

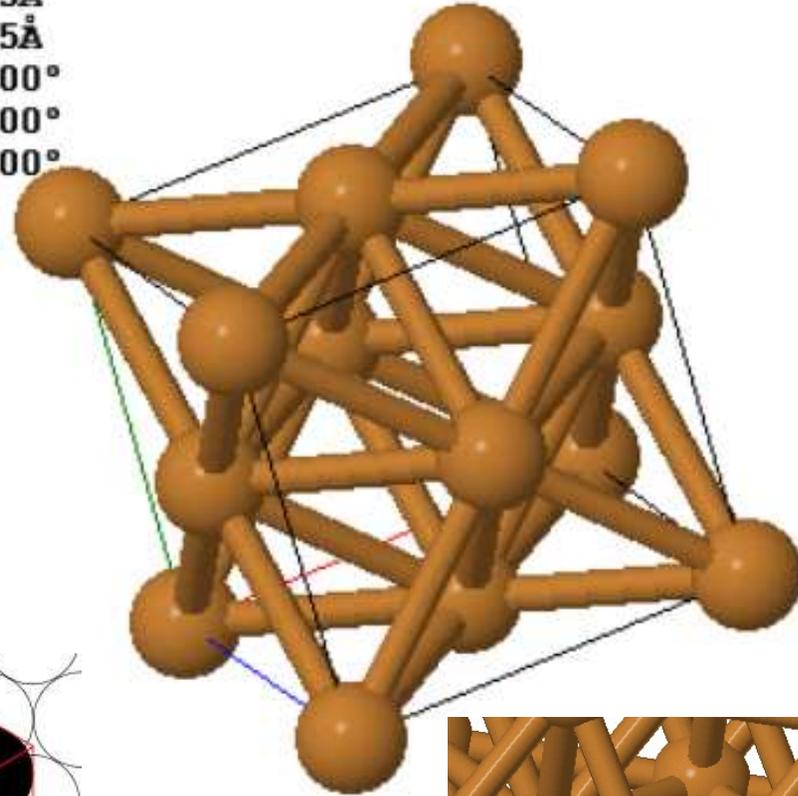
Crystal structure

fcc

Number 225

Al, Cu,
Ni, Sr,
Rh, Pd,
Ag, Ce,
Tb, Ir,
Pt, Au,
Pb, Th

HM: $F m \bar{3} m$
 $a=3.615\text{\AA}$
 $b=3.615\text{\AA}$
 $c=3.615\text{\AA}$
 $\alpha=90.000^\circ$
 $\beta=90.000^\circ$
 $\gamma=90.000^\circ$



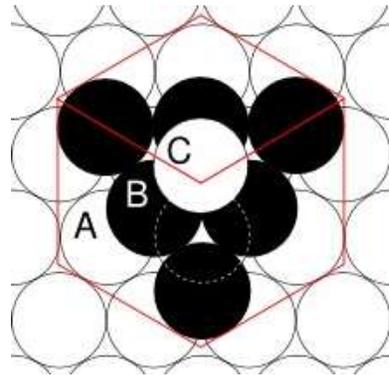
[111]

Primitive Vectors:

$$\vec{a}_1 = \frac{a}{2} \hat{y} + \frac{a}{2} \hat{z}$$

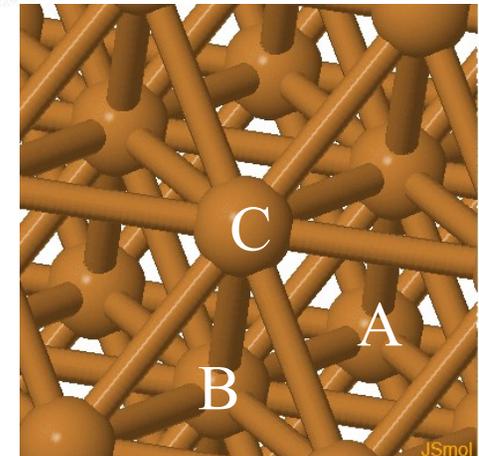
$$\vec{a}_2 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{z}$$

$$\vec{a}_3 = \frac{a}{2} \hat{x} + \frac{a}{2} \hat{y}$$

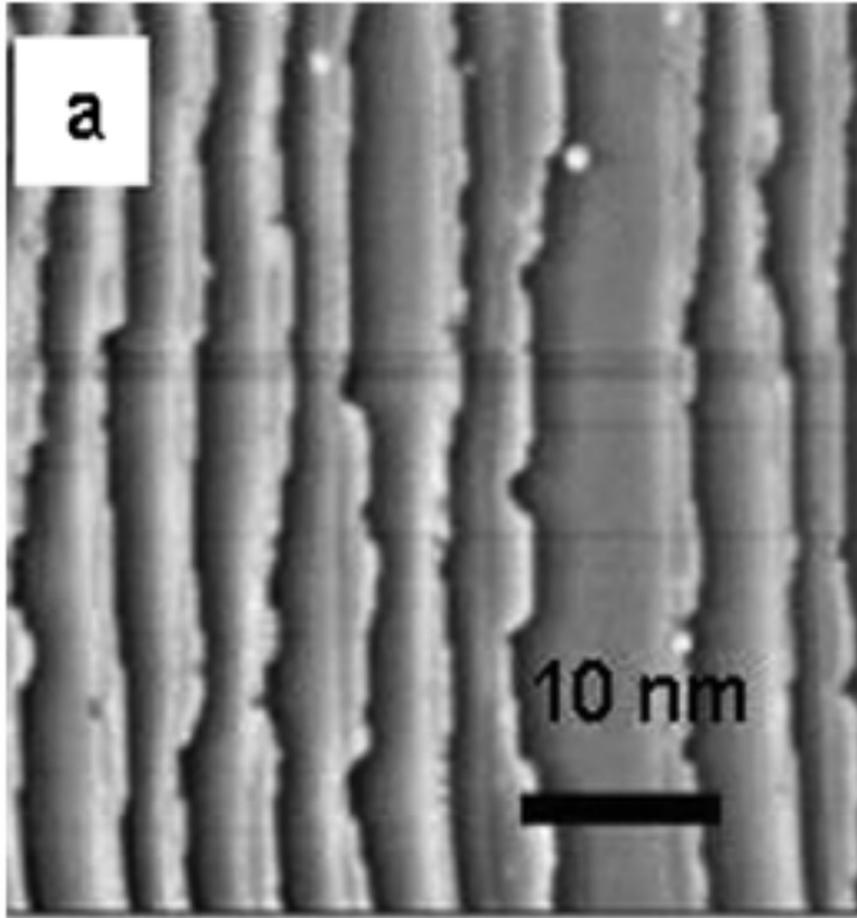


Basis Vector:

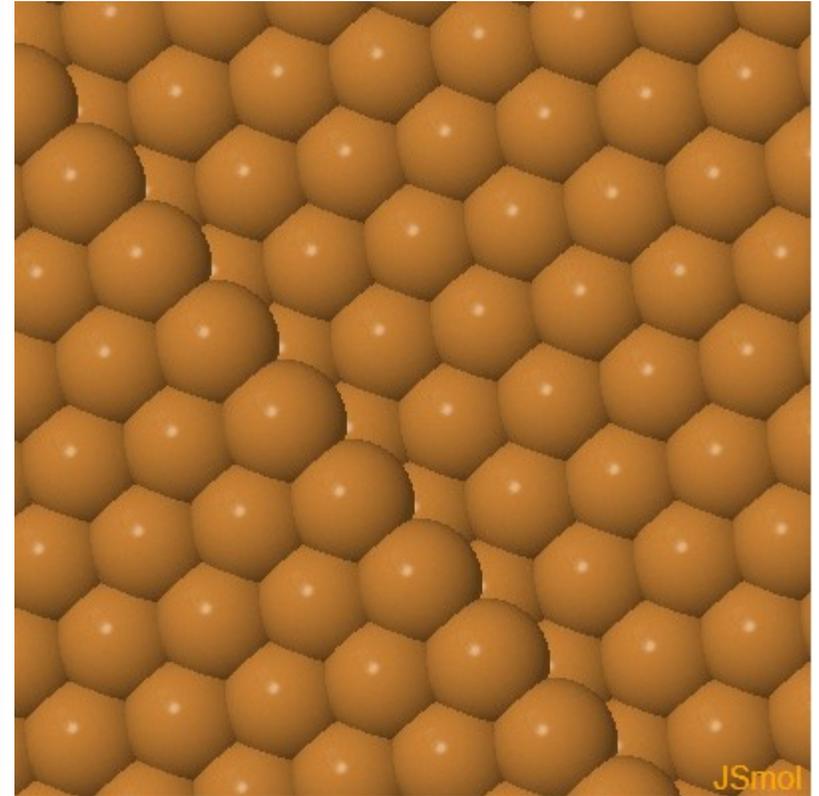
$$\vec{B}_1 = (0, 0, 0)$$



Crystal planes: Miller indices



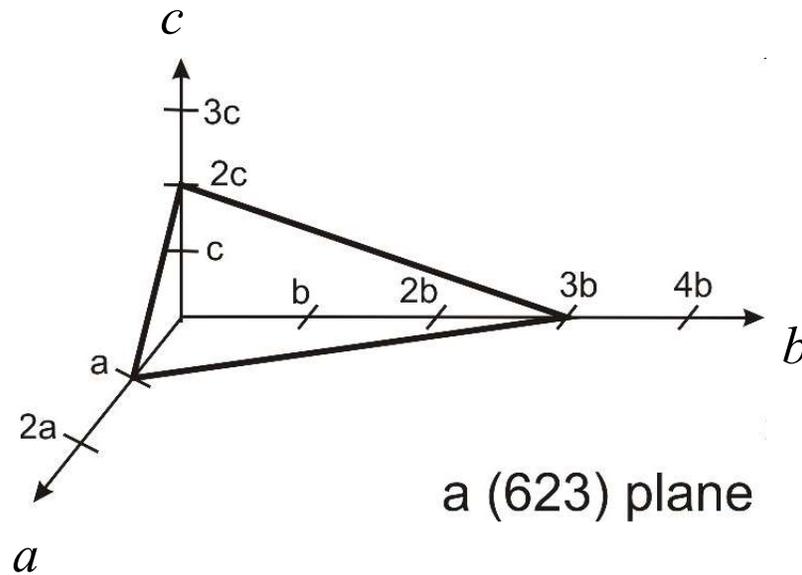
Rh(15,15,13) fcc



(15,15,13) fcc

Reaction studies on nanostructured surfaces, Adolf Winkler, in *The Oxford Handbook of Nanoscience and Technology*, A. V. Narlikar and Y. Y. Fu ed., 2009.

Miller indices: Crystal planes



() specific plane

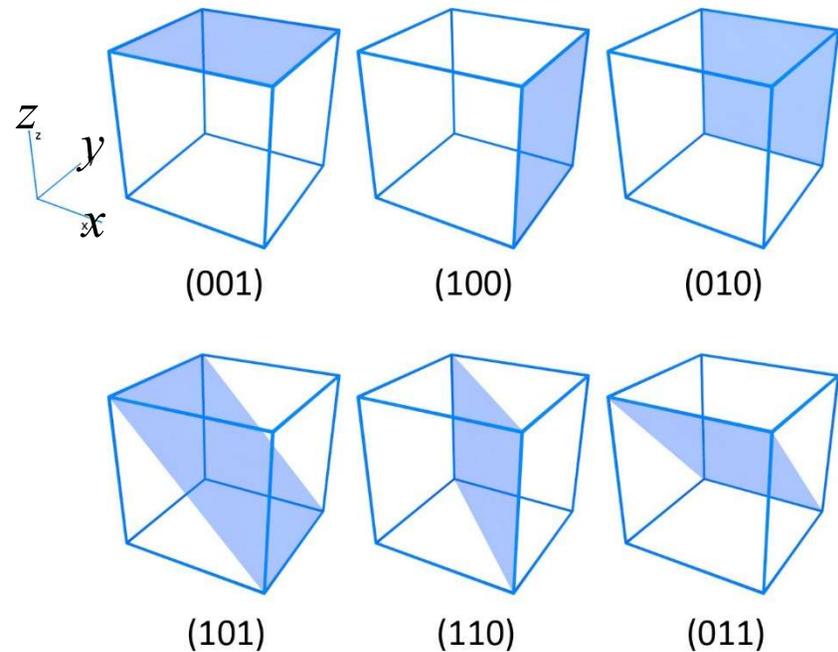
{ } family of equivalent planes



MOSFETs are made on {100} wafers

A plane with the intercepts $1/h, 1/k, 1/l$ is the (h, k, l) plane.

always use integers for h, k, l

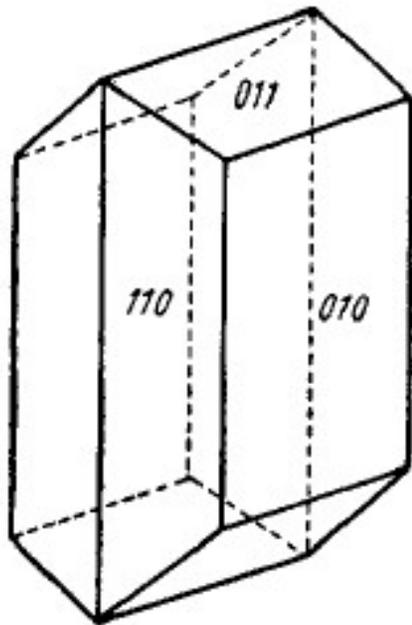


Crystals

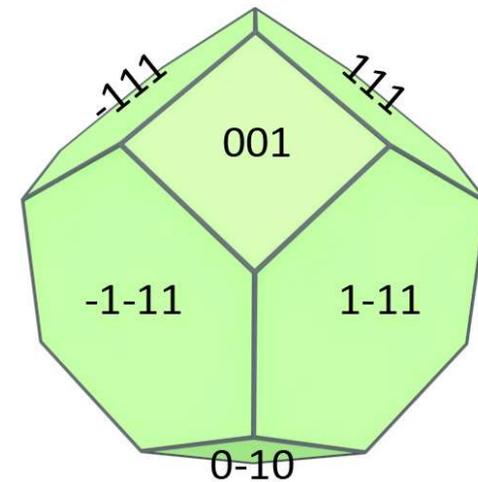
rule of rationality

R. J. Haüy (1743-1822):

the indices of external planes of crystals are generally simple full numbers



orthorhombic
Aragonit CaCO_3



one possible morphology
of a crystal with cubic structure

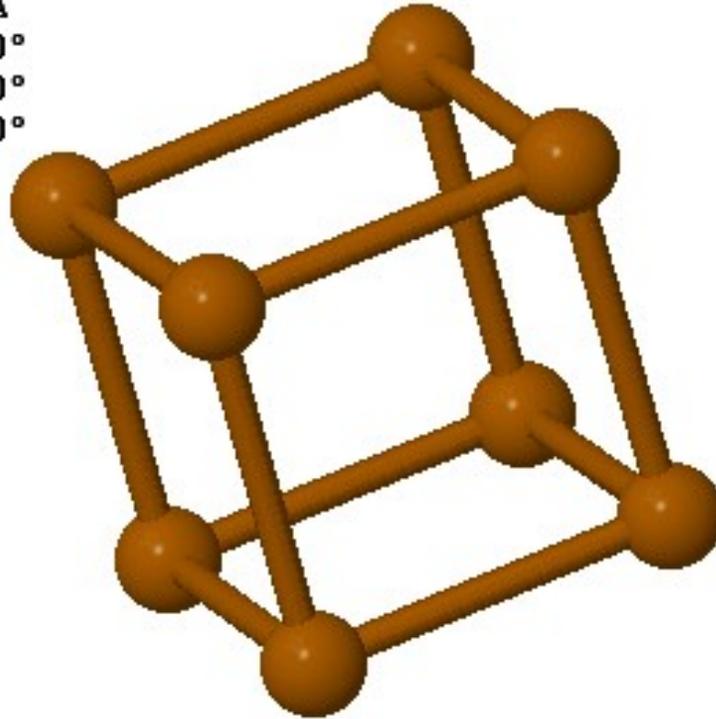
Bravais:

Planes with high atomic densities tend to dominate

simple cubic

Po

HM: P m $\bar{3}$ m
a=3.359Å
b=3.359Å
c=3.359Å
 $\alpha=90.000^\circ$
 $\beta=90.000^\circ$
 $\gamma=90.000^\circ$



Number: 221

Primitive Vectors:

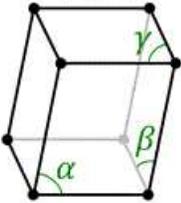
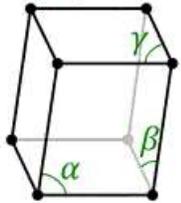
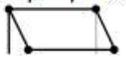
$$\vec{a}_1 = a\hat{x}$$

$$\vec{a}_2 = a\hat{y}$$

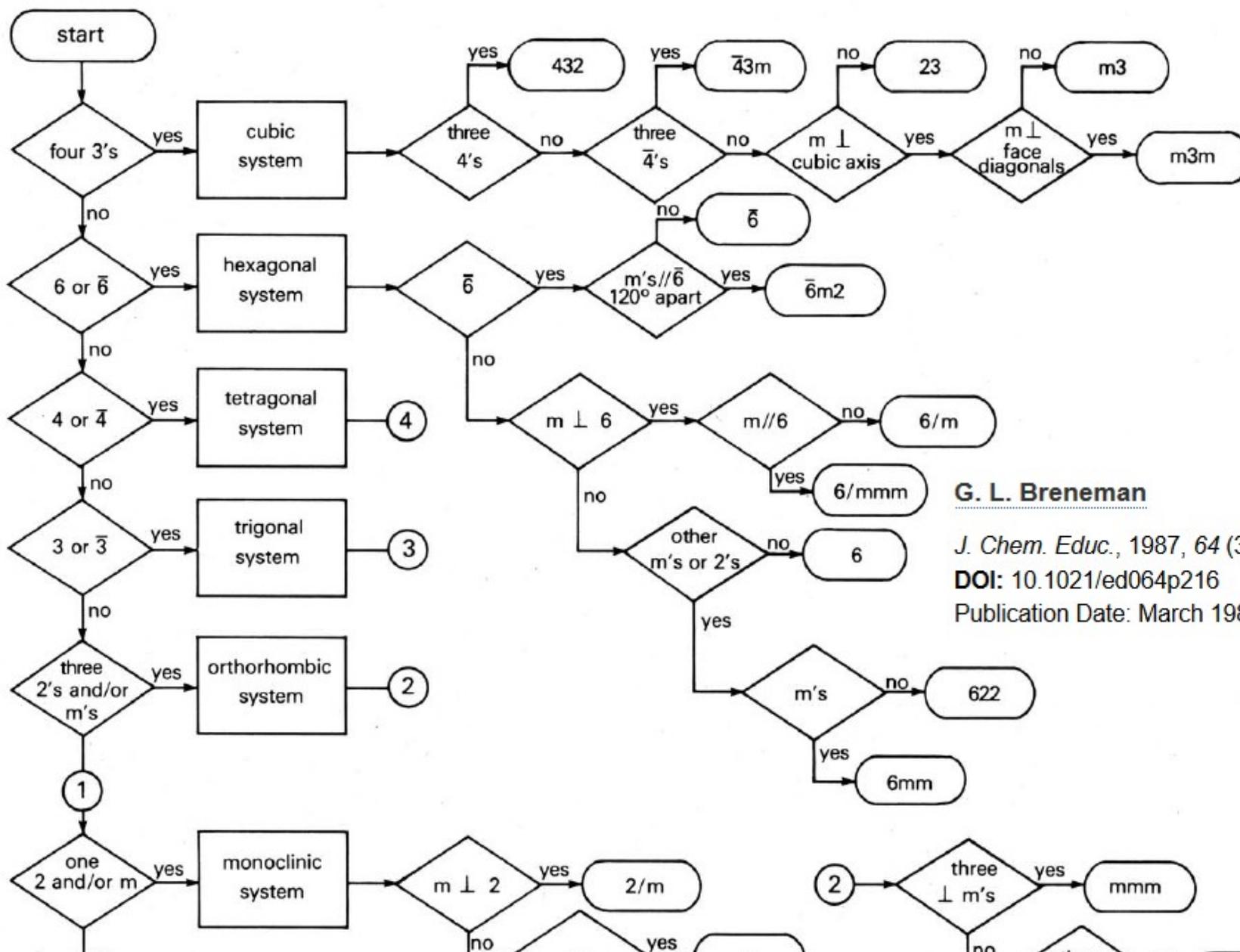
$$\vec{a}_3 = a\hat{z}$$

Basis Vector: $\vec{B}_1 = (0, 0, 0)$

The 32 Crystal Classes

Crystal system	Crystal Class	International symbol	Schoenflies symbol	Space groups	2-fold axes	3-fold axes	4-fold axes	6-fold axes	mirror planes	inversion	Examples	Number of symmetry elements
Triclinic $a \neq b \neq c$ $\alpha \neq \beta \neq \gamma$ 	triclinic-pedial	1	C_1	1: P1	-	-	-	-	-	n		1
	triclinic-pinacoidal	$\bar{1}$	$S_2 = C_i$	2: $P\bar{1}$	-	-	-	-	-	y		2
Monoclinic $a \neq b \neq c$ $\alpha \neq 90^\circ$, $\beta = \gamma = 90^\circ$ 	monoclinic-sphenoidal	2	C_2	3: P2, 4: $P2_1$, 5: C2	1	-	-	-	-	n		2
	monoclinic-domatic	m	$C_{1h} = C_s$	6: Pm, 7: Pc, 8: Cm, 9: Cc	-	-	-	-	1	n		2
	monoclinic-prismatic	$2/m$	C_{2h}	10: P2/m, 11: $P2_1/m$, 12: C2/m, 13: P2/c, 14: $P2_1/c$, 15: C2/c	1	-	-	-	1	y		4
Orthorhombic $a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$ 	orthorhombic-disphenoidal	222	$V = D_2$	16: P222, 17: $P222_1$, 18: $P2_12_12_1$, 19: $P2_12_12_1$, 20: $C222_1$, 21: C222, 22: F222, 23: I222, 24: $I2_12_12_1$	3	-	-	-	-	n		4

Crystallographic symmetry point group notation flow chart



G. L. Breneman

J. Chem. Educ., 1987, 64 (3), p 216

DOI: 10.1021/ed064p216

Publication Date: March 1987

International Tables for Crystallography Volume A: Space-group symmetry

First online edition (2006) ISBN: 978-0-7923-6590-7 eISBN: 978-1-4020-5406-8 doi: 10.1107/97809553602060000100

Edited by Th. Hahn



- | [contents](#) | [indexes](#) |
- | [contributors](#) | [editors](#) |
- | [sample pages](#) | [purchase](#) |
- | [explanation of the space-group data](#) |

Go to No.

- 1 (P1)
- 2 (P-1)
- 3 (P2)
- 4 (P21)
- 5 (C2)
- 6 (Pm)
- 7 (Pc)
- 8 (Cm)
- 9 (Cc)
- 10 (P2/m)
- 11 (P21/m)
- 12 (C2/m)
- 13 (P2/c)
- 14 (P21/c)
- 15 (C2/c)
- 16 (P222)
- 17 (P2221)
- 18 (P21212)
- 19 (P212121)
- 20 (C2221)

Volume A treats crystallographic symmetry in direct or physical space. It contains extensive tables of the 17 plane groups, the 230 space groups and the 32 crystallographic point groups.

The first five parts of the volume contain introductory material: lists of symbols and terms; symbols; and unit-cell (coordinate) transformations. These are followed by the plane-group tables; the determination of space groups; synoptic tables of space-groups (Parts 6 and 7). For each group type, the following information is presented:

- headline with the relevant group symbols;
- diagrams of the symmetry elements and of the general position;
- specification of the origin and the asymmetric unit;
- list of symmetry operations;
- generators;
- general and special positions with multiplicities, site symmetries, coordinates and reflections;
- symmetries of special projections;
- extensive subgroup and supergroup data.

Parts 8 to 15 deal with the following aspects of symmetry theory: the mathematical approach to space groups; crystal lattices; point groups and crystal classes; symbols for symmetry operations; symbols for space groups; isomorphic subgroups of space groups; lattice complexes; and normalizers of space groups.

Sodalite

From Wikipedia, the free encyclopedia

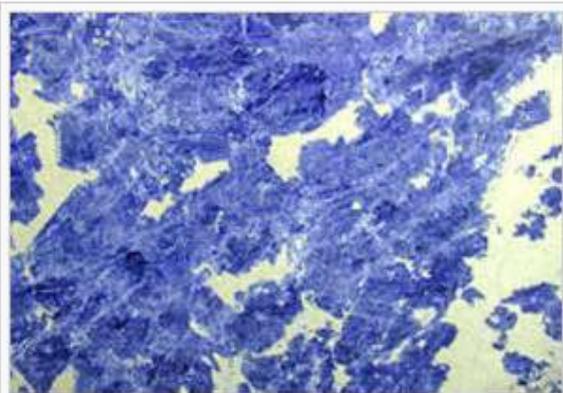
Sodalite is a rich royal blue mineral widely enjoyed as an [ornamental gemstone](#). Although massive sodalite samples are opaque, crystals are usually transparent to translucent. Sodalite is a member of the sodalite group with [hauyne](#), [nosean](#), [lazurite](#) and [tugtupite](#).

Discovered in 1811 in the [Ilmaussaq intrusive complex](#) in [Greenland](#), sodalite did not become important as an ornamental stone until 1891 when vast deposits of fine material were discovered in [Ontario, Canada](#).

Contents [hide]

- 1 Properties
- 2 Hackmanite
- 3 Occurrence
- 4 References

Properties [edit]



A sample of **sodalite-carbonate nephrite** from [Bolivia](#), with a polished rock.

A light, relatively hard yet fragile mineral, sodalite is named after its [sodium](#) content; in [mineralogy](#) it may be classed as a [feldspathoid](#). Well known for its blue color, sodalite may also be grey, yellow, green, or pink and is often mottled with white veins or patches. The more uniformly blue material is used in [jewellery](#), where it is fashioned into [cabochons](#) and [beads](#). Lesser material is more often seen as facing or inlay in

Sodalite



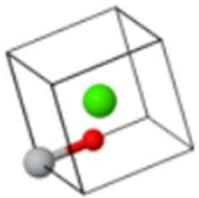
A sample of sodalite

General

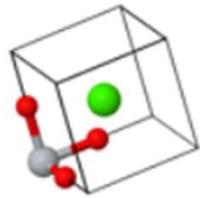
Category	Tectosilicates without zeolitic H ₂ O
Formula (repeating unit)	Na ₈ (Al ₆ Si ₆ O ₂₄)Cl ₂
Strunz classification	09.FB.10
Crystal symmetry	Isometric hextetrahedral H-M symbol: $\bar{4}3m$ Space group: $P\bar{4}3n$ 218
Unit cell	$a = 8.876(6) \text{ \AA}$; $Z = 1$

Identification

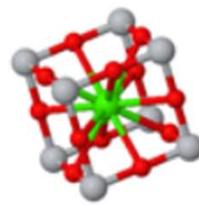
Asymmetric unit



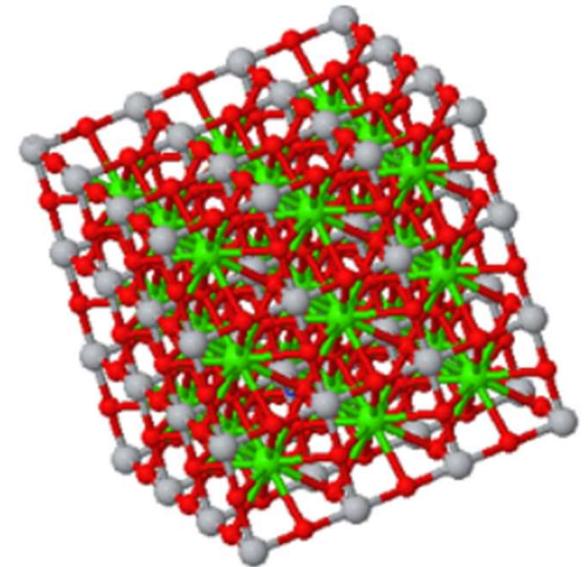
Asymmetric unit



Primitive unit cell



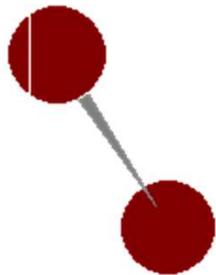
Conventional unit cell



Crystal

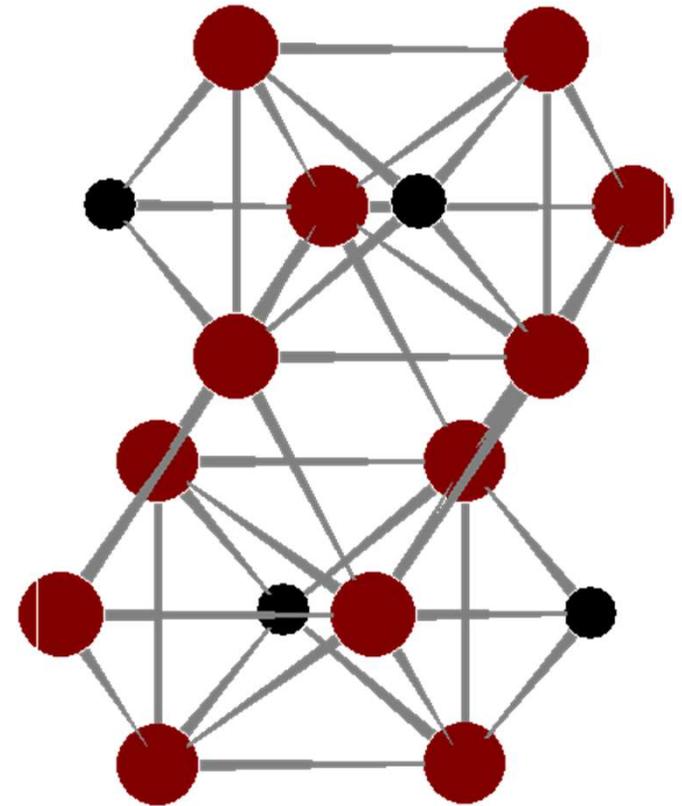
Asymmetric unit

```
cell 5.09000 6.74800 4.52300 90.000 90.000 90.000
natom 3
Fe1 26 0.18600 0.06300 0.32800
Fe2 26 0.03600 0.25000 0.85200
C 6 0.89000 0.25000 0.45000
rgnr 62
Cohenite (Cementite) Fe3 C
```



Asymmetric unit

Unit cell

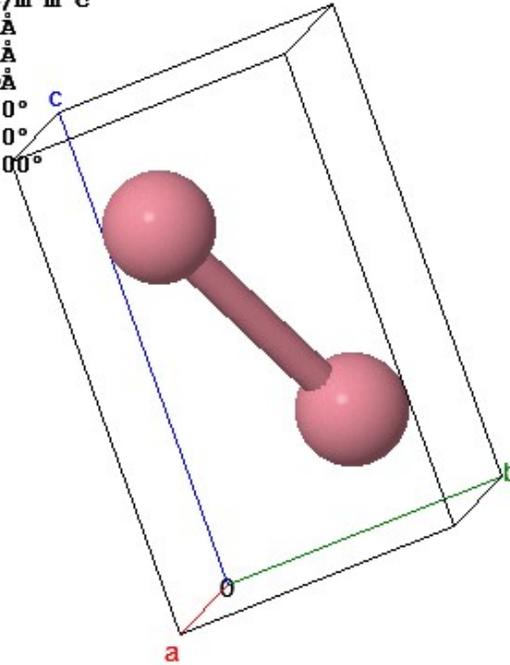


hcp

Space group 194 Crystallographic unit cell

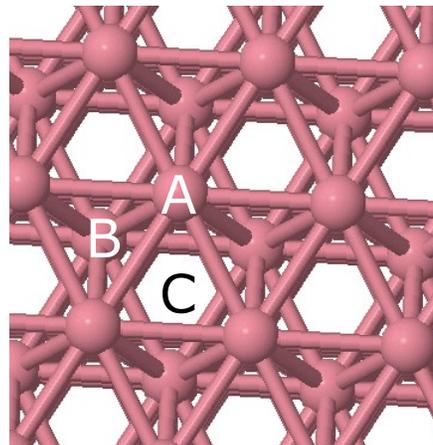
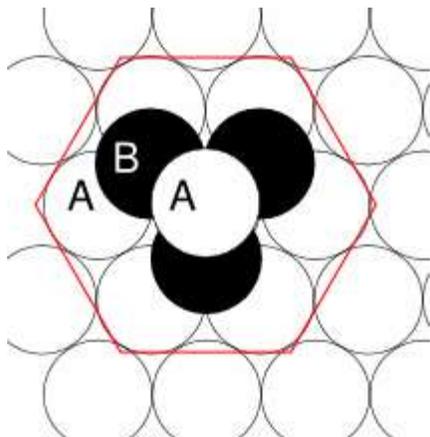
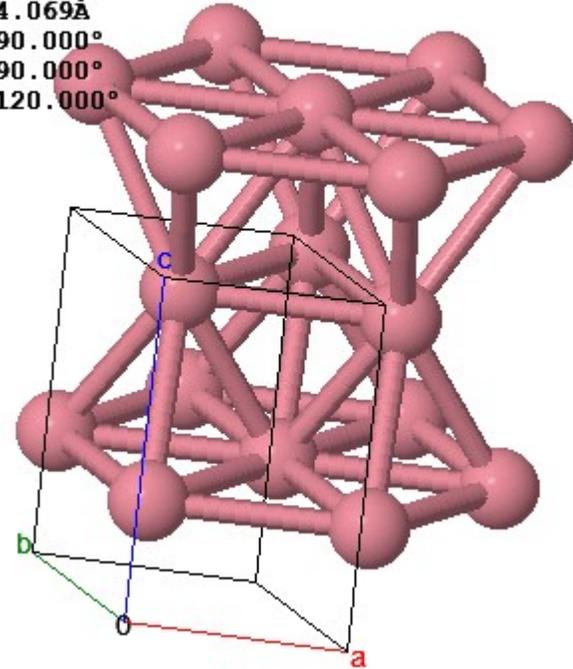
Mg, Be,
Sc, Ti,
Co, Zn,
Y, Zr, Tc,
Ru, Cd,
Gd, Tb,
Dy, Ho,
Er, Tm,
Lu, Hf,
Re, Os,
Tl

HM: P 63/m m c
a=2.507Å
b=2.507Å
c=4.069Å
α=90.000°
β=90.000°
γ=120.000°



Hexagonal unit cell

HM: P 63/m m c
a=2.507Å
b=2.507Å
c=4.069Å
α=90.000°
β=90.000°
γ=120.000°



Hexagonal Bravais lattice
Basis vectors:

$$\vec{B}_1 = (0, 0, 0) \quad \vec{B}_2 = \left(\frac{2}{3}, \frac{1}{3}, \frac{1}{2}\right)$$

bcc

W Number 229

Na

K

V

Cr

Fe

Rb

Nb

Mo

Cs

Ba

Eu

Ta

Primitive Vectors:

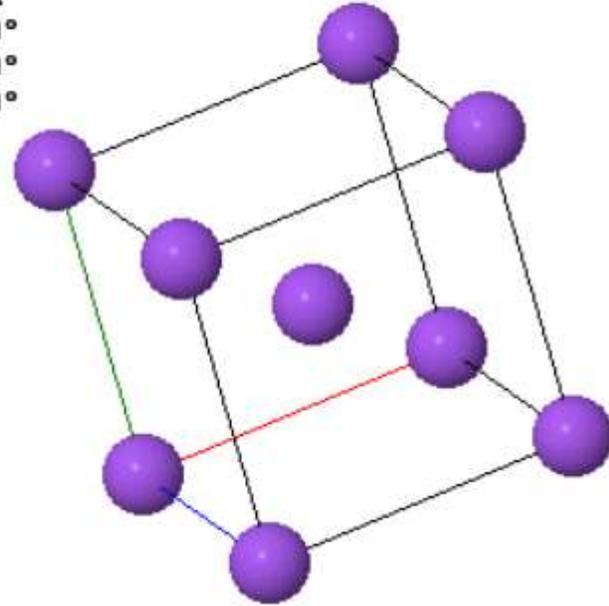
$$\vec{a}_1 = -\frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

$$\vec{a}_2 = \frac{a}{2}\hat{x} - \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}$$

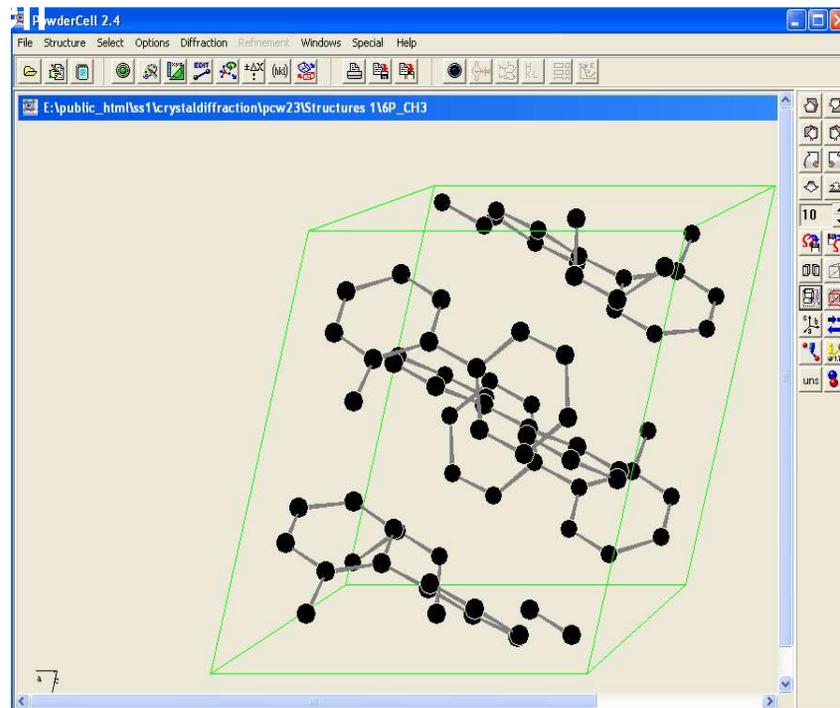
$$\vec{a}_3 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y} - \frac{a}{2}\hat{z}$$

Basis Vector: $\vec{B}_1 = (0, 0, 0)$

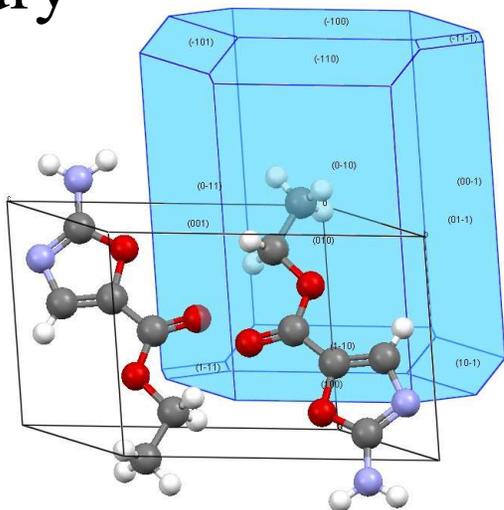
HM: IM-3M
a=4.291Å
b=4.291Å
c=4.291Å
α=90.000°
β=90.000°
γ=90.000°



PowderCell



Mercury

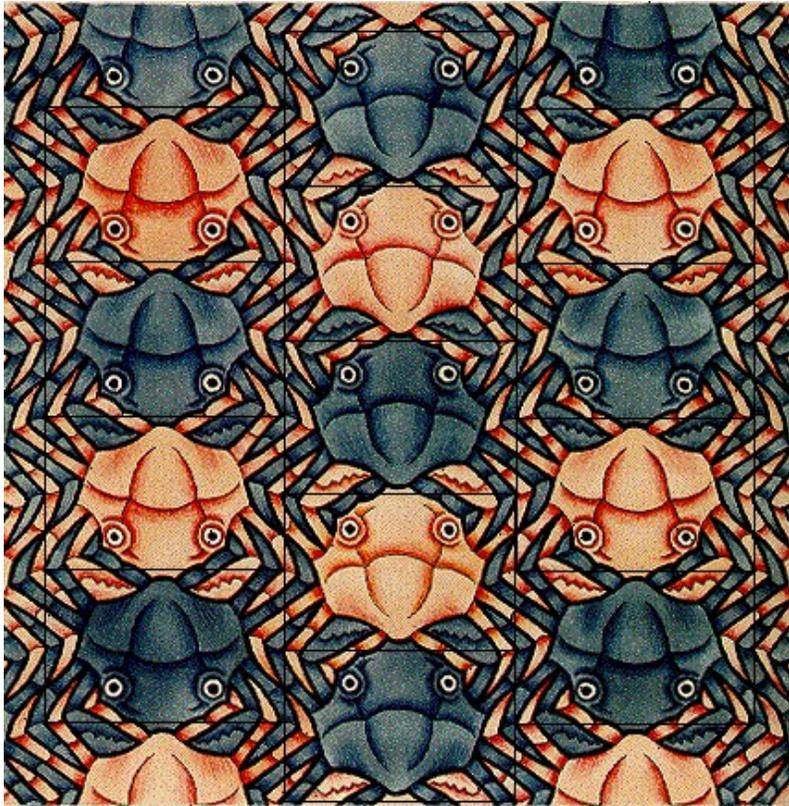


Standard data file: *.cif

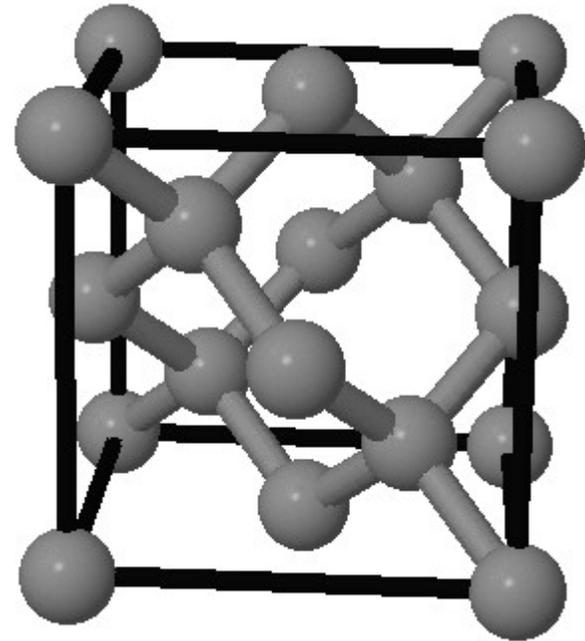
http://www.bam.de/de/service/publikationen/powder_cell.htm

<https://www.ccdc.cam.ac.uk/Community/csd-community/freemercury/>

Inequivalent atoms in the unit cell

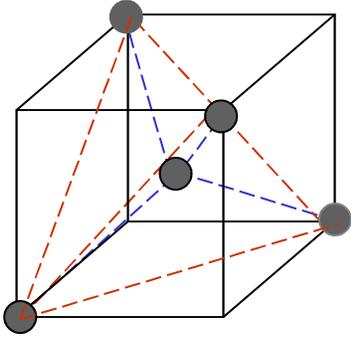


An element can have two distinct positions



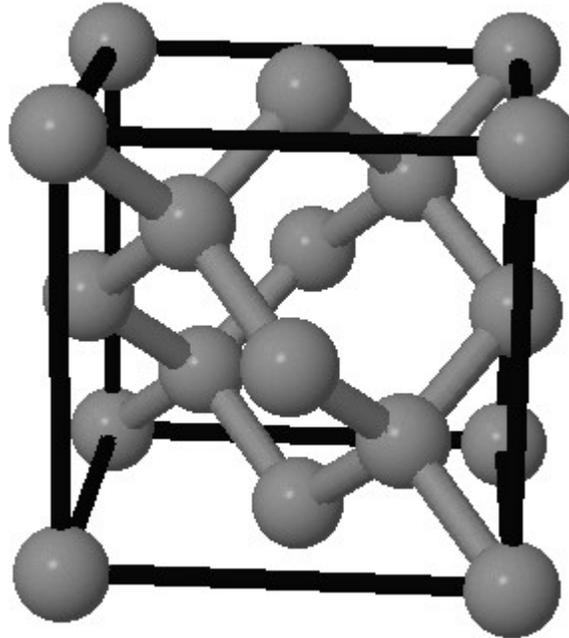
Diamond conventional unit cell

Diamond



$$a = b = c, \quad \alpha = 90^\circ, \beta = 90^\circ, \gamma = 90^\circ$$

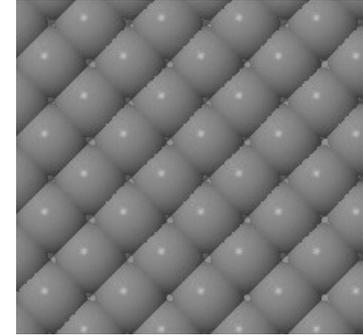
Space group: 227
point group: m3m



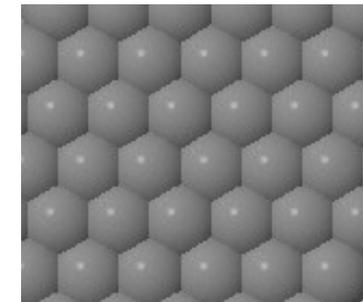
Primitive lattice vectors:

$$\vec{a}_1 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{y}, \quad \vec{a}_2 = \frac{a}{2}\hat{x} + \frac{a}{2}\hat{z}, \quad \vec{a}_3 = \frac{a}{2}\hat{y} + \frac{a}{2}\hat{z}.$$

Basis: $\vec{B}_1 = (0, 0, 0), \quad \vec{B}_2 = (0.25, 0.25, 0.25).$



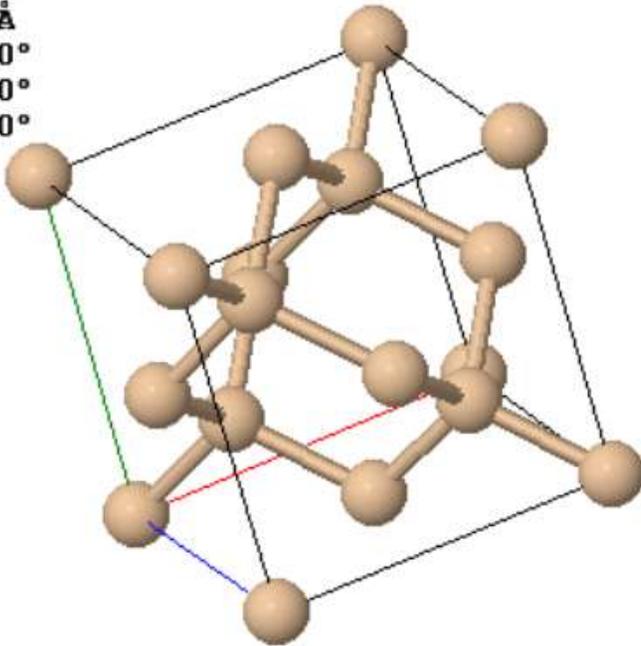
$$(100): \frac{2}{a^2}$$



$$(111): \frac{4}{\sqrt{3}a^2}$$

Silicon

HM:F d -3 m S
a=5.430Å
b=5.430Å
c=5.430Å
α=90.000°
β=90.000°
γ=90.000°



Conventional unit cell Primitive unit cell Asymmetric unit

2 x 2 x 2

3 x 3 x 3

5 x 5 x 5

Ball and Stick

Spacefill

H: 1

K: 0

L: 0

show HKL plane

hide HKL plane

draw atoms in HKL plane

Thickness of HKL planes:

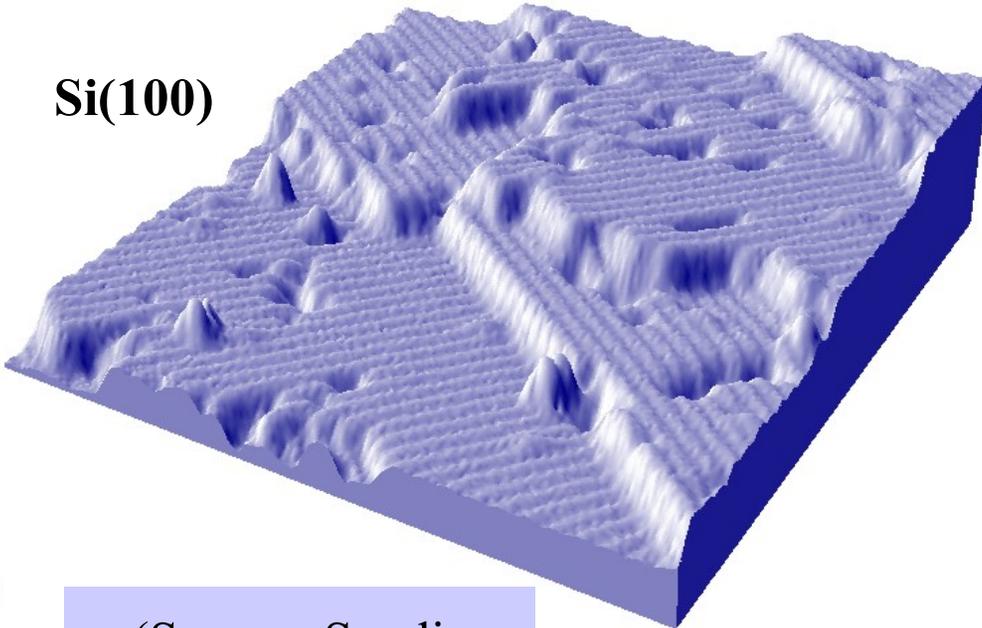


The conventional unit cell is a cube with sides of 0.543 nm. There are 8 atoms in the conventional unit cell. (The image can be rotated with a mouse.)

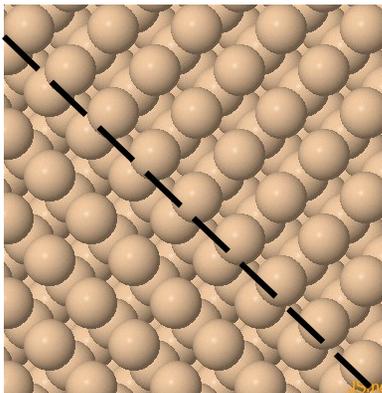
JSmol

Silicon surfaces

Si(100)



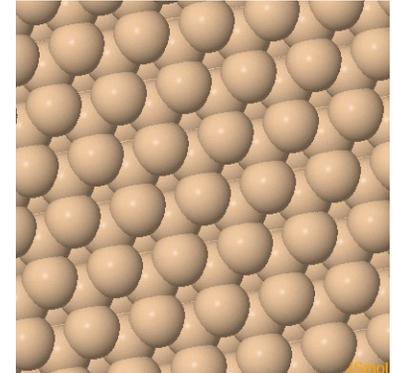
(Source: Sandia
Nat.Labs.)



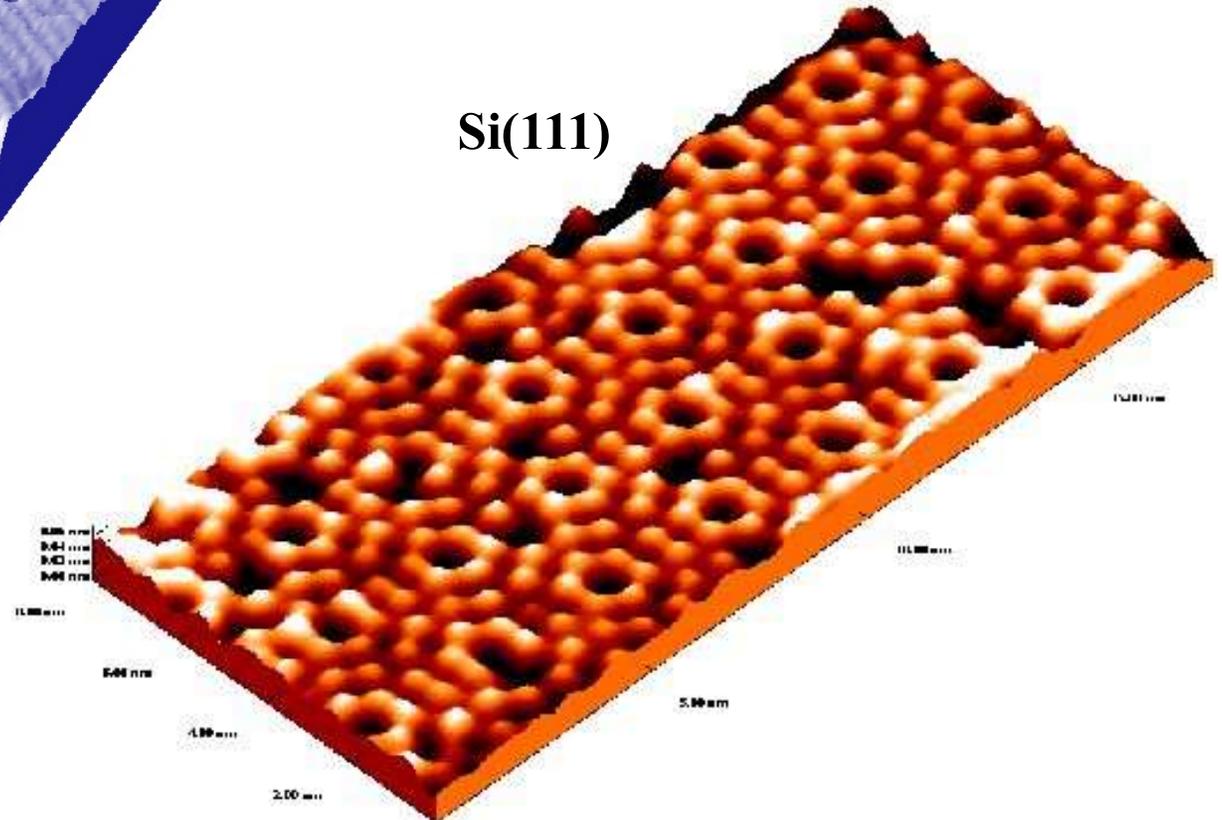
atomic
step in
Si(100)

unreconstructed

Si(111) →

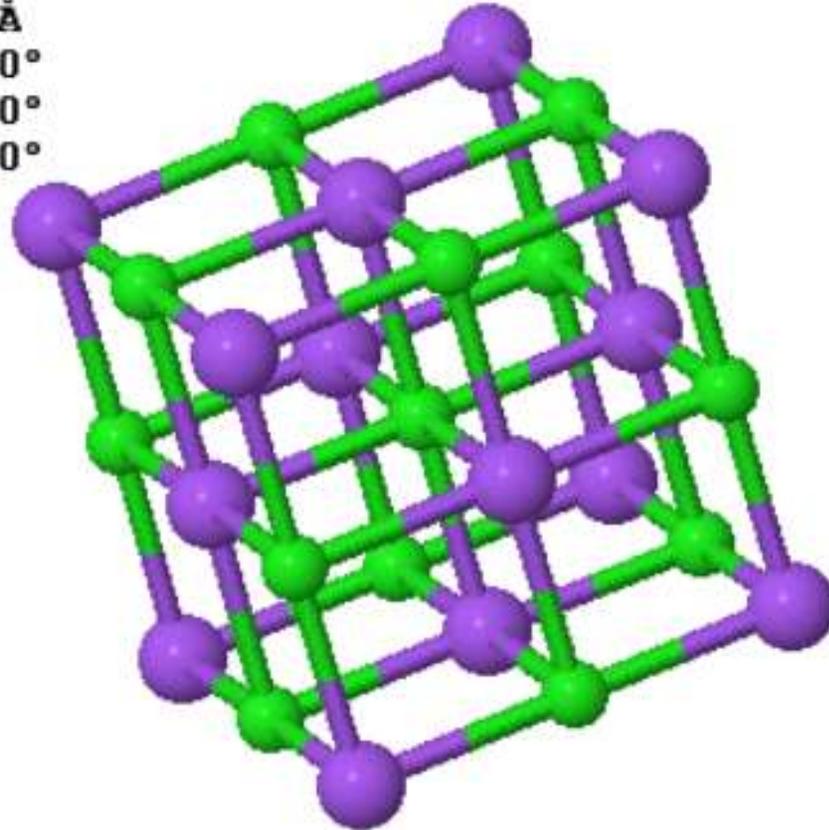


Si(111)



NaCl

HM: $F m \bar{3} m$
 $a=5.639\text{\AA}$
 $b=5.639\text{\AA}$
 $c=5.639\text{\AA}$
 $\alpha=90.000^\circ$
 $\beta=90.000^\circ$
 $\gamma=90.000^\circ$

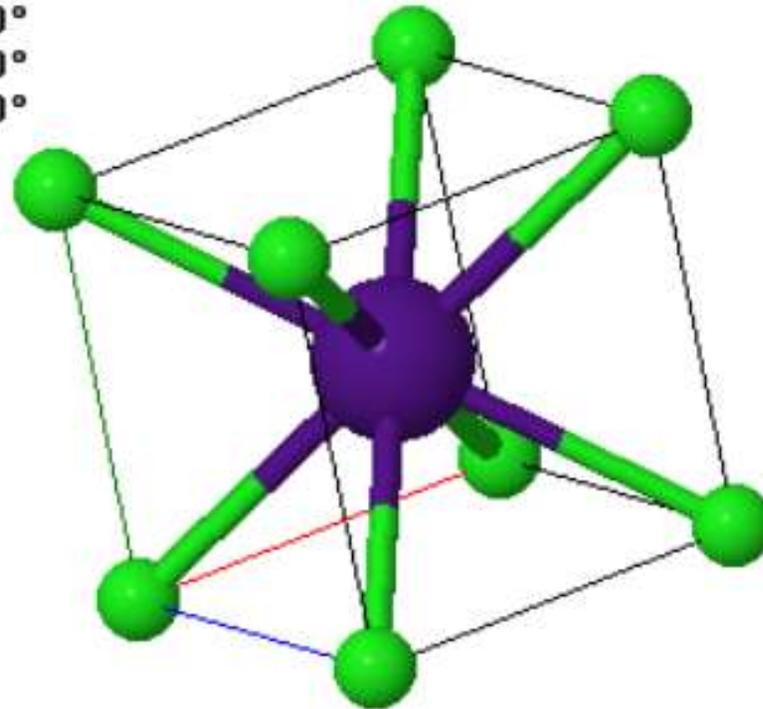


Number 225

Bravais: fcc

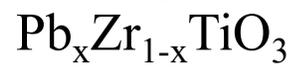
CsCl

HM: PM-3M
a=4.110Å
b=4.110Å
c=4.110Å
 $\alpha=90.000^\circ$
 $\beta=90.000^\circ$
 $\gamma=90.000^\circ$

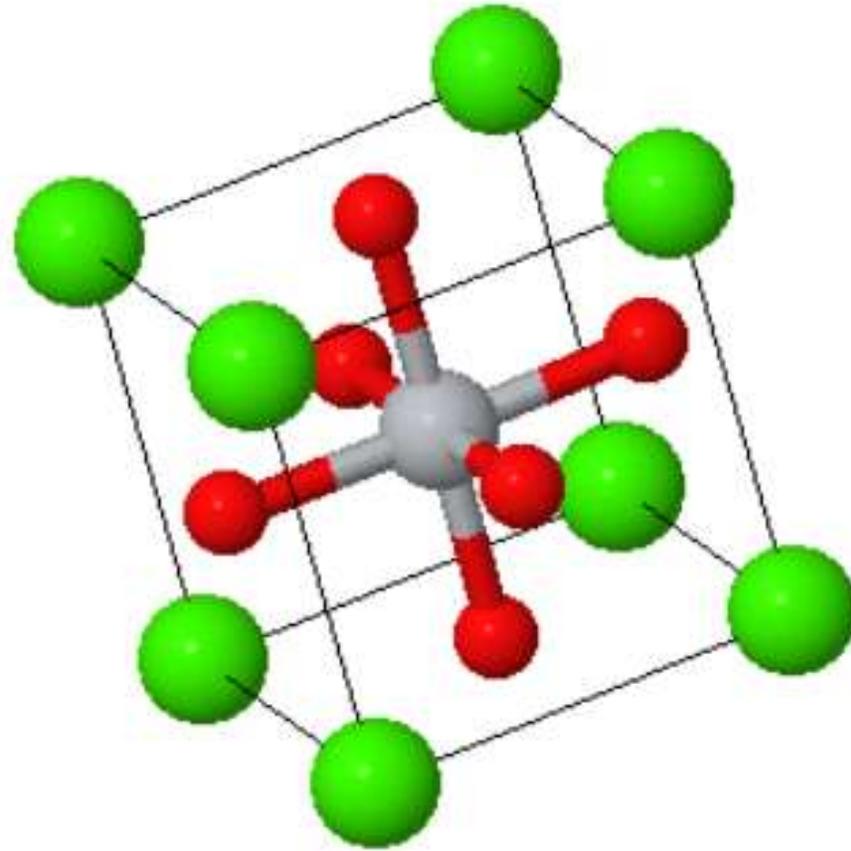


Number 221

perovskite

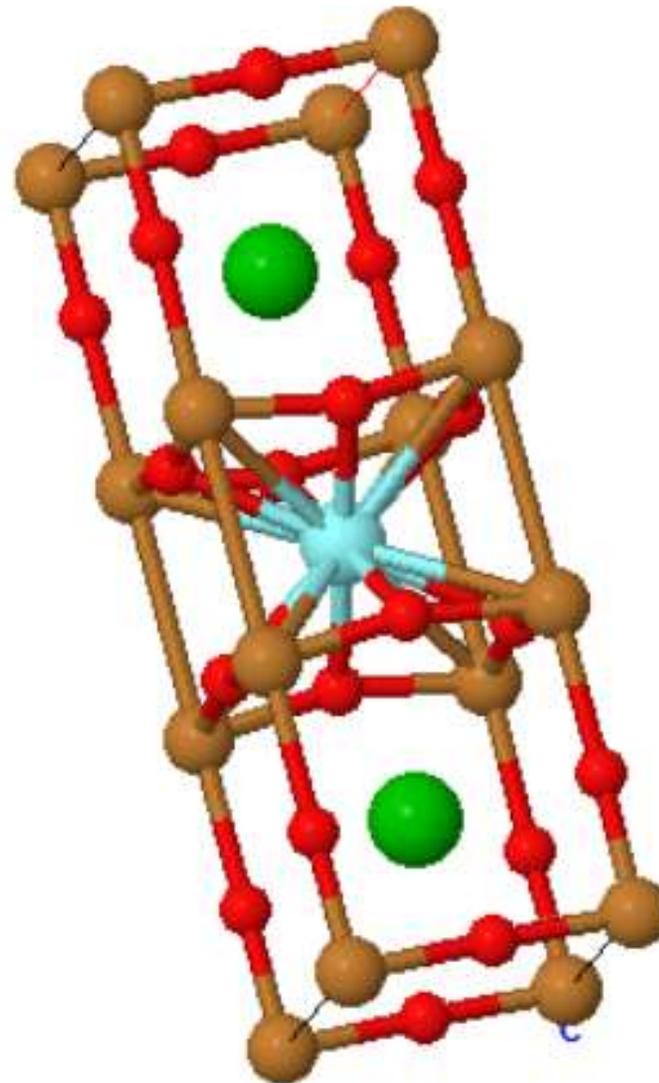


Number 221
simple cubic





HM: P m m m
a=3.820Å
b=3.885Å
c=11.683Å
α=90.000°
β=90.000°
γ=90.000°



Number 47