

# Electron bands

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## Band structures and Fermi surfaces of metallic elements

Introduction

Literature survey of calculations and experiments

Data for Ac...Bi

Data for C...Cu

Data for Dy...Ir

Data for K...Nd

Data for Ni...Ru

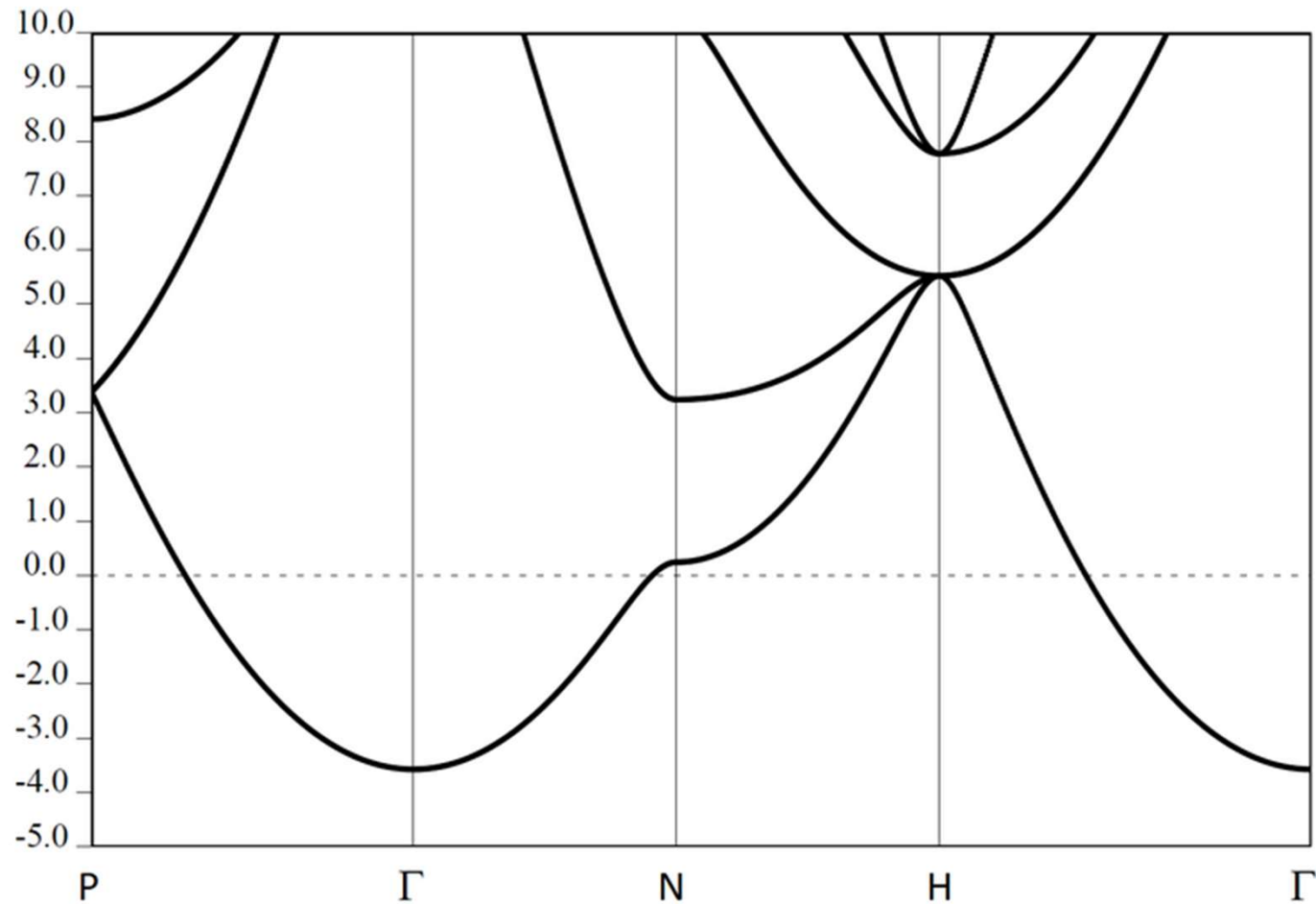
Data for Sb...Ti

Data for Tl...Zr

References

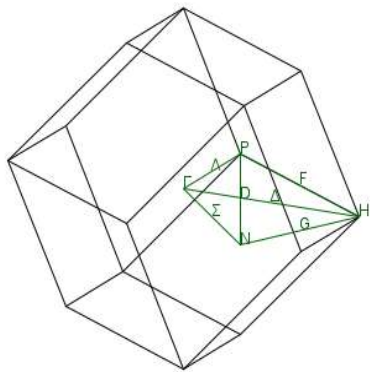
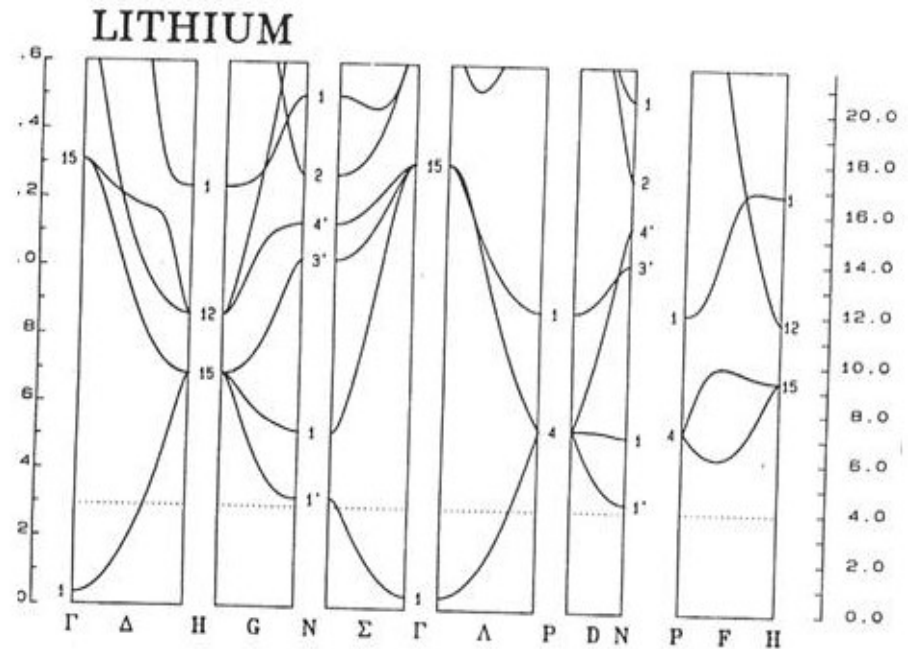
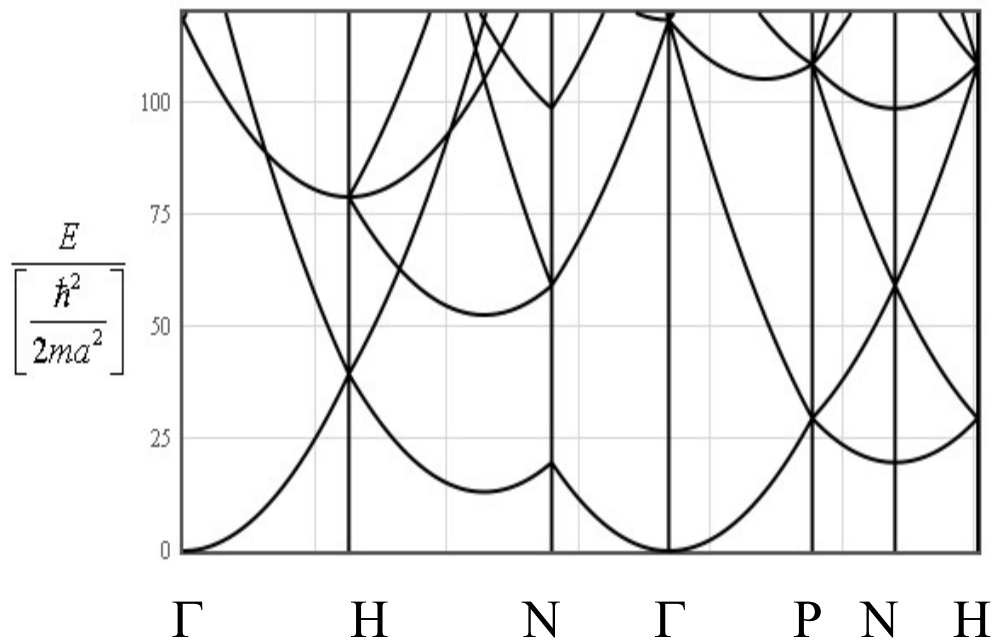
Density Functional Theory (DFT)

## Bandstructure of bcc lithium (Li)

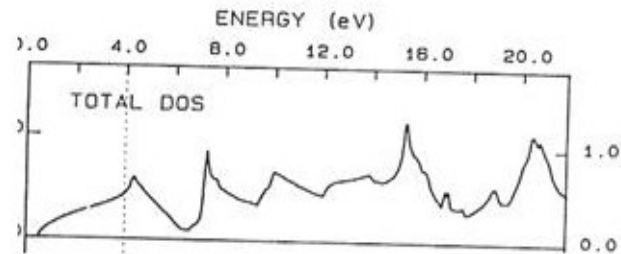
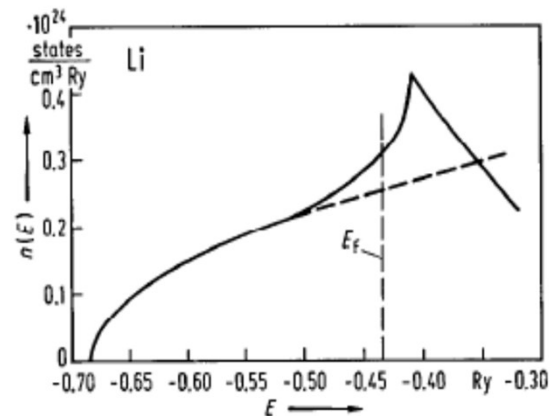


[http://lampx.tugraz.at/~hadley/ss1/bands/bandstructures/Li/Li\\_Bandstructure.html](http://lampx.tugraz.at/~hadley/ss1/bands/bandstructures/Li/Li_Bandstructure.html)

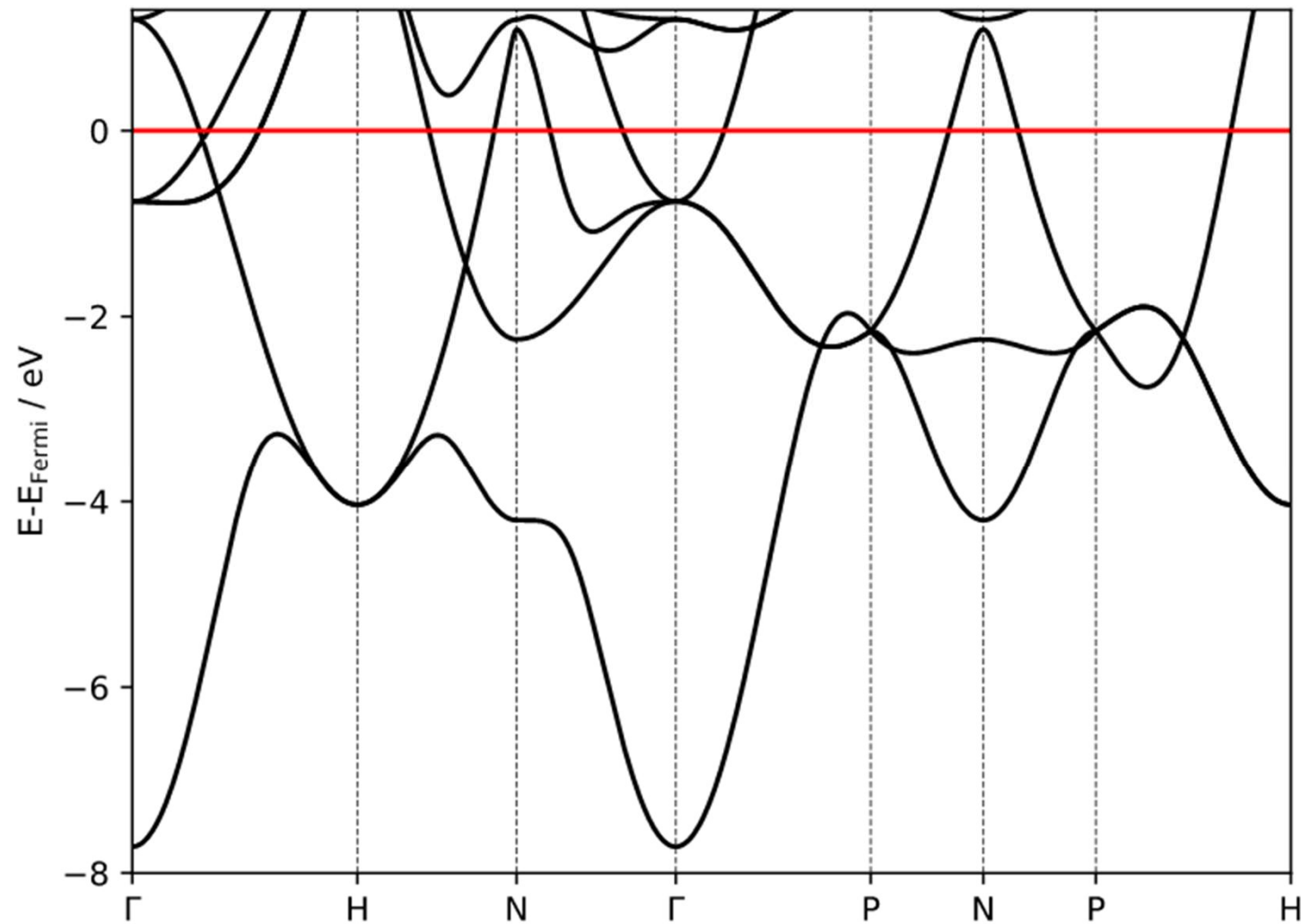
# Lithium bcc



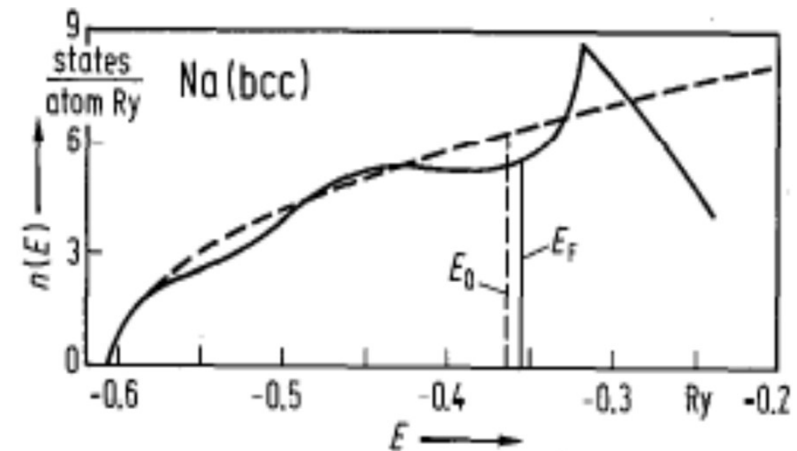
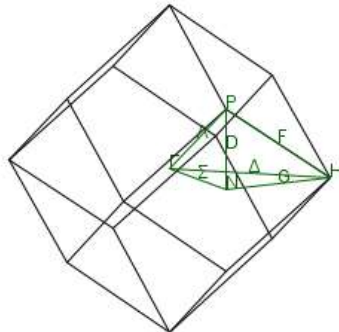
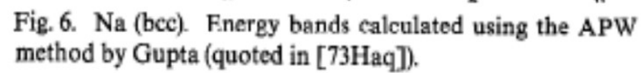
Density of states



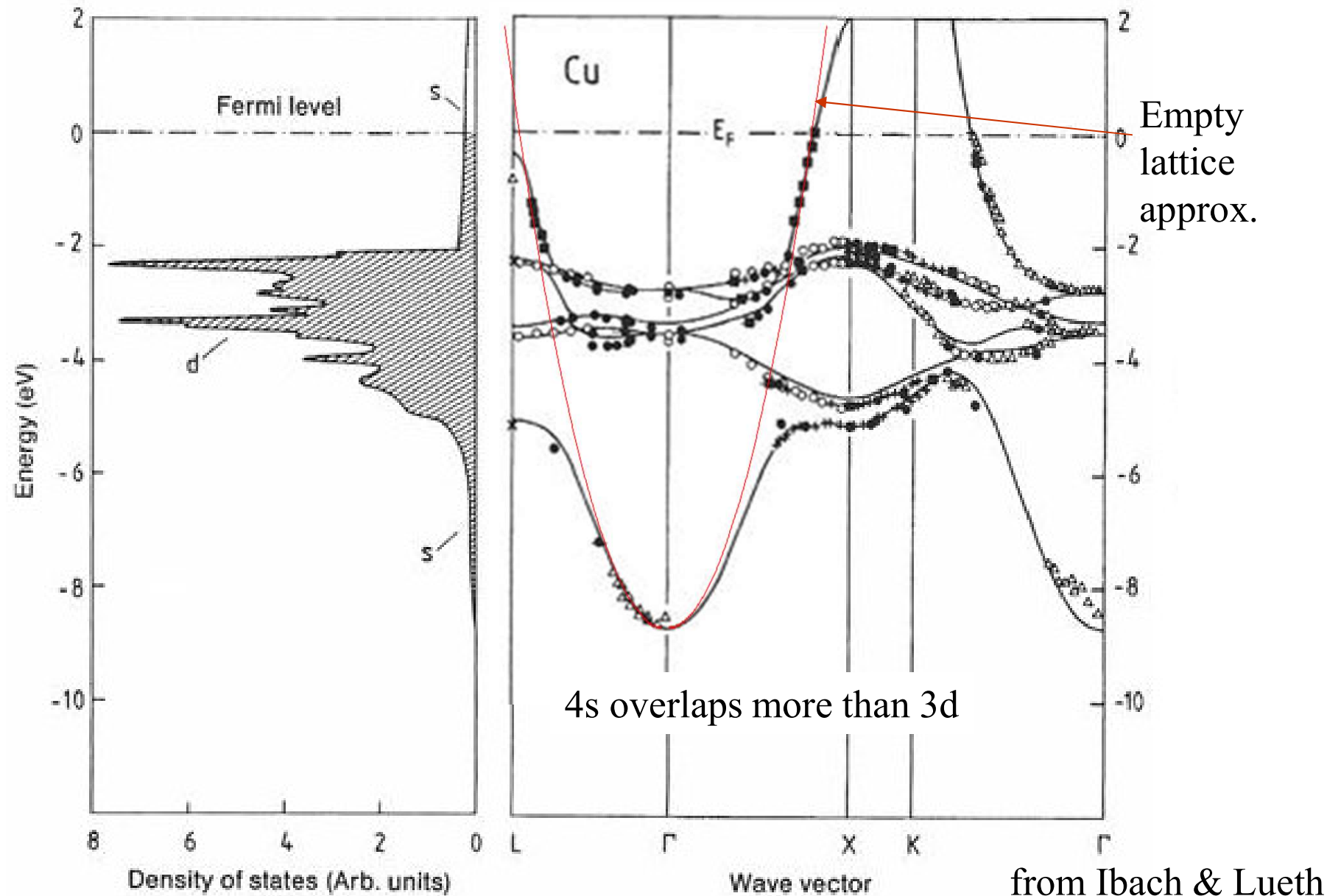
## Bandstructure of bcc chromium (Cr)



[http://lampx.tugraz.at/~hadley/ss1/bands/bandstructures/Cr/Cr\\_Bandstructure.html](http://lampx.tugraz.at/~hadley/ss1/bands/bandstructures/Cr/Cr_Bandstructure.html)



# Copper dispersion relation and density of states





# Silver

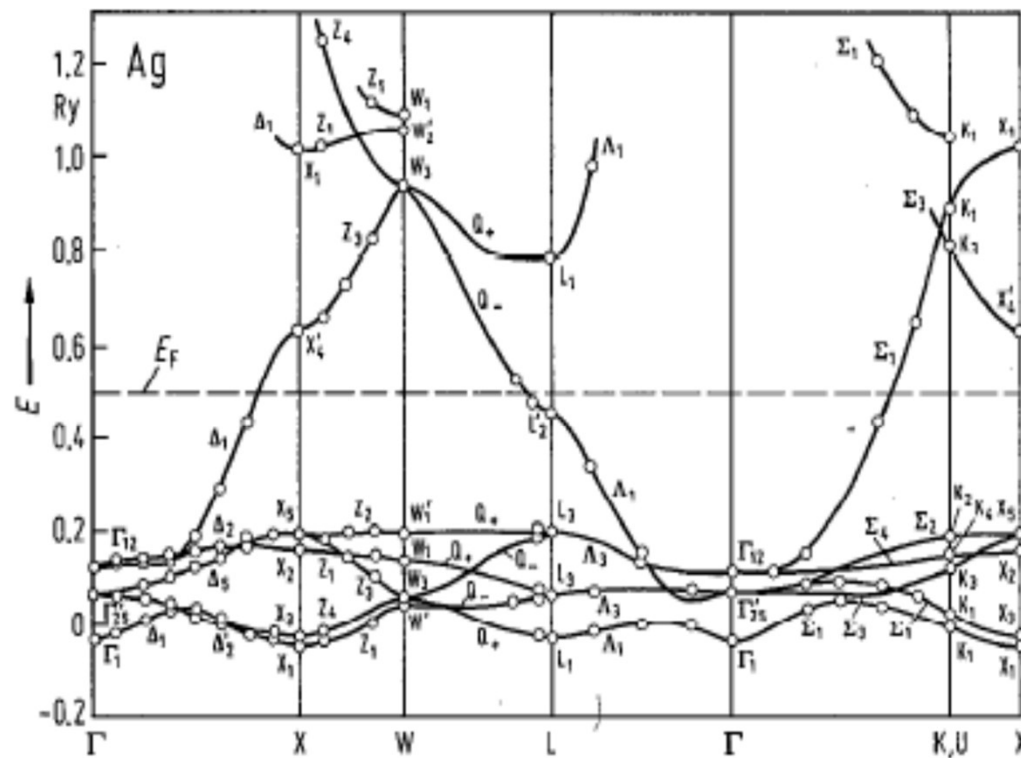


Fig. 3. Ag. Energy bands calculated using the APW method [69Chr].

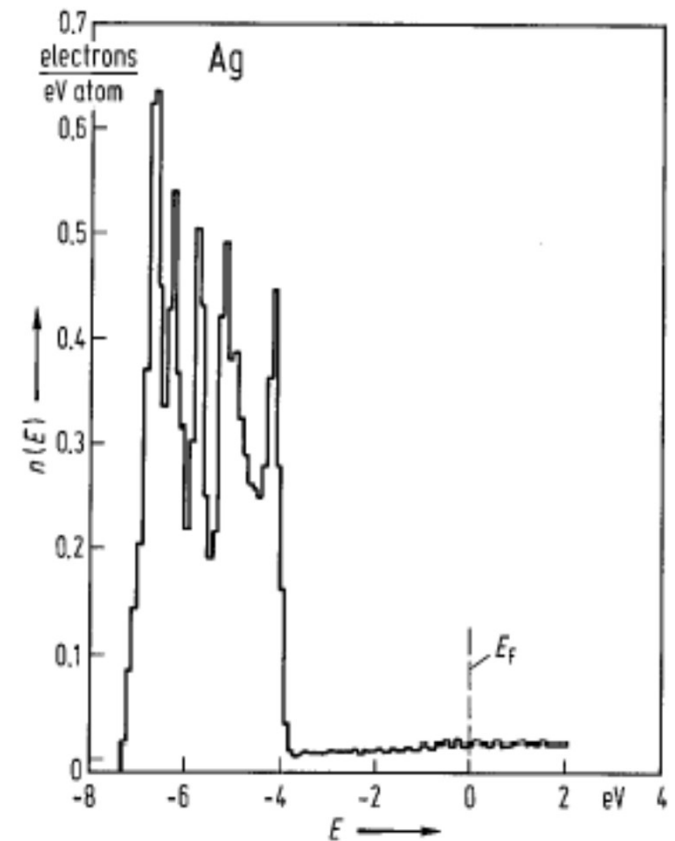


Fig. 15. Ag. Density of states calculated from the energy bands in Fig. 10. Ag [75Fon].



# Gold

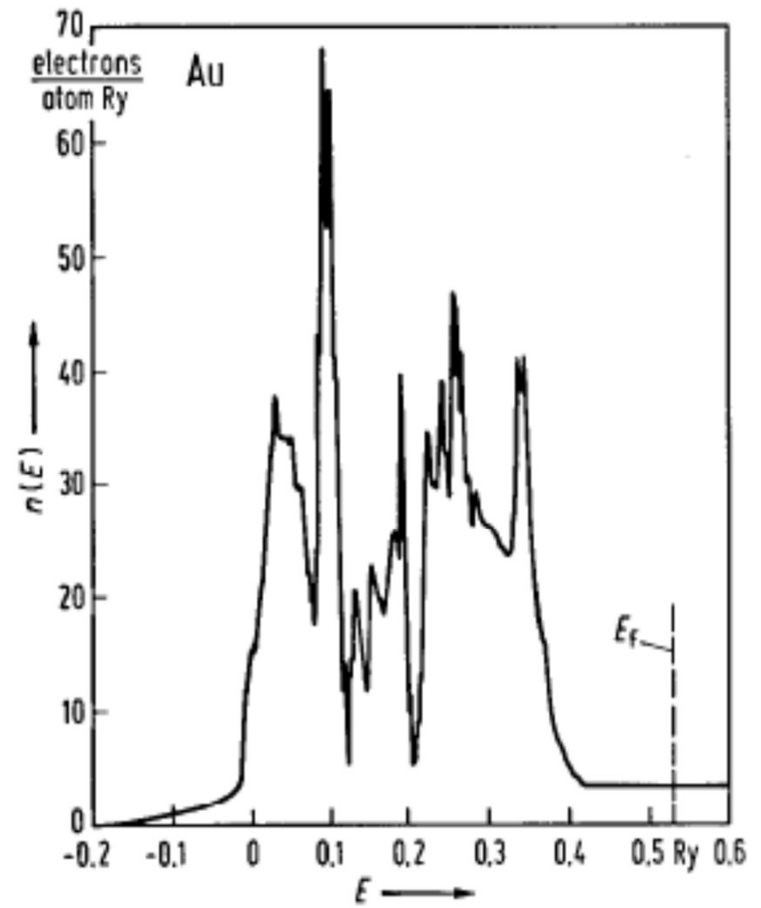
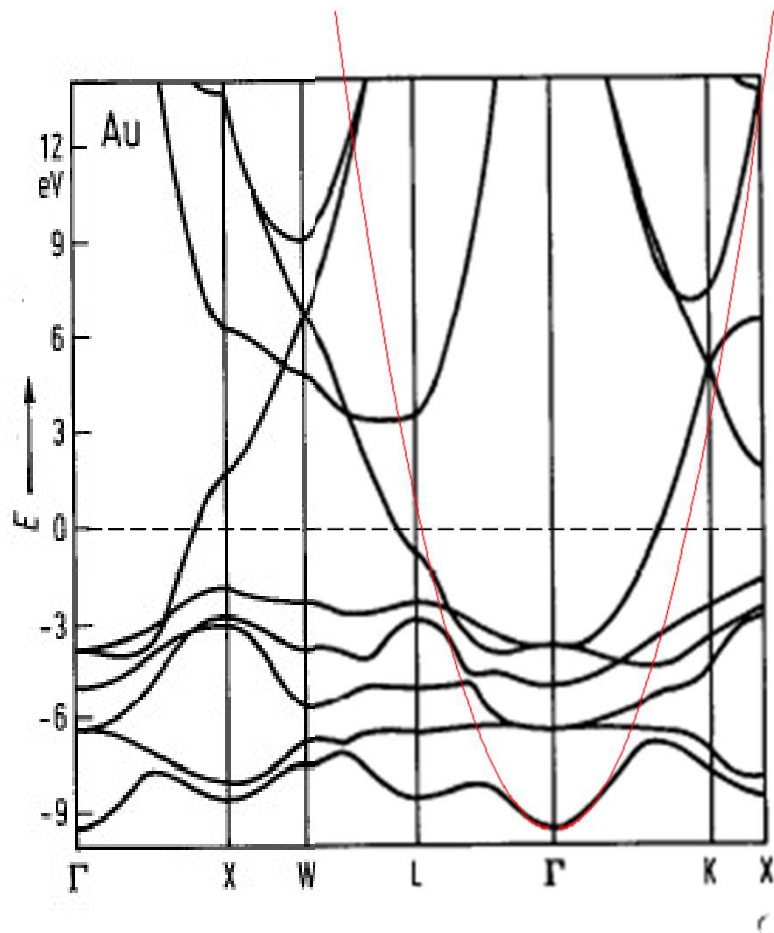


Fig. 9. Au. Density of states calculated from the energy bands in Fig. 4b. Au [71Chr2].

hydrogen 1 <b>H</b> 1.0079																		helium 2 <b>He</b> 4.0026																			
lithium 3 <b>Li</b> 6.941		beryllium 4 <b>Be</b> 9.0122																		boron 5 <b>B</b> 10.811		carbon 6 <b>C</b> 12.011		nitrogen 7 <b>N</b> 14.007		oxygen 8 <b>O</b> 15.999		fluorine 9 <b>F</b> 18.998		neon 10 <b>Ne</b> 20.180							
sodium 11 <b>Na</b> 22.990		magnesium 12 <b>Mg</b> 24.305																		aluminium 13 <b>Al</b> 26.982		silicon 14 <b>Si</b> 28.086		phosphorus 15 <b>P</b> 30.974		sulfur 16 <b>S</b> 32.065		chlorine 17 <b>Cl</b> 35.453		argon 18 <b>Ar</b> 39.948							
potassium 19 <b>K</b> 39.098		calcium 20 <b>Ca</b> 40.078		scandium 21 <b>Sc</b> 44.956		titanium 22 <b>Ti</b> 47.867		vanadium 23 <b>V</b> 50.942		chromium 24 <b>Cr</b> 51.996		manganese 25 <b>Mn</b> 54.938		iron 26 <b>Fe</b> 55.845		cobalt 27 <b>Co</b> 58.933		nickel 28 <b>Ni</b> 58.693		copper 29 <b>Cu</b> 63.546		zinc 30 <b>Zn</b> 65.39		gallium 31 <b>Ga</b> 69.723		germanium 32 <b>Ge</b> 72.61		arsenic 33 <b>As</b> 74.922		selenium 34 <b>Se</b> 78.96		bromine 35 <b>Br</b> 79.904		krypton 36 <b>Kr</b> 83.80			
rubidium 37 <b>Rb</b> 85.468		strontium 38 <b>Sr</b> 87.62		yttrium 39 <b>Y</b> 88.906		zirconium 40 <b>Zr</b> 91.224		niobium 41 <b>Nb</b> 92.906		molybdenum 42 <b>Mo</b> 95.94		technetium 43 <b>Tc</b> [98]		ruthenium 44 <b>Ru</b> 101.07		rhodium 45 <b>Rh</b> 102.91		palladium 46 <b>Pd</b> 106.42		silver 47 <b>Ag</b> 107.87		cadmium 48 <b>Cd</b> 112.41		indium 49 <b>In</b> 114.82		tin 50 <b>Sn</b> 118.71		antimony 51 <b>Sb</b> 121.76		tellurium 52 <b>Te</b> 127.60		iodine 53 <b>I</b> 126.90		xenon 54 <b>Xe</b> 131.29			
caesium 55 <b>Cs</b> 132.91		barium 56 <b>Ba</b> 137.33		57-70 ★		lutetium 71 <b>Lu</b> 174.97		hafnium 72 <b>Hf</b> 178.49		tantalum 73 <b>Ta</b> 180.95		tungsten 74 <b>W</b> 183.84		rhenium 75 <b>Re</b> 186.21		osmium 76 <b>Os</b> 190.23		iridium 77 <b>Ir</b> 192.22		platinum 78 <b>Pt</b> 195.08		gold 79 <b>Au</b> 196.97		mercury 80 <b>Hg</b> 200.59		thallium 81 <b>Tl</b> 204.38		lead 82 <b>Pb</b> 207.2		bismuth 83 <b>Bi</b> 208.98		polonium 84 <b>Po</b> [209]		astatine 85 <b>At</b> [210]		radon 86 <b>Rn</b> [222]	
francium 87 <b>Fr</b> [223]		radium 88 <b>Ra</b> [226]		89-102 ★ ★		lawrencium 103 <b>Lr</b> [262]		rutherfordium 104 <b>Rf</b> [261]		dubnium 105 <b>Db</b> [262]		seaborgium 106 <b>Sg</b> [266]		bohrium 107 <b>Bh</b> [264]		hassium 108 <b>Hs</b> [269]		meitnerium 109 <b>Mt</b> [268]		ununnium 110 <b>Uun</b> [271]		ununium 111 <b>Uuu</b> [272]		unubium 112 <b>Uub</b> [277]		ununquadium 114 <b>Uuq</b> [289]											

d band metals, transition metals

d band metals, transition metals



\* Lanthanide series

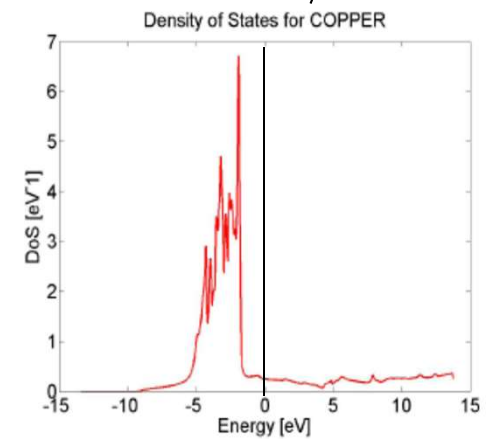
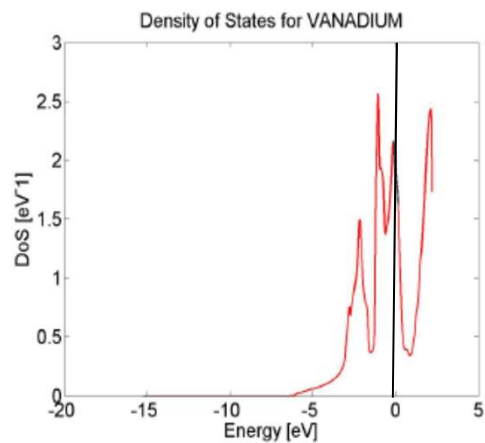
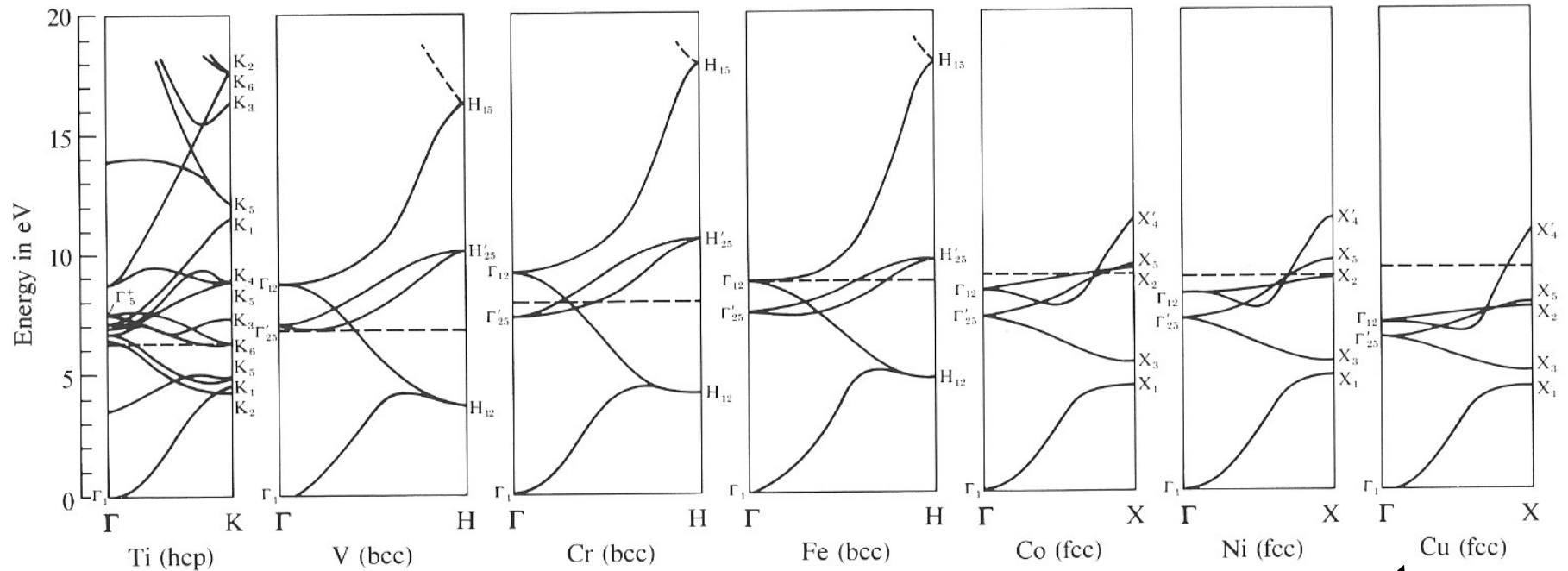
\*\* Actinide series

lanthanum 57 <b>La</b> 138.91	cerium 58 <b>Ce</b> 140.12	praseodymium 59 <b>Pr</b> 140.91	neodymium 60 <b>Nd</b> 144.24	promethium 61 <b>Pm</b> [145]	samarium 62 <b>Sm</b> 150.36	europium 63 <b>Eu</b> 151.96	gadolinium 64 <b>Gd</b> 157.25	terbium 65 <b>Tb</b> 158.93	dysprosium 66 <b>Dy</b> 162.50	holmium 67 <b>Ho</b> 164.93	erbium 68 <b>Er</b> 167.26	thulium 69 <b>Tm</b> 168.93	ytterbium 70 <b>Yb</b> 173.04
actinium 89 <b>Ac</b> [227]	thorium 90 <b>Th</b> 232.04	protactinium 91 <b>Pa</b> 231.04	uranium 92 <b>U</b> 238.03	neptunium 93 <b>Np</b> [237]	plutonium 94 <b>Pu</b> [244]	americium 95 <b>Am</b> [243]	curium 96 <b>Cm</b> [247]	berkelium 97 <b>Bk</b> [247]	californium 98 <b>Cf</b> [251]	einsteinium 99 <b>Es</b> [252]	fermium 100 <b>Fm</b> [257]	mendelevium 101 <b>Md</b> [258]	nobelium 102 <b>No</b> [259]

f band metals, rare earths



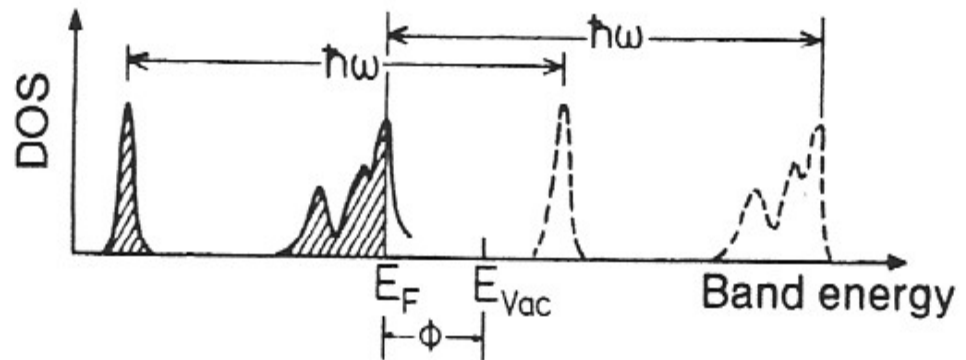
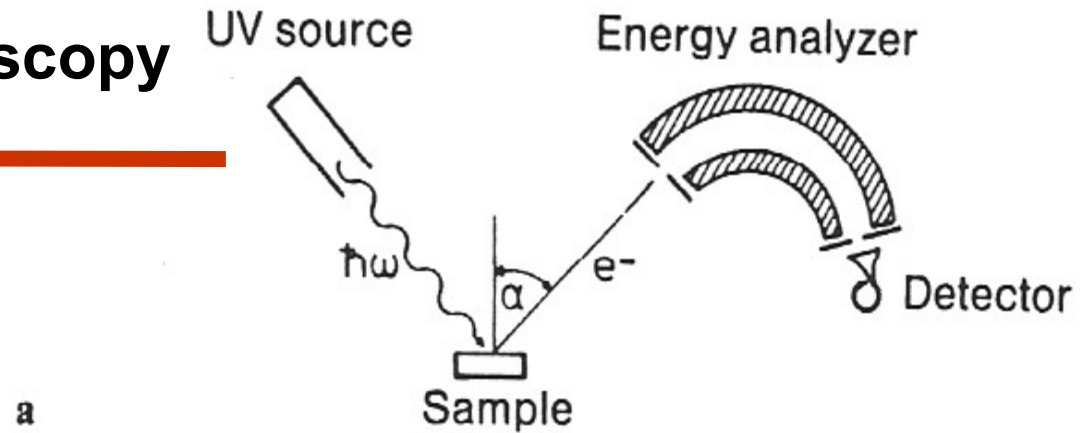
# Transition metals



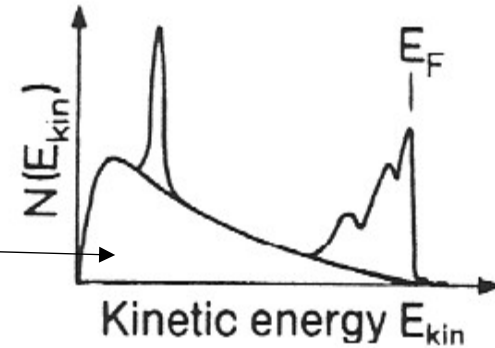
# Photoemission spectroscopy

UPS - Ultraviolet  
photoemission spectroscopy

Measure the density of states  
with photoemission  
spectroscopy



Secondary  
electrons



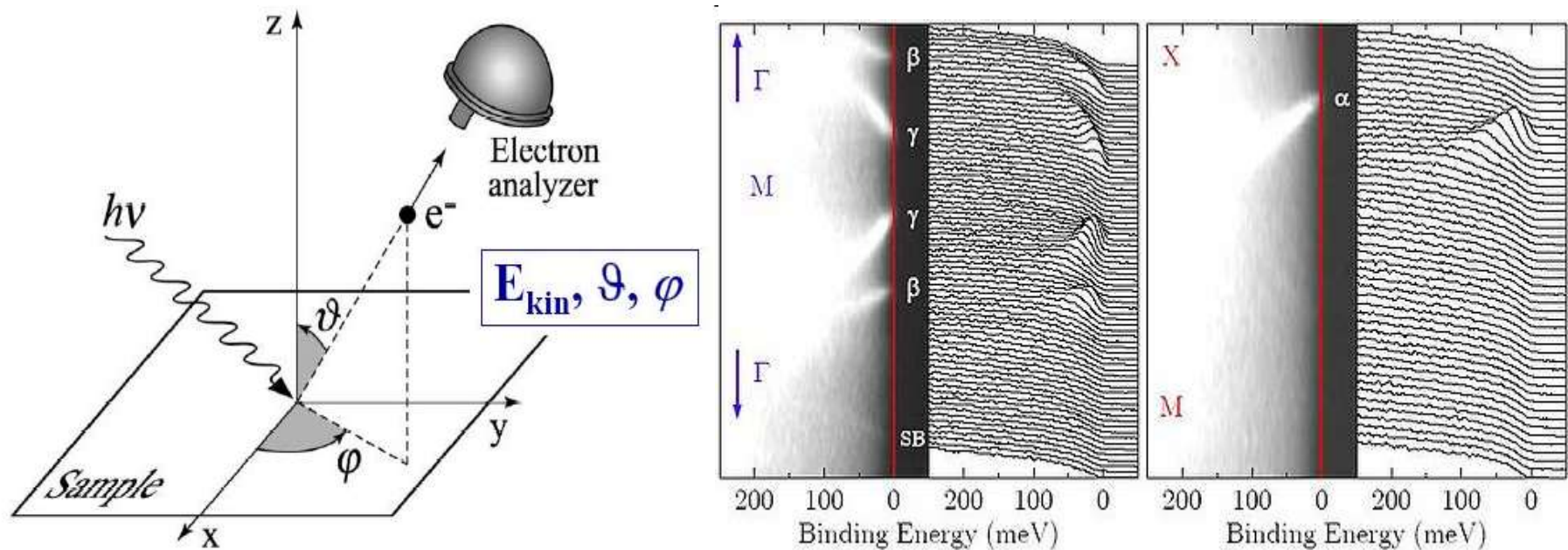
Binding energy

From: Ibach & Lueth

b

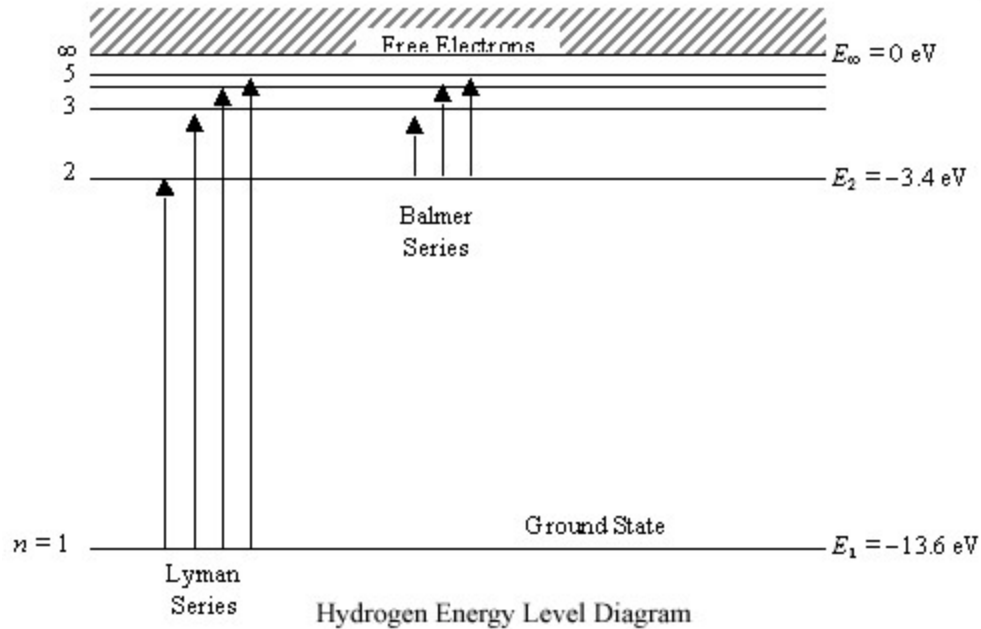
# Angle resolved photoemission spectroscopy (ARPES)

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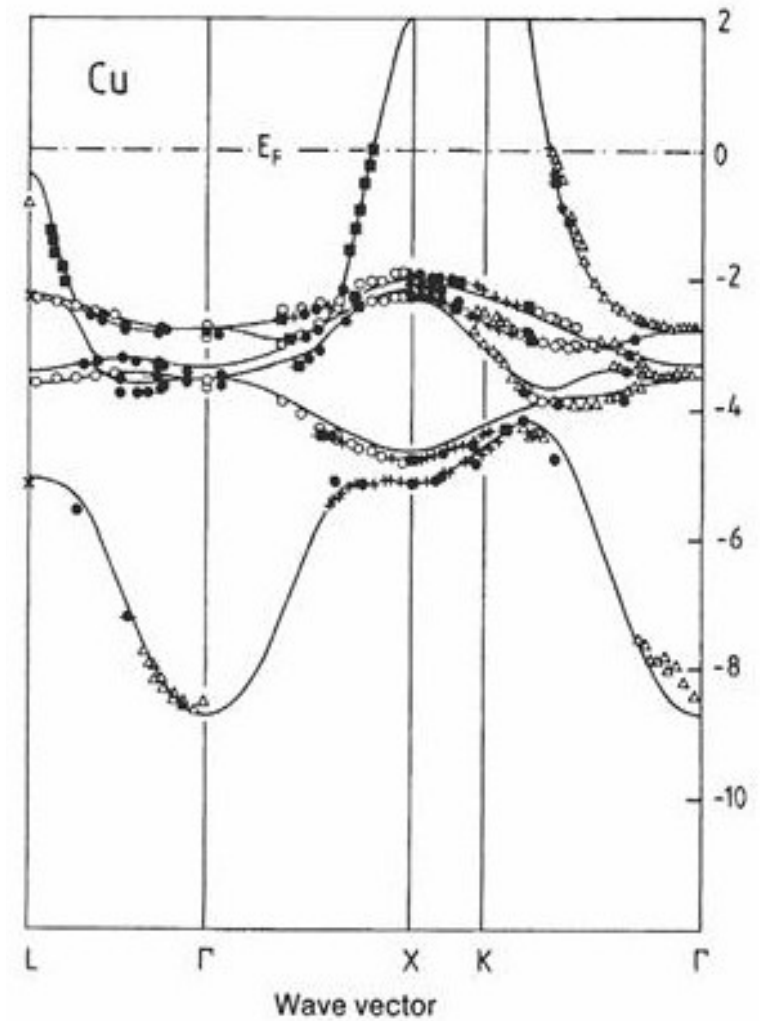
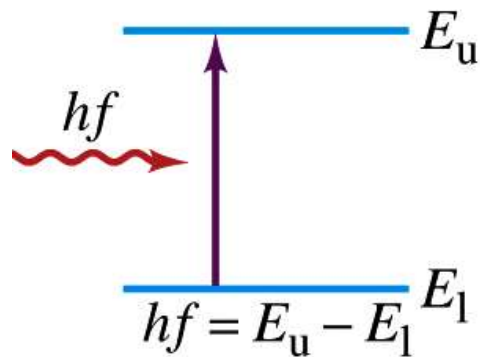


Measure the dispersion relation with angle resolved photoemission

# Optical absorption



Hydrogen atom

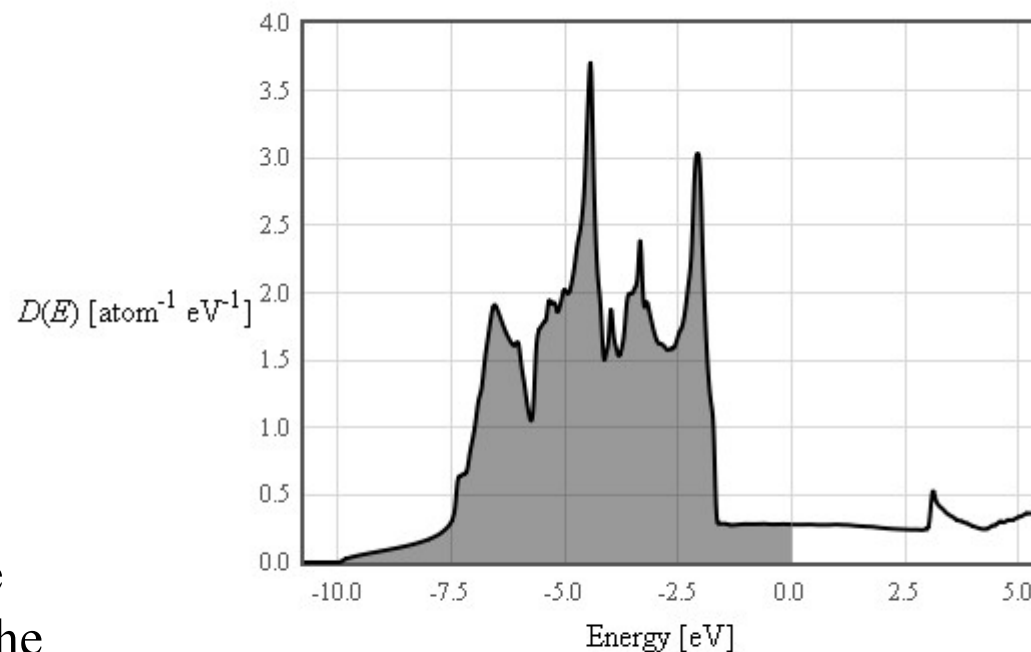


Copper fcc crystal

# Thermodynamic properties of metals

From the band structure measurements, we obtain the electron density of states.

Electron density of states for fcc gold



Thermodynamic properties can be calculated from the tabulated data for the density of states

$E$ [eV]	$D(E)$ [ $\text{atom}^{-1} \text{eV}^{-1}$ ]
-10.74913	0
-10.73552	0
-10.72192	0



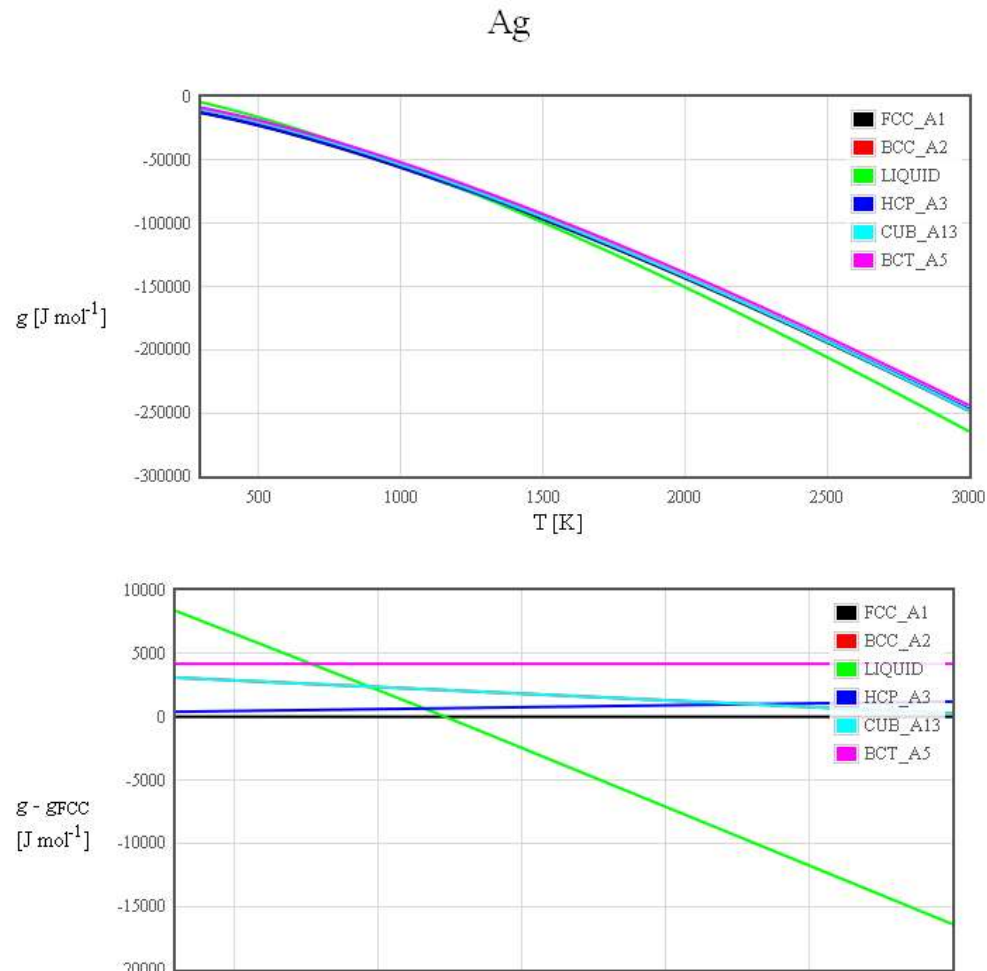
# SGTE data for pure elements

## SGTE thermodynamic data

The [Scientific Group Thermodata Europe SGTE](http://www.sciencedirect.com/science/article/pii/036459169190030N) maintains [thermodynamic databanks for inorganic and metallurgical systems](http://www.sciencedirect.com/science/article/pii/036459169190030N). Data from their 'pure element database' is plotted below.

Typically, experiments are performed at constant pressure  $p$ , temperature  $T$ , and number  $N$ . Under these conditions, the system will go to the minimum of the Gibbs energy  $G = U + pV - TS$ . Here  $U$  is the internal energy,  $V$  is the volume, and  $S$  is the entropy. The top plot is the Gibbs energy per mole  $g = u + p\nu - Ts$ , where  $u$  is the internal energy per mole,  $\nu$  is the volume per mole, and  $s$  is the entropy per mole.

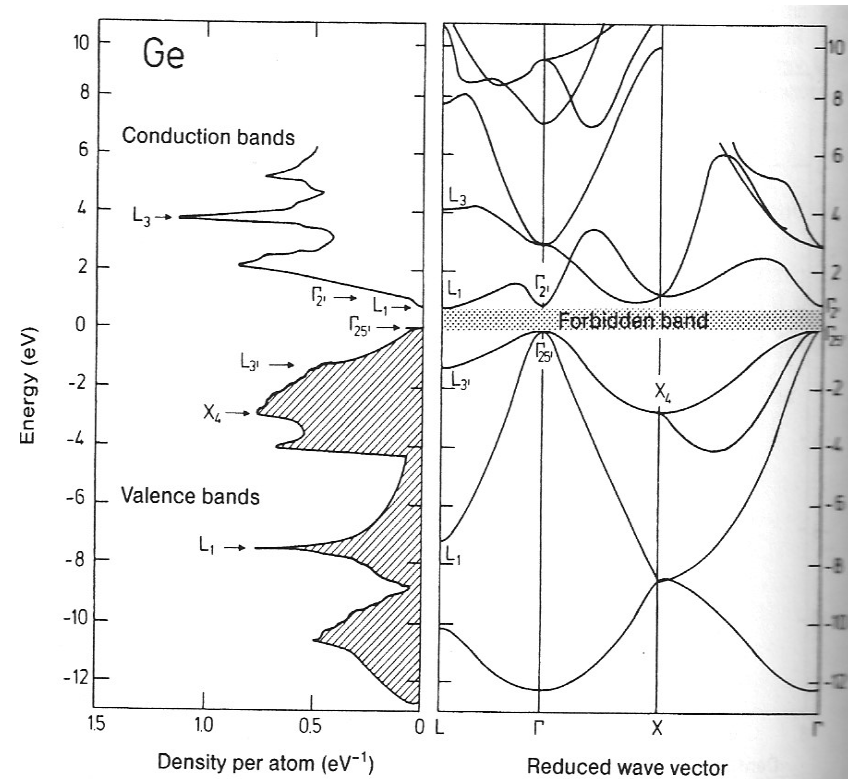
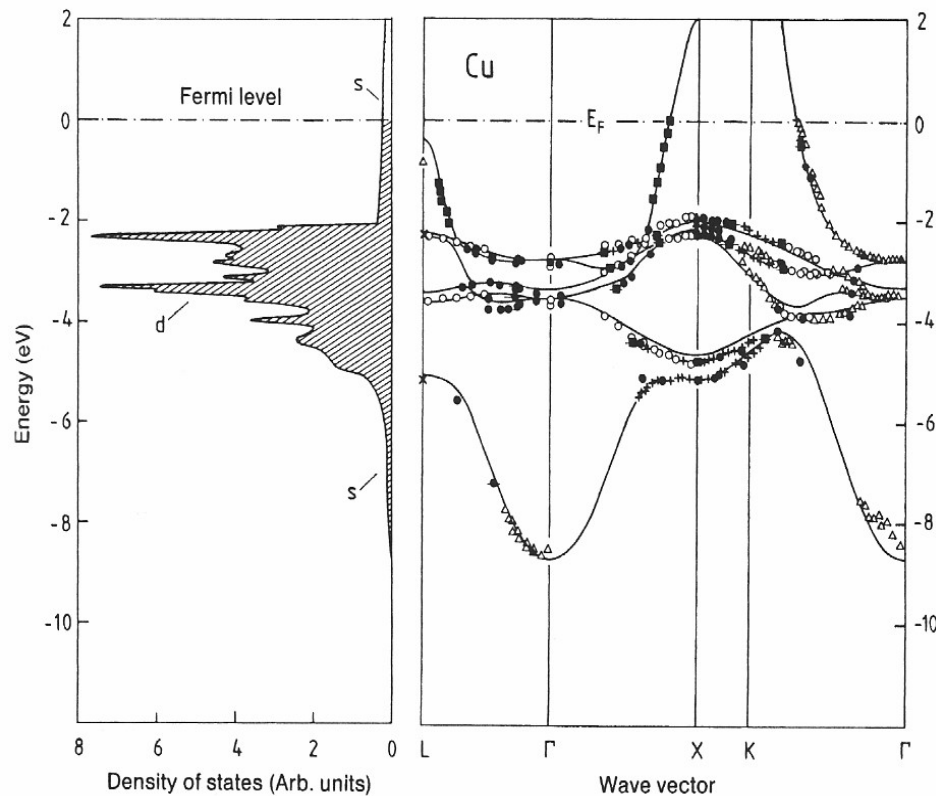
Ag	Al	Am	As
Au	B	Ba	Be
Bi	C	Ca	Cd
Ce	Co	Cr	Cs
Cu	Dy	Er	Eu
Fe	Ga	Gd	Ge
Hf	Hg	Ho	In
Ir	K	La	Li
Lu	Mg	Mn	Mo
N	Na	Nb	Nd
Ni	Np	O	Os
P	Pa	Pb	Pd
Pr	Pt	Pu	Rb
Re	Rh	Ru	S
Sb	Sc	Se	Si
Sm	Sn	Sr	Ta
Tb	Tc	Te	Th
Ti	Tl	Tm	U
V	W	Y	Yb
Zn	Zr		



<http://www.sciencedirect.com/science/article/pii/036459169190030N>

<http://www.sciencedirect.com/science/article/pii/036459169190030N>

# Metals, semiconductors, and insulators



Insulators: band gap  $> 3$  eV

From Ibach & Lueth

# Student Projects

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Plot the dispersion relation for a 1-D square wave potential  
Using the Kronig-Penney model, the plane wave method, and tight binding.

Draw the missing Fermi surfaces

Use the tight-binding model to calculate a dispersion relation.

Expand the table of tight binding solutions and  
plane wave method solutions

# kinetic theory

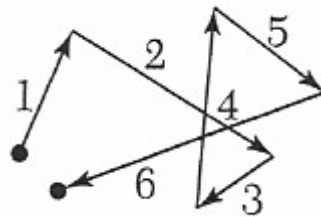
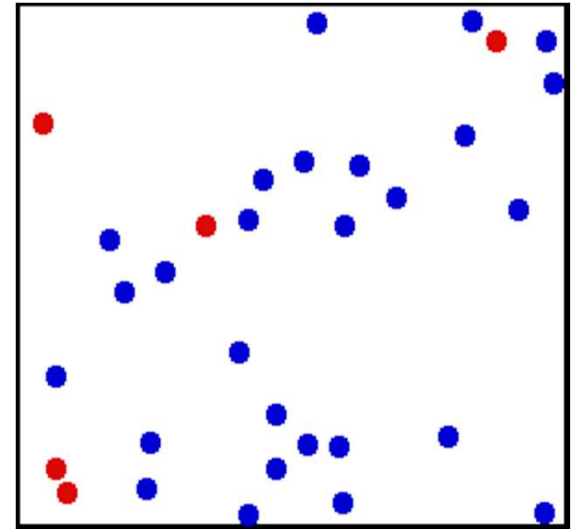
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describe electrons as a gas of particles

$$v_F = 10^8 \text{ cm/s.}$$

The average time between scattering events  $\tau_{sc}$  can be calculated by Fermi's golden rule

mean free path:  $l = v_F \tau_{sc} \sim 1 \text{ nm} - 1 \text{ cm}$



# Diffusion equation/ heat equation

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Diffusion constant  $\frac{dn}{dt} = -D\nabla^2 n$

Fick's law  $\vec{j} = -D\nabla n$

Continuity equation  $\frac{dn}{dt} = \nabla \cdot \vec{j}$



$$n = \frac{1}{\sqrt{4\pi Dt}} \exp\left(\frac{-r^2}{4Dt}\right)$$

# Ballistic transport

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$$\vec{F} = m\vec{a} = -e\vec{E} = m \frac{d\vec{v}}{dt}$$

$$\vec{v} = \frac{-e\vec{E}t}{m} + \vec{v}_0$$

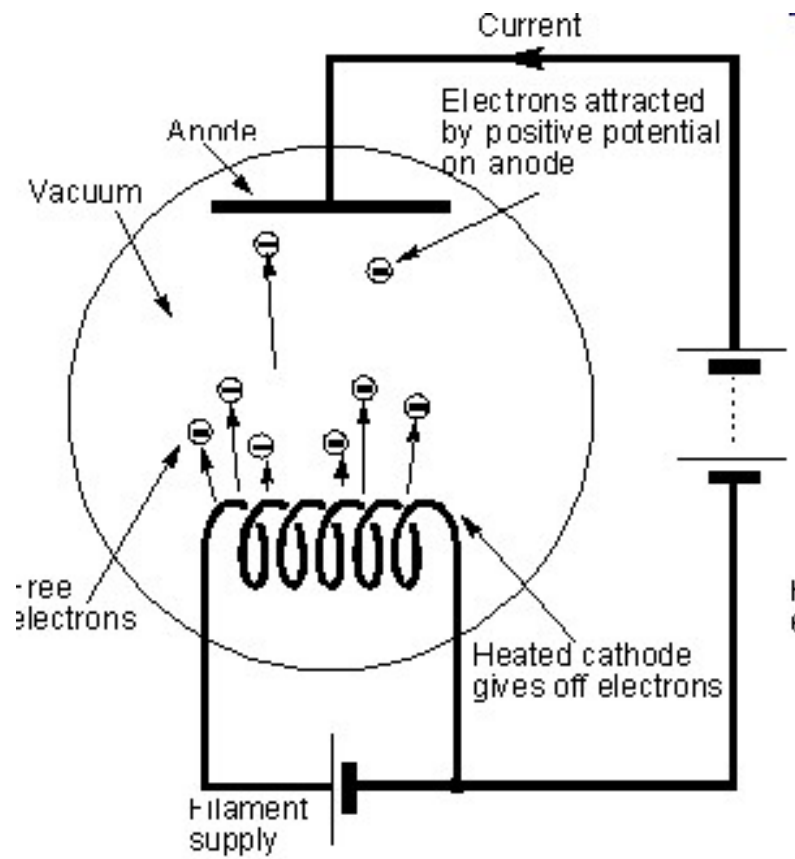
$$\vec{x} = \frac{-e\vec{E}t^2}{2m} + \vec{v}_0t + \vec{x}_0$$

electrons in an electric field follow a parabola.

electrons in a magnetic field move in a spiral

electrons crossed electric and magnetic fields spiral  
along the direction perpendicular to the electric and  
magnetic fields

# Vacuum diodes



diode





# Diffusive transport

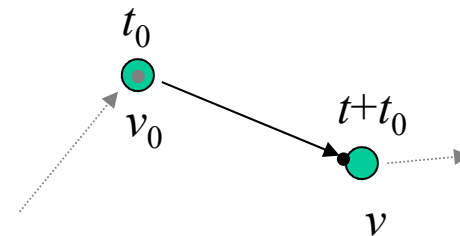
$$\vec{F} = -e\vec{E} = m^* \vec{a} = m^* \frac{d\vec{v}}{dt}$$

$$\vec{v} = \vec{v}_0 - \frac{e\vec{E}}{m^*} (t - t_0)$$

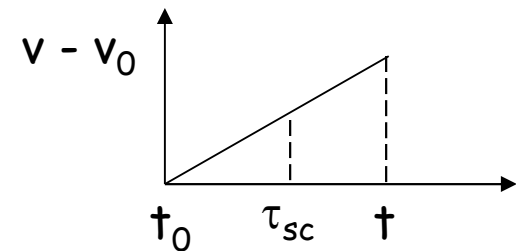
$$\langle v_0 \rangle = 0$$

$$\langle t - t_0 \rangle = \tau_{sc} < \text{average time between scattering events}$$

time between two collisions



$$\vec{v}_d = \frac{-e\vec{E}\tau_{sc}}{m^*} = \frac{-e\vec{E}\ell}{m^* v_F}$$



drift velocity:  $\vec{v}_d = -\mu\vec{E}$

Ohm's law:  $\vec{j} = -ne\vec{v}_d = ne\mu\vec{E} = \sigma\vec{E}$