{b0}}{W_{bc} - W_{be}}\right] \qquad \qquad I_{CS} = \left[\frac{eA_{bc}D_{p}P_{c0}}{x_{c} - W_{c}} + \frac{eA_{bc}D_{n}n_{b0}}{W_{bc} - W_{be}}\right]$$

 $I_{ES}$  and  $I_{CS}$  are treated as constants but the depletion widths  $W_{bc}$ ,  $W_{be}$ ,  $W_{c}$ , and  $W_{e}$  depend on the voltages.



#### Minority carrier concentration



### Early effect



Common emitter configuration

Base width modulation: smaller width increases the diffusion current and increases the gain.

Punchthrough: The neutral base width goes to zero and all gain is lost. Lightly dope the collector -> voltage drops in collector. Makes circuit slower.



#### **NPN common emitter configuration**

#### Common emitter configuration



 $I_C \sim \beta I_B$  amplifier

### Small signal response



#### Small signal response



#### Small signal response



### Heterojunction bipolar transistors



Semiinsulating GaAs substrate