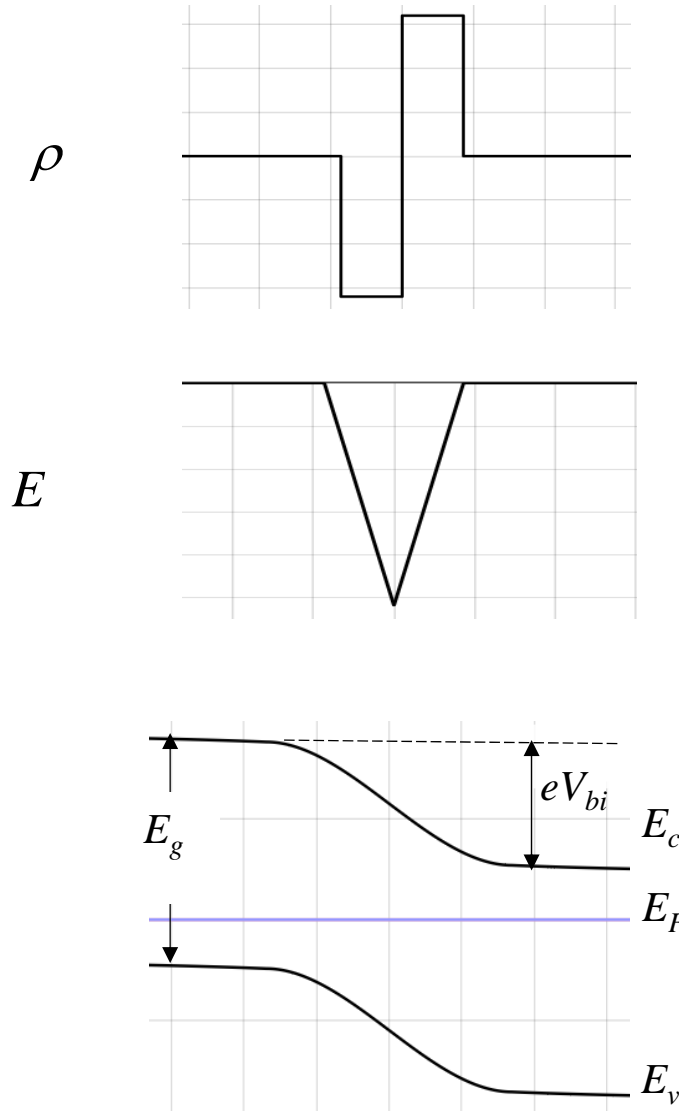


# Biased pn - Junctions

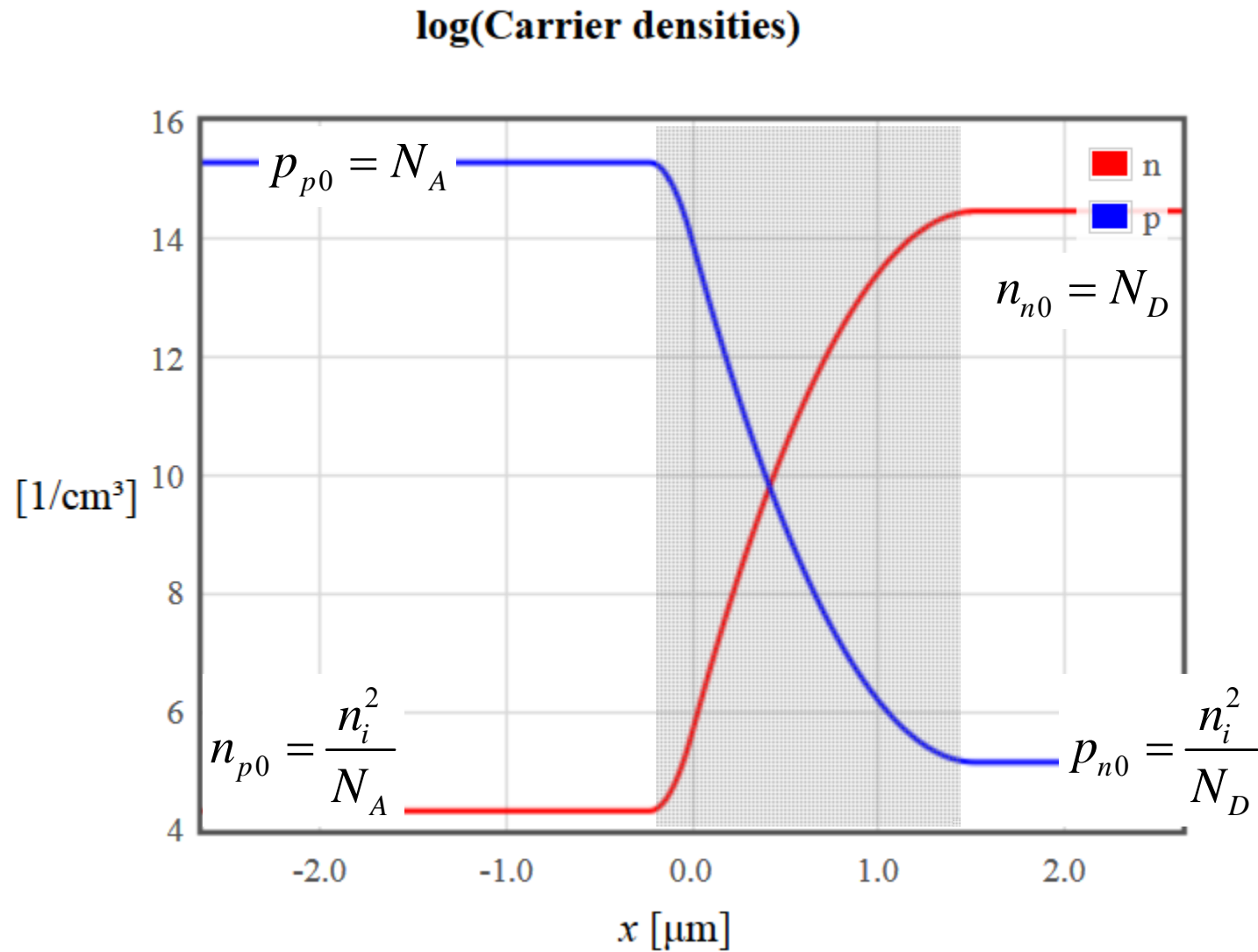
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# abrupt pn junction



$$eV_{bi} = k_B T \ln \left( \frac{N_D N_A}{n_i^2} \right)$$

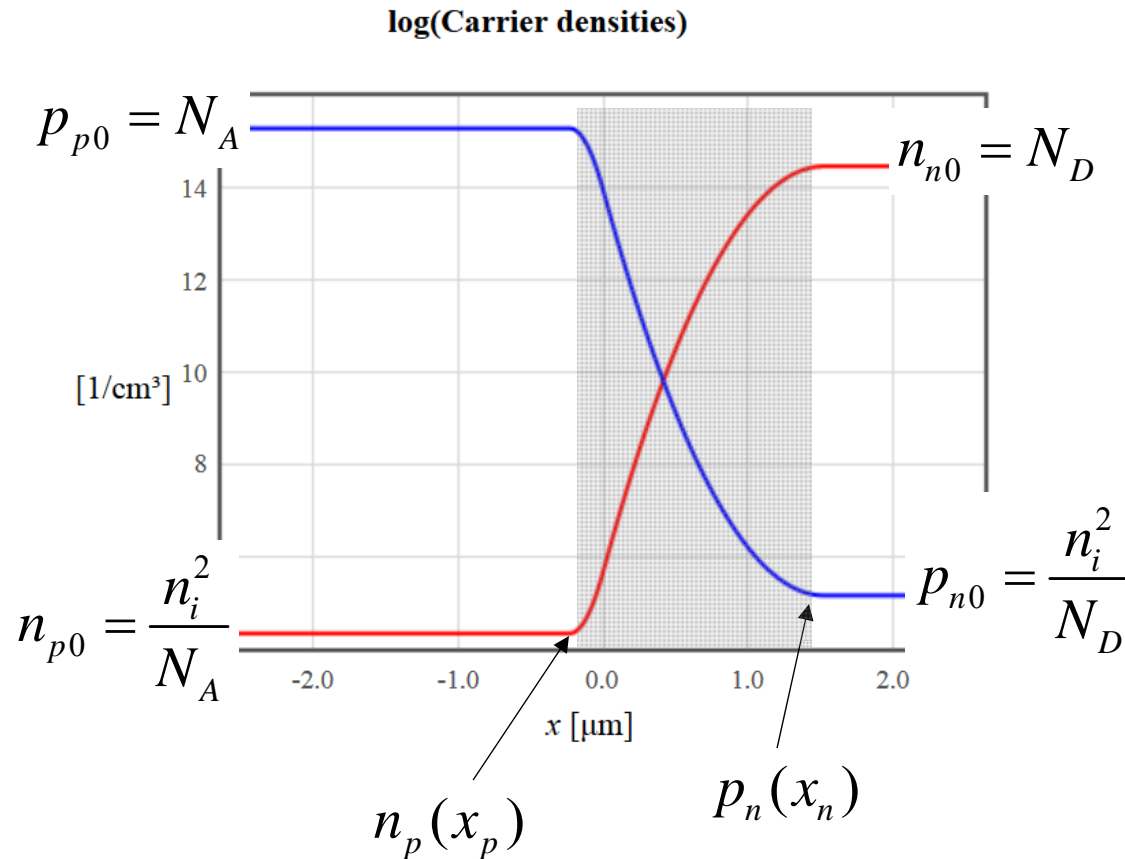
# Equilibrium concentrations, $V = 0$



$$n_{p0}p_{p0} = n_{n0}p_{n0} = n_i^2$$

# Bias voltage, $V = 0$

$$eV_{bi} = k_B T \ln \left( \frac{N_D N_A}{n_i^2} \right) = k_B T \ln \left( \frac{N_D}{n_{p0}} \right) = k_B T \ln \left( \frac{N_A}{p_{n0}} \right)$$



$$n_{p0} p_{p0} = n_{n0} p_{n0} = n_i^2$$

**$V = 0$**

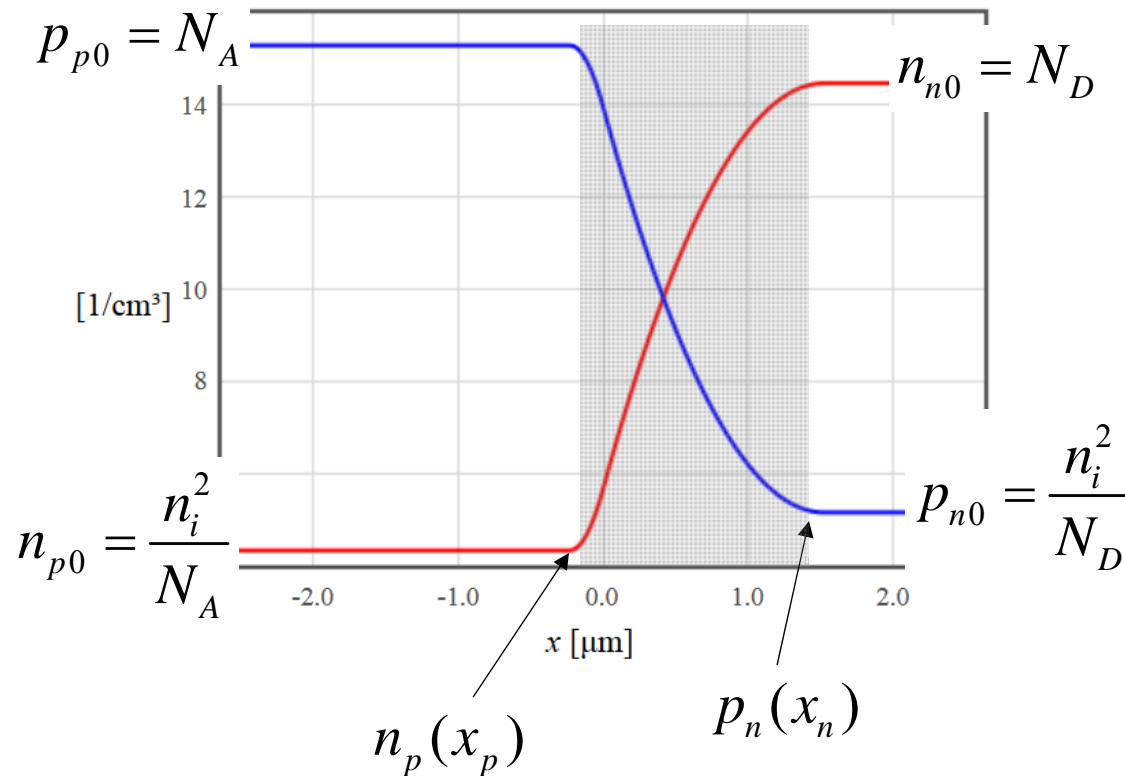
$$n_{p0} = N_D \exp \left( \frac{-eV_{bi}}{k_B T} \right)$$

$$p_{n0} = N_A \exp \left( \frac{-eV_{bi}}{k_B T} \right)$$

# Bias voltage, $V \neq 0$

$$eV_{bi} = k_B T \ln\left(\frac{N_D N_A}{n_i^2}\right) = k_B T \ln\left(\frac{N_D}{n_{p0}}\right) = k_B T \ln\left(\frac{N_A}{p_{n0}}\right)$$

log(Carrier densities)



$$n_{p0} p_{p0} = n_{n0} p_{n0} = n_i^2$$

$V = 0$

$$n_{p0} = N_D \exp\left(\frac{-eV_{bi}}{k_B T}\right)$$

$$p_{n0} = N_A \exp\left(\frac{-eV_{bi}}{k_B T}\right)$$

$V \neq 0$

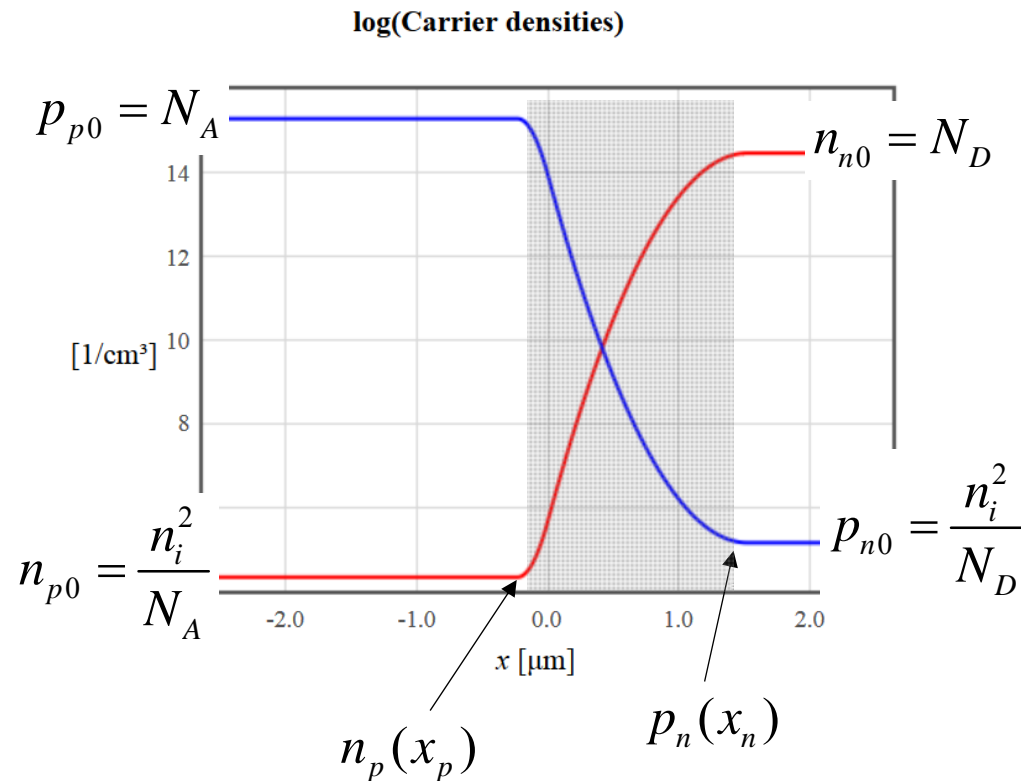
$$n_p(x_p) = N_D \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

$$p_n(x_n) = N_A \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right)$$

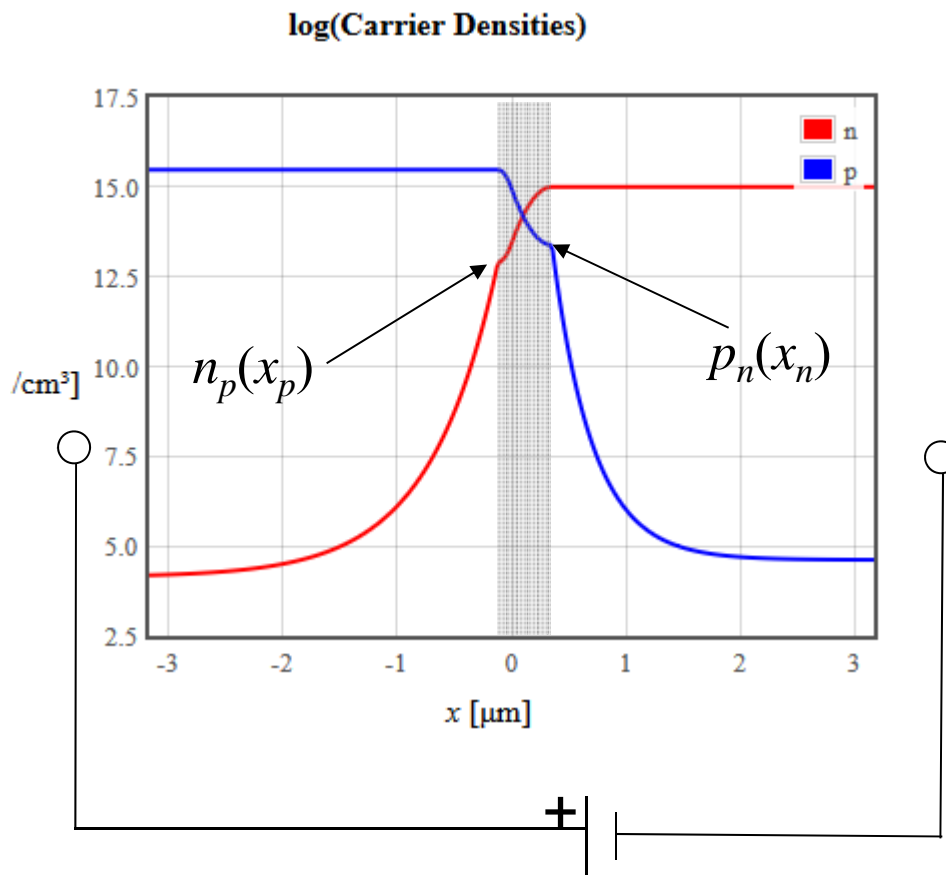
# Bias voltage, $V \neq 0$

$$n_p(x_p) = N_D \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_n(x_n) = N_A \exp\left(\frac{-e(V_{bi} - V)}{k_B T}\right) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$



# Forward bias, $V > 0$



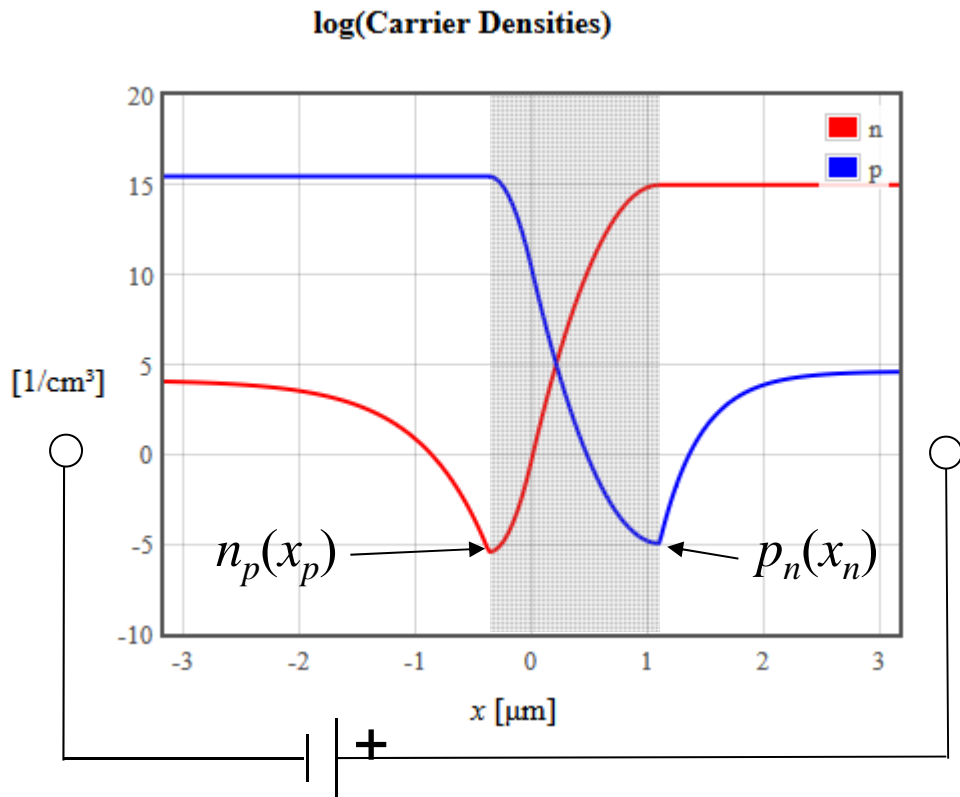
Electrons and holes are driven towards the junction.  
The depletion region becomes narrower

$$n_p(x_p) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_n(x_n) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$

Minority electrons are injected into the p-region  
Minority holes are injected into the n-region

# Reverse bias, $V < 0$



Electrons and holes are driven away from the junction.

The depletion region becomes wider

$$n_p(x_p) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_n(x_n) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$

Minority electrons are extracted from the p-region by the electric field  
 Minority holes are extracted from the n-region by the electric field

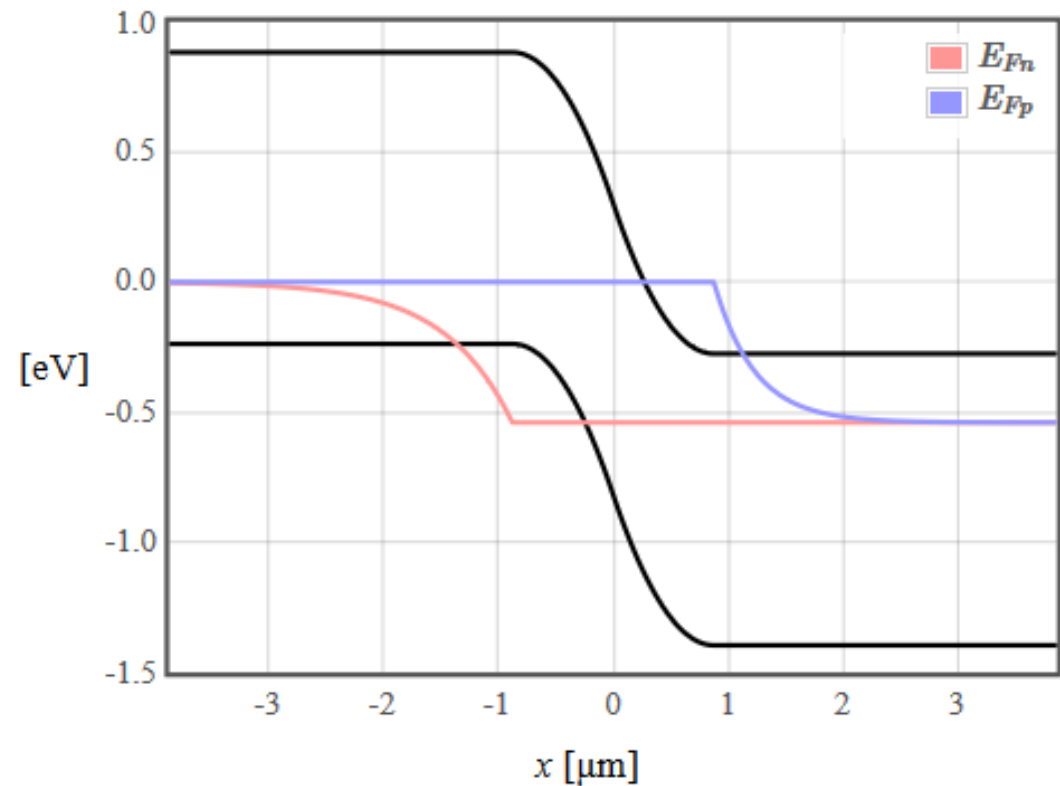


# Quasi Fermi level

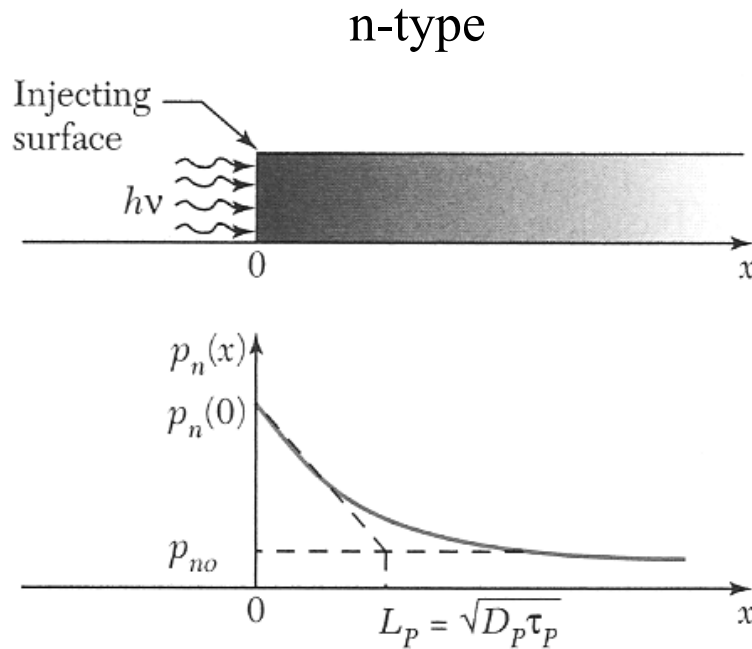
When the charge carriers are not in equilibrium the Fermi energy can be different for electrons and holes.

$$n = N_c \exp\left(\frac{E_{Fn} - E_c}{k_B T}\right)$$

$$p = N_v \exp\left(\frac{E_v - E_{Fp}}{k_B T}\right)$$



# Review of Diffusion



$$D_p \frac{\partial^2 p_n}{\partial x^2} = \frac{p_n - p_{n0}}{\tau_p}$$

recombination time

$$p_n(x) = p_{n0} + (p_n(0) - p_{n0}) \exp\left(\frac{-x}{L_p}\right)$$

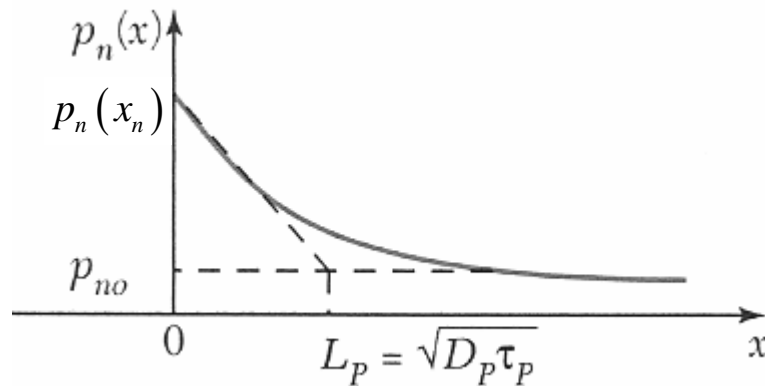
$$L_p = \sqrt{D_p \tau_p}$$

diffusion length

Injection only occurs at the surface. There the minority carrier density is  $p_n(0)$ .

# Diffusion current

n-type



$$p_n(x) = p_{n0} + (p_n(x_n) - p_{n0}) \exp\left(\frac{-x}{L_p}\right)$$

$$J_{diff,p} = -eD_p \frac{dp}{dx}$$


$$J_{diff,p} = -eD_p \frac{dp}{dx} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p} \exp\left(\frac{-x}{L_p}\right)$$


At the edge of the depletion region:

$$J_{diff,p} = -eD_p \frac{dp}{dx} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p}$$

# Diffusion current

---

$$J_{diff,p} = (p_n(x_n) - p_{n0}) \frac{eD_p}{L_p}$$
$$p_n(x_n) = p_{p0} \exp\left(-\frac{e(V_{bi} - V)}{k_B T}\right)$$


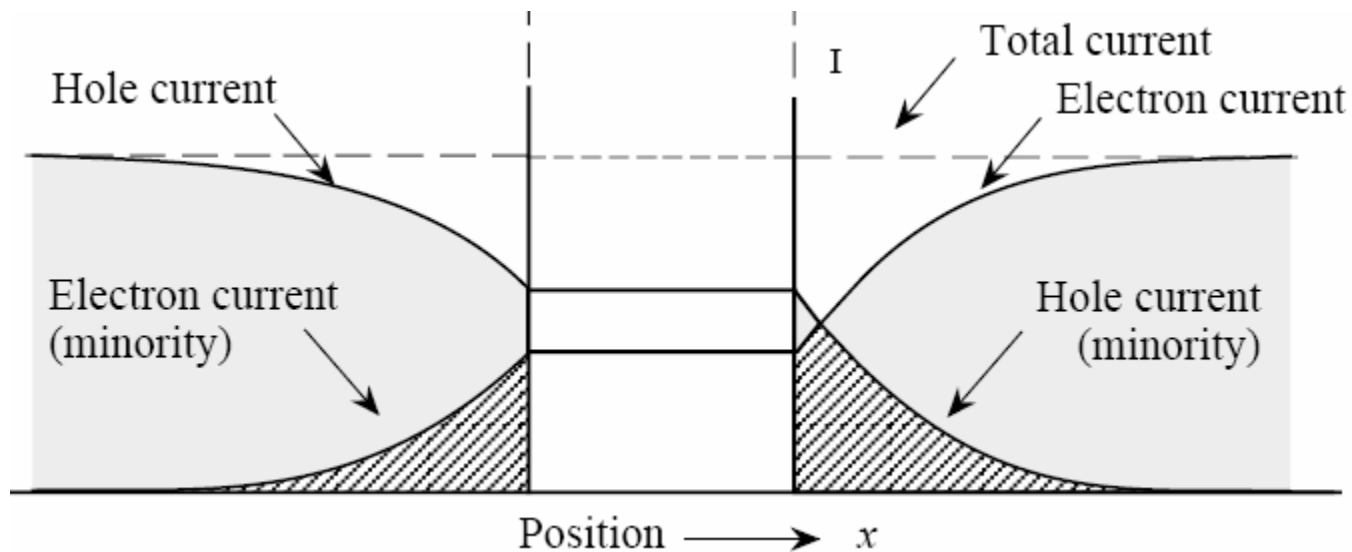
$$J_{diff,p} = \left( p_{p0} \exp\left(-\frac{e(V_{bi} - V)}{k_B T}\right) - p_{n0} \right) \frac{eD_p}{L_p}$$
$$p_{p0} = p_{n0} \exp\left(\frac{eV_{bi}}{k_B T}\right)$$


$$J_{diff,p} = p_{n0} \frac{eD_p}{L_p} \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

# Diffusion current

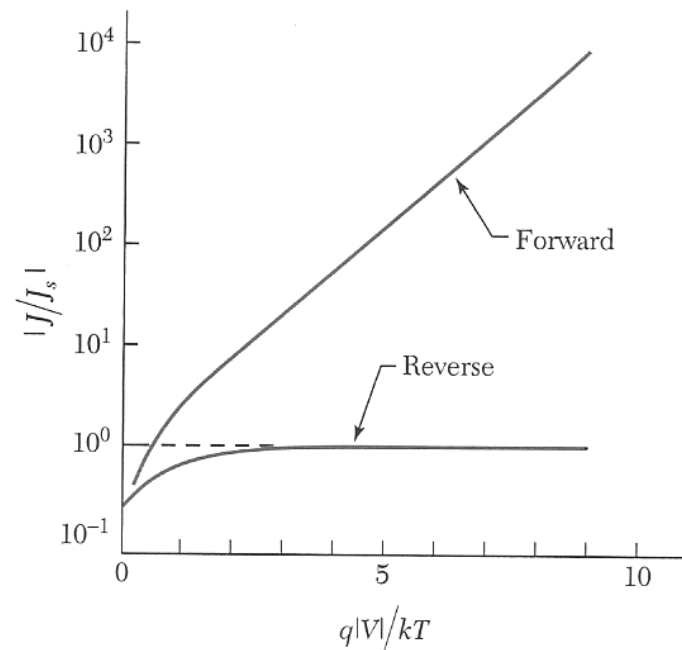
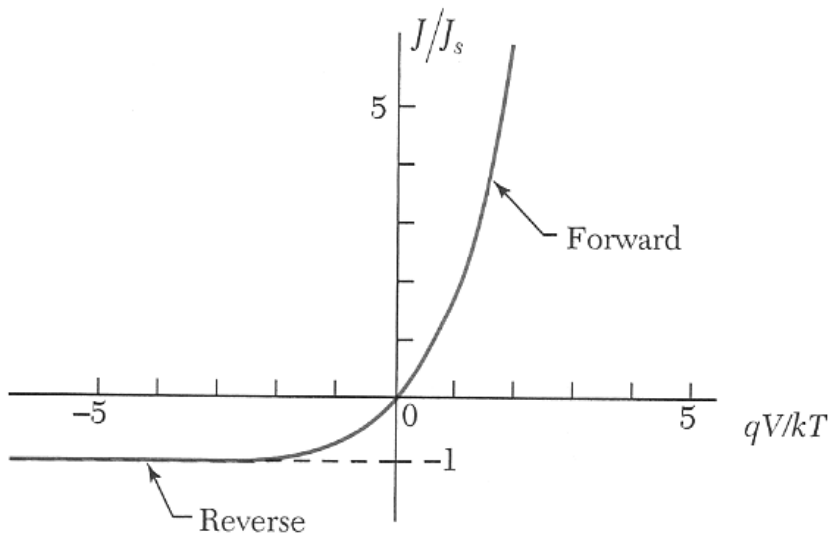
$$J_{diff,p} = \frac{p_{n0} e D_p}{L_p} \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

$$J_{diff,n} = \frac{n_{p0} e D_n}{L_n} \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

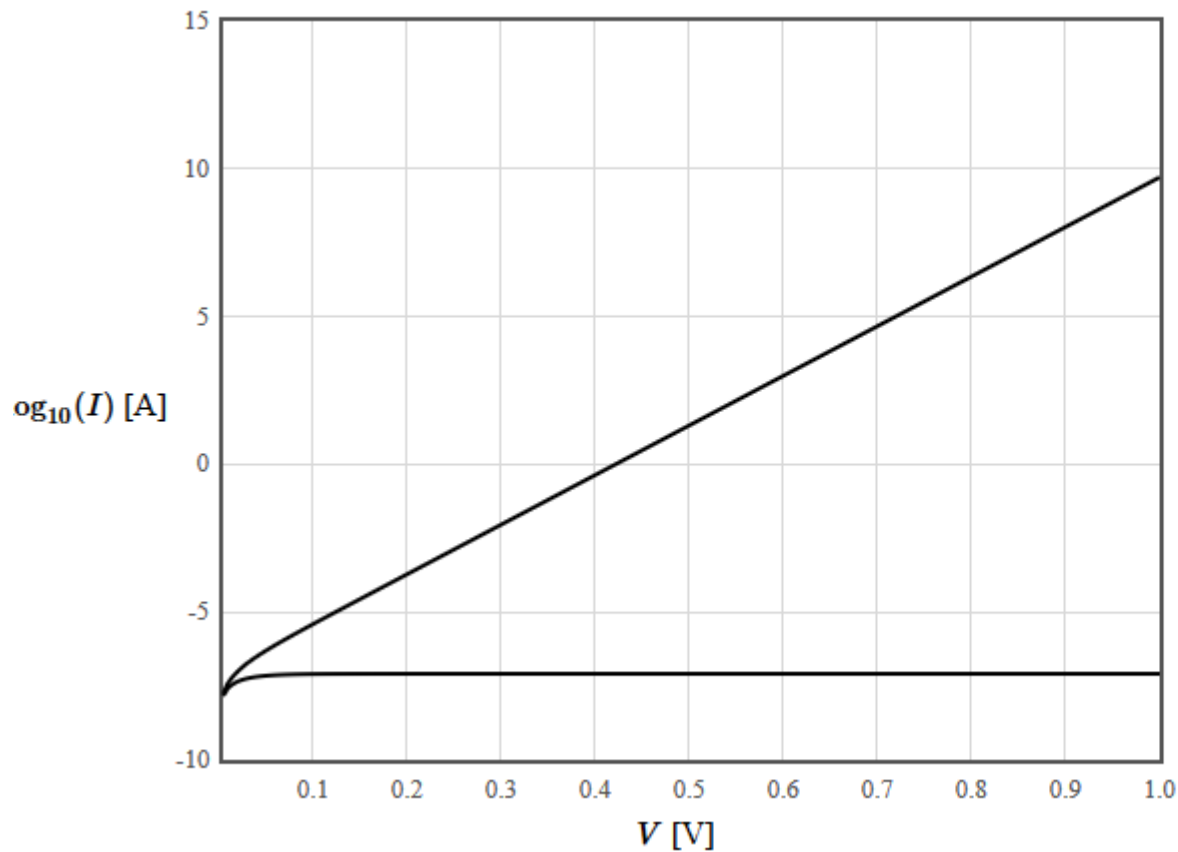


# Diode current

$$I = \underset{\substack{\uparrow \\ \text{Area}}}{eA} \left( \frac{p_{n0} D_p}{L_p} + \frac{n_{p0} D_n}{L_n} \right) \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right) = \underset{\substack{\uparrow \\ \text{Saturation current}}}{I_s} \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$



# Diode I-V characteristics



$A = 1E-3$  cm<sup>2</sup>  
 $N_c(300K) = 1.04E19$  cm<sup>-3</sup>  
 $N_v(300K) = 6.0E18$  cm<sup>-3</sup>  
 $E_g = 0.7437-4.77E-4T^*T/(T+235)$  eV

$\mu_p = 1900$  cm<sup>2</sup>/Vs  
 $\tau_p = 1E-8$  s  
 $N_a = 1E17$  cm<sup>-3</sup>

$\mu_n = 3900$  cm<sup>2</sup>/Vs  
 $\tau_n = 1E-8$  s  
 $N_d = 5E17$  cm<sup>-3</sup>

$T = 300$  K

Replot

Si Ge GaAs

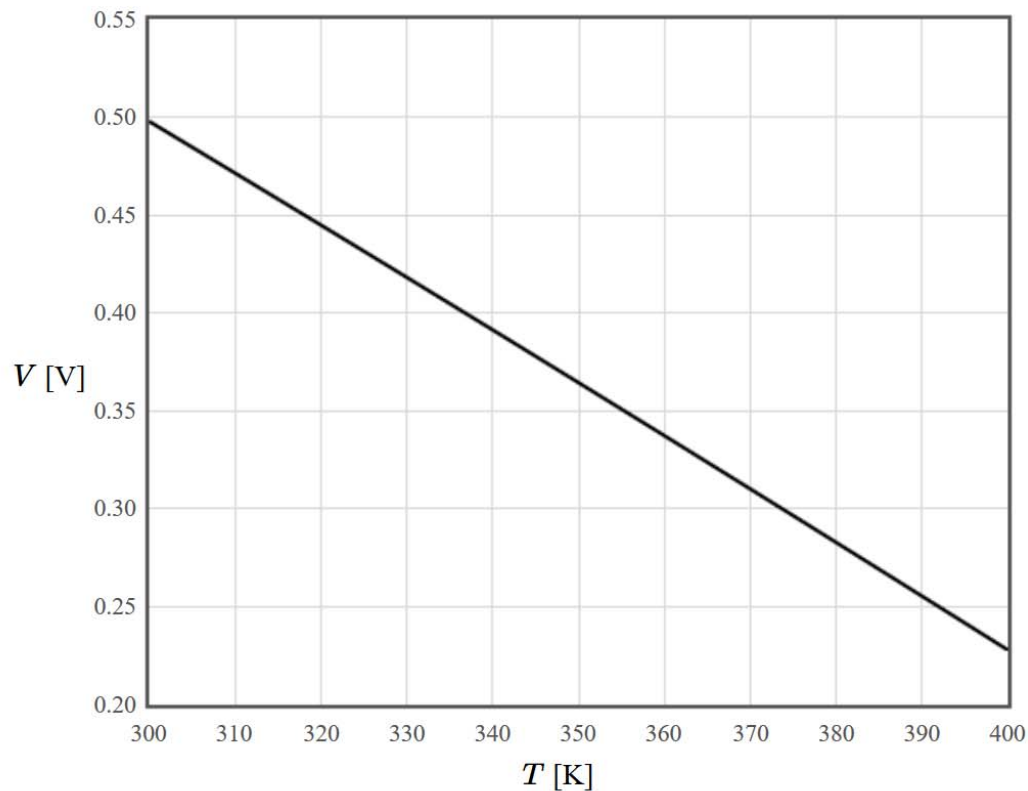
<http://lamp.tu-graz.ac.at/~hadley/psd/L6/pnIV.php>

# Thermometer

$$I_S = Aen_i^2 \left( \frac{D_p}{L_p N_d} + \frac{D_n}{L_n N_a} \right)$$

$$n_i = \sqrt{N_c \left( \frac{T}{300} \right)^{3/2} N_v \left( \frac{T}{300} \right)^{3/2} \exp\left( \frac{-E_g}{2k_B T} \right)}$$

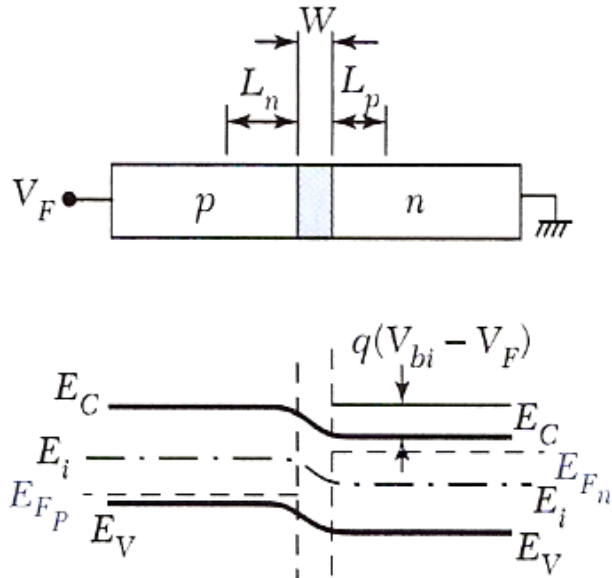
$$D_n = \frac{\mu_n k_B T}{e}$$



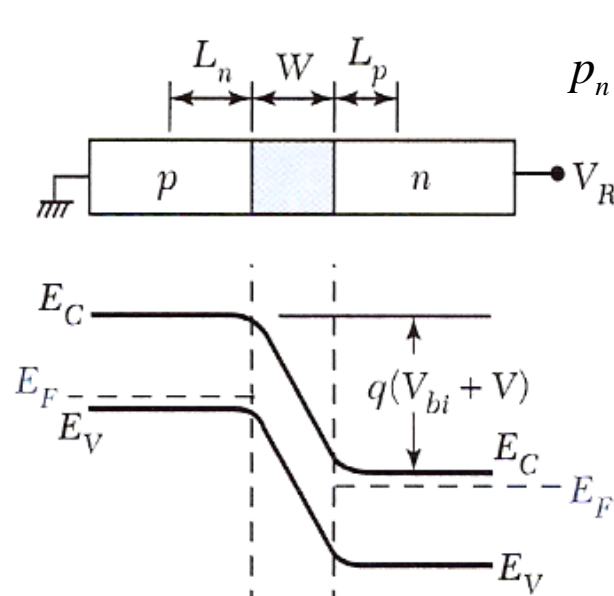
$A$	<input type="text" value="1E-3"/>	cm <sup>2</sup>
$N_c(300K)$	<input type="text" value="2.78E19"/>	cm <sup>-3</sup>
$N_v(300K)$	<input type="text" value="9.84E18"/>	cm <sup>-3</sup>
$E_g$	<input type="text" value="1.166-4.73E-4*T*(T+636)"/>	eV
$\mu_p$	<input type="text" value="480"/>	cm <sup>2</sup> /Vs
$\tau_p$	<input type="text" value="1E-8"/>	s
$N_a$	<input type="text" value="1E17"/>	cm <sup>-3</sup>
$\mu_n$	<input type="text" value="1350"/>	cm <sup>2</sup> /Vs
$\tau_n$	<input type="text" value="1E-8"/>	s
$N_d$	<input type="text" value="5E17"/>	cm <sup>-3</sup>
$T_{start}$	<input type="text" value="300"/>	K
$T_{stop}$	<input type="text" value="400"/>	K
$I$	<input type="text" value="1E-6"/>	A
<input type="button" value="Replot"/>		
<input type="button" value="Si"/> <input type="button" value="Ge"/> <input type="button" value="GaAs"/>		



# Forward



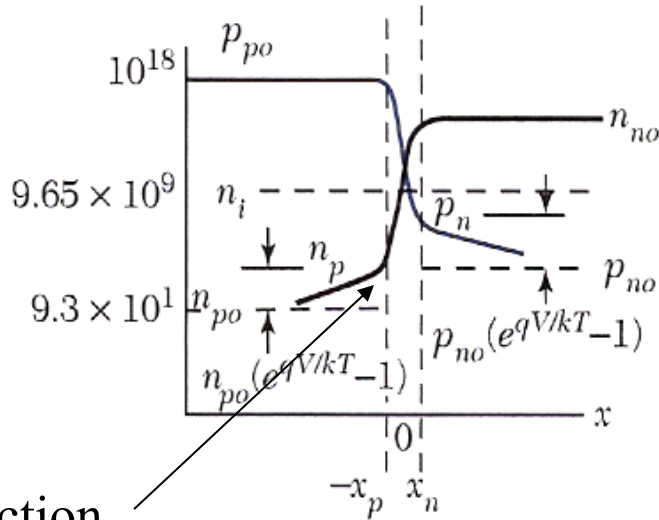
# Reverse



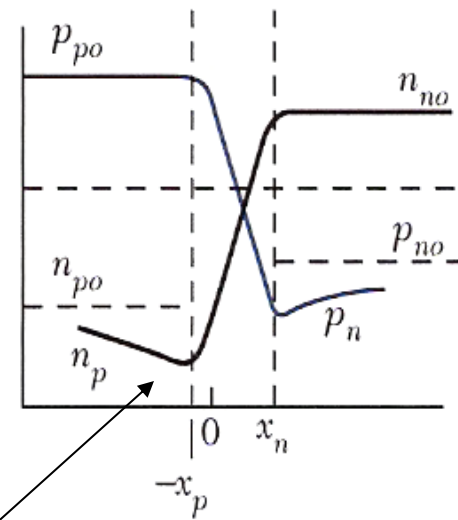
$$n_p(x_p) = n_{p0} \exp\left(\frac{eV}{k_B T}\right)$$

$$p_n(x_n) = p_{n0} \exp\left(\frac{eV}{k_B T}\right)$$

$$J_{diff} > J_{drift}$$



$$J_{diff} < J_{drift}$$



Injection

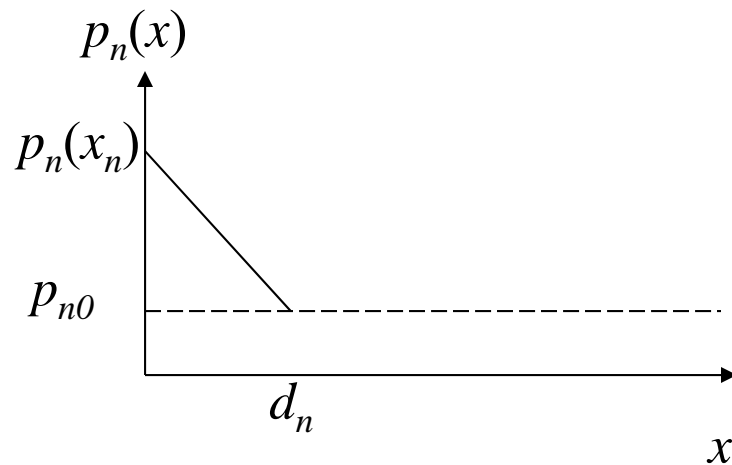
Extraction

# Short diode

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n-type

$$d_n \ll L_p$$



Metal contact is much closer to the depletion region than the diffusion length

$$J_{diff,p} = -eD_p \frac{dp}{dx}$$

$$J_{diff,p} = -eD_p \frac{dp}{dx} = \frac{eD_p}{d_n} (p_n(x_n) - p_{n0})$$

# Diffusion current

---

$$J_{diff,p} = (p_n(x_n) - p_{n0}) \frac{eD_p}{d_n}$$

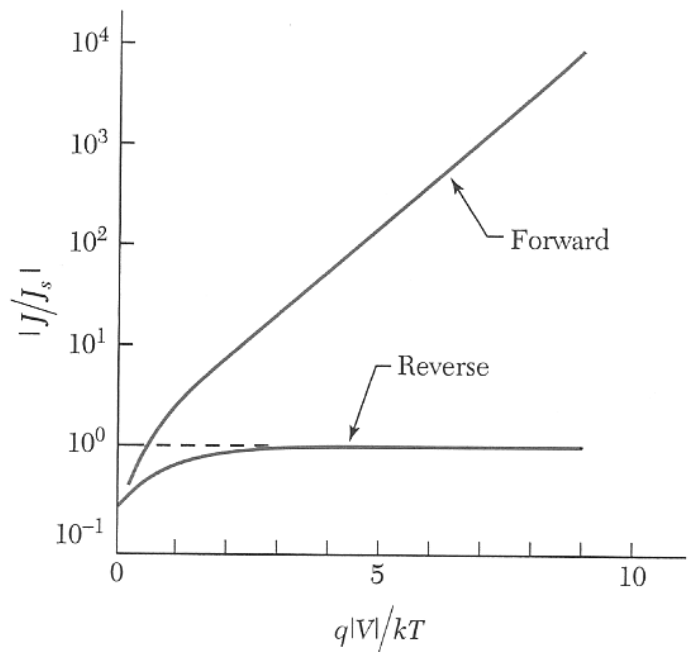
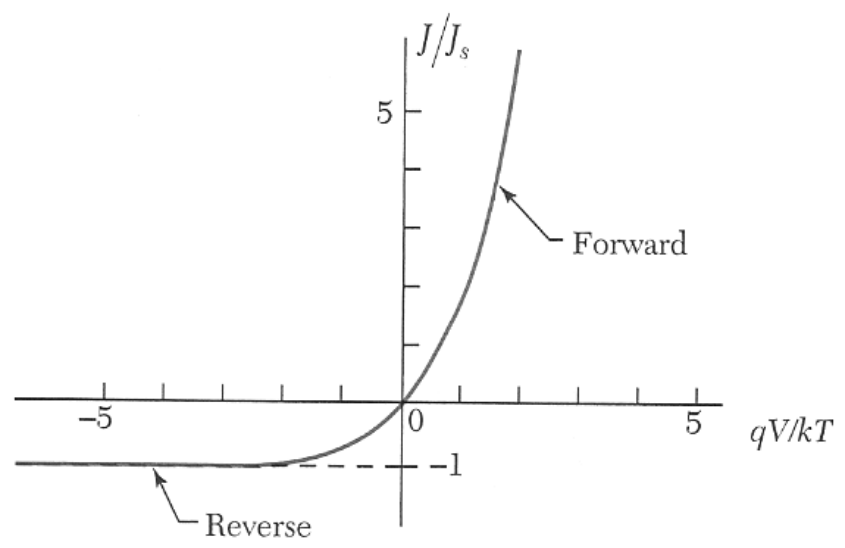
$$J_{diff,p} = \left( p_{n0} \exp\left(\frac{e(V)}{k_B T}\right) - p_{n0} \right) \frac{eD_p}{d_n}$$

$$J_{diff,p} = \frac{p_{n0} eD_p}{d_n} \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

# Short diode current

$$I = eA \left( \frac{p_{n0} D_p}{d_n} + \frac{n_{p0} D_n}{d_p} \right) \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right) = I_s \left( \exp\left(\frac{eV}{k_B T}\right) - 1 \right)$$

Area



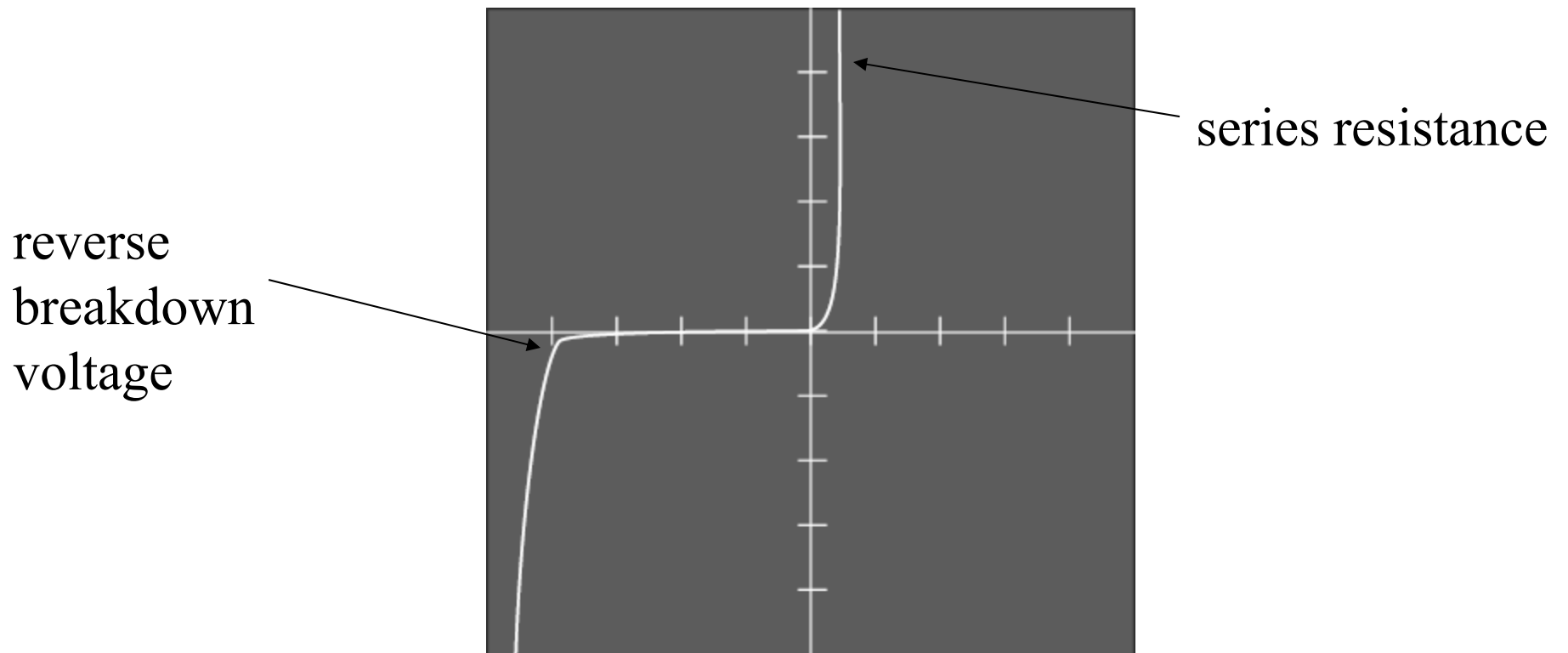
# Real diodes

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$$I = I_s \left( \exp\left(\frac{eV}{nk_B T}\right) - 1 \right)$$

$n$  = nonideality factor

$n = 1$  for an ideal diode



# Real diodes

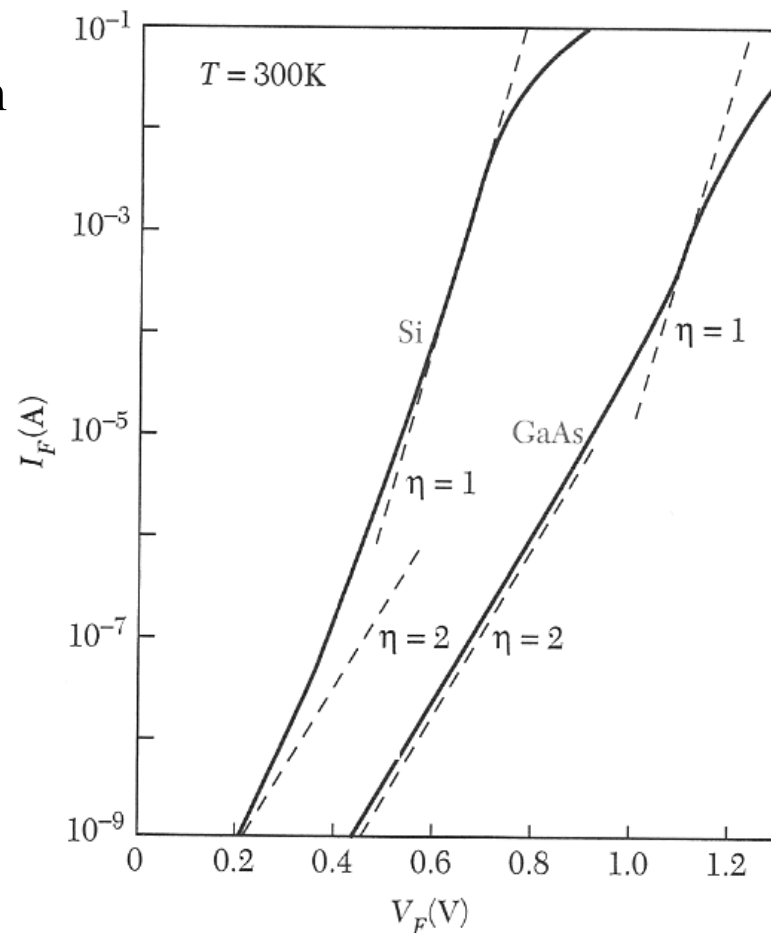
There is constant generation/recombination of electron hole pairs.

In forward bias there is an extra current from recombination.

In reverse bias there is an extra current from generation.

Low bias: recombination dominates,  $n = 2$

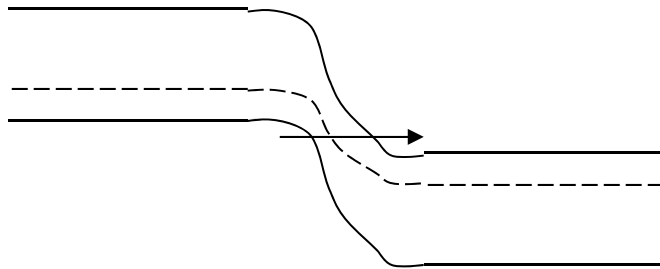
$$I = I_s \left( \exp \left( \frac{eV}{nk_B T} \right) - 1 \right)$$



Very high bias: series resistance

High bias: ideal behavior,  $n = 1$

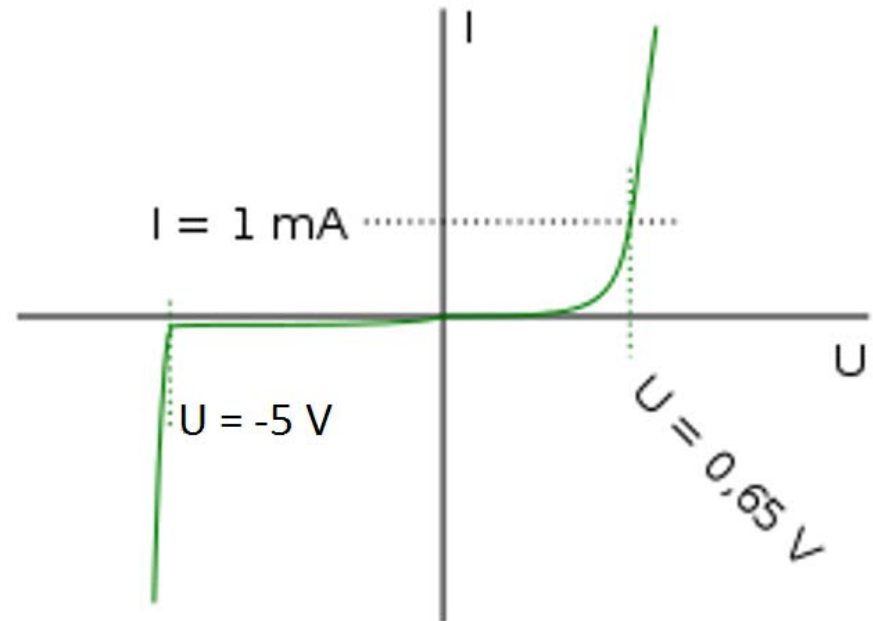
# Zener tunneling



Electrons tunnel from valence band to conduction band

Occurs at high doping

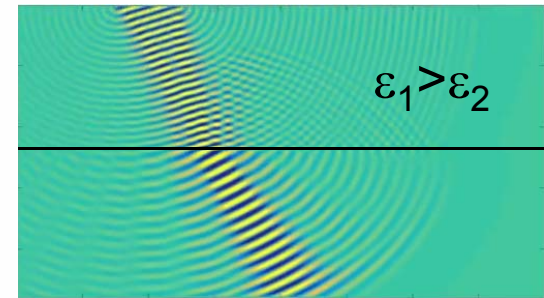
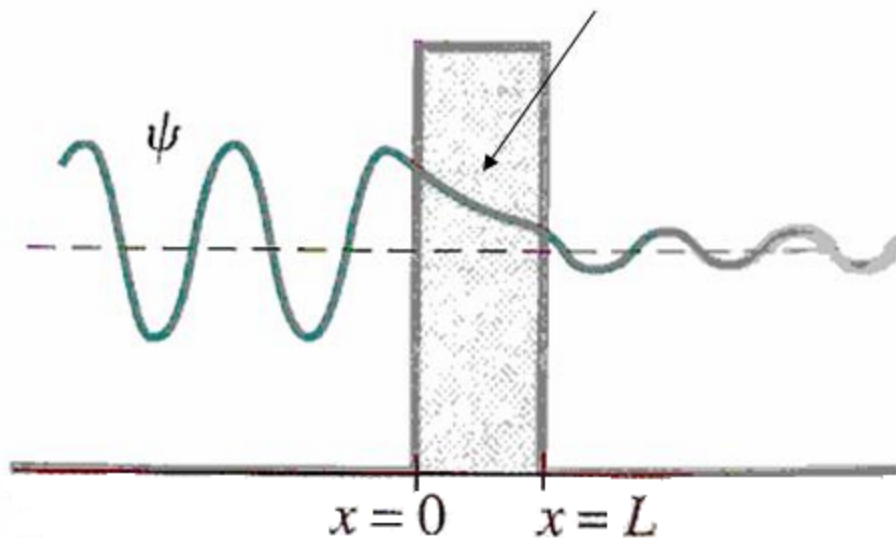
$$|V_{\text{zener}}| < 5.6 \text{ V}$$



# Tunneling

---

wave decays exponentially in the classically forbidden region



Tunneling is a wave phenomena. Tunneling and total internal reflection are used in a beam splitter.



# Zener tunneling

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Breakdown voltage is typically much lower than the breakdown voltage of an avalanche diode and can be tuned by adjusting the width of the depletion layer.

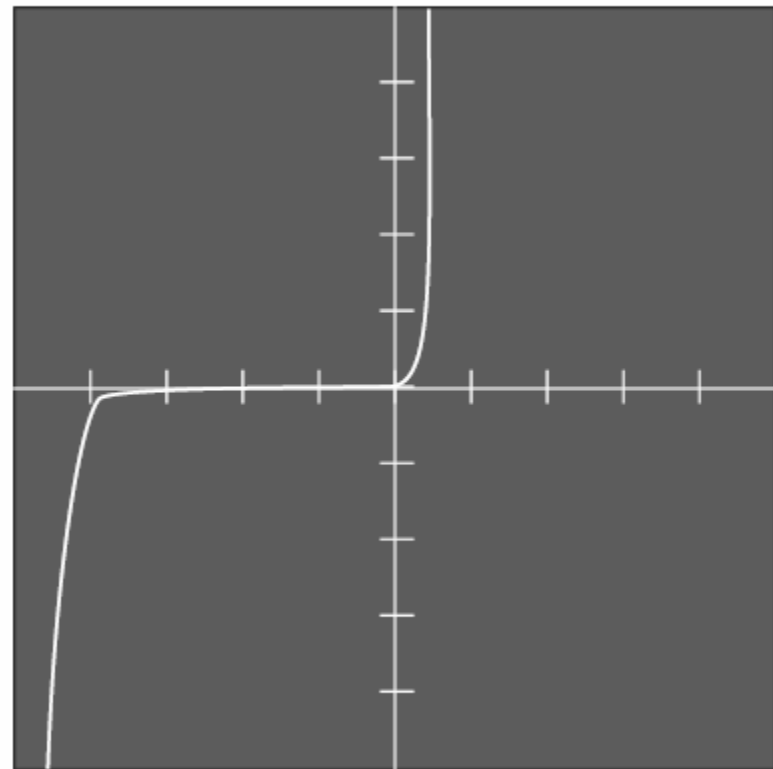
Used to provide a reference voltage.

# Avalanche breakdown

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Impact ionization  
causes an avalanche of  
current

Occurs at low doping



Vertical: 5 mA/div

Horizontal: 5 V/div

# Avalanche breakdown

